JC10 2001/PTO 2 2 JUN 2001.

FORM PTO-1390 ; (REV. 11-94) U.S. DEPARTMENT OF COMMERCE PATENT AND TRADEMARK OFFICE

ATTORNEY'S DOCKET NUMBER

# TRANSMITTAL LETTER TO THE UNITED STATES DESIGNATED/ELECTED OFFICE (DO/EO/US)

9392-016-999

09/86898**T** 

INTERNATIONAL APPLICATION NO. PCT/US99/30640

INTERNATIONAL FILING DATE December 22, 1999

PRIORITY DATE CLAIMED December 22, 1998

TITLE OF INVENTION

A SYSTEM AND METHOD FOR THE ANALYSIS AND PREDICTION OF ECONOMIC MARKETS

APPLICANT(S) FOR DO/EO/US

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Applicant herewith submits to the United States Designated/ Elected Office (DO/EO/US) the following items under 35 U.S.C. 371:

- This is a FIRST submission of items concerning a filing under 35 U.S.C. 371.
- 3. This is an express request to begin national examination procedures (35 U.S.C. 371(f)) at any time rather than delay examination until the expiration of the applicable time limit set in 35 U.S.C. 371(b) and PCT Articles 22 and 39(1).
- 4. 

  A proper Demand for International Preliminary Examination was made by the 19th month from the earliest claimed priority date.
- 5. 

  ✓ A copy of the International Application as filed (35 U.S.C. 371(c)(2))
  - a.  $\Box$  is transmitted herewith (required only if not transmitted by the international Bureau).
  - b.  $\square$  has been transmitted by the International Bureau.
  - c. 

    is not required, as the application was filed in the United States Receiving Office (RO/US)
- 6. 

  A translation of the International Application into English (35 U.S.C. 371(c)(2)).
- 7. 

  Amendments to the claims of the International Application under PCT Article 19 (35 U.S.C. 371(c)(3))
  - a.  $\square$  are transmitted herewith (required only if not transmitted by the International Bureau).
  - b. □ have been transmitted by the International Bureaus.
  - c.  $\Box$  have not been made; however, the time limit for making such amendments has NOT expired.
  - d. Me have not been made and will not be made.
- 8. 

  A translation of the amendments to the claims under PCT Article 19 (35 U.S.C. 37(c)(3)).
- 10. 

  A translation of the annexes to the International Preliminary Examination Report under PCT Article 36 (35 U.S.C. 371(c)(5)).

### Items 11. to 16. below concern document(s) or information included:

- 11. 

  An Information Disclosure Statement under 37 CFR 1.97 and 1.98.
- 12. 

  An assignment document for recording. A separate cover sheet in compliance with 37 CFR 3.28 and 3.31 is included.
- 13. 

  A FIRST preliminary amendment.
  - □ A SECOND or SUBSEQUENT preliminary amendment.
- 14. □ A substitute specification.
- 15. 

  A change of power of attorney and/or address letter.
- 16. Other items or information:

JC18 Reo'd PCT/PTO 222 JUN 2001

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December 22, 1999							
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	INDEPENDENT CLAIMS	18 - 3	15	X \$ 80.00		1,200.00	
	MULTIPLE DEPENDENT CLAIM(S) (if applicable) + \$ 270.00						
	BASIC NATIONAL FEE (37 CFR 1.492(a)(1)-(5)):  CHECK ONE BOX ONLY  International preliminary examination fee paid to USPTO (37 CFR 1.482)				\$	690.00	
	□ No international preliminary examination fee paid to USPTO (37 CFR 1.482) but international search fee paid to USPTO (37 CFR 1.445(a)(2))				\$	0.00	
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	☐ Filing with EPO or JPO search report				\$	0.00	
	Surcharge of \$130.00 for furnishing the National fee or oath or declaration later than □ 20 ⋈ 30 mos. from the earliest claimed priority date (37 CFR 1.492(e)).				\$	130.00	
			TOTAL OF ABOVE	CALCULATIONS	=	3,460.00	
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<ul> <li>18. □ Other instructions n/a</li> <li>19. ☒ All correspondence for this application should be mailed to</li> </ul>							
PENNIE & EDMONDS LLP  1667 K STREET, N.W.  WASHINGTON, D.C. 20006  20.   ■ All telephone inquiries should be made to (202) 496-4478							
for: Francis E. Morris (Reg. No. 24,615)  August  Augu							
NAME SIGNATURE 43,639 REGISTRATION NUMBER					June 22 DATE	, 2001	

## Rec'd PCT/PTO 22 JUL 2001

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## A SYSTEM AND METHOD FOR THE ANALYSIS AND PREDICTION OF ECONOMIC MARKETS

#### FIELD OF THE INVENTION

The present invention relates generally to a method and system for the analysis and prediction of economic markets. More particularly, the present invention forms a search space of different economic models, forms a fitness landscape by extracting observables from executions of the economic models with dimension reduction and by comparing the observables with actual data, and performs model selection and composite model synthesis through optimization over the fitness landscape.

#### BACKGROUND

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The stock market and non financial markets are complex systems in which one or more stocks, goods, services, or their derivatives are sold or bought. Many techniques exist that attempt to analyze expected behavior of these markets, including predictions of price and volatility for a forward time series from any given date. Among these methods are those concerning prediction of volatility based on Black Scholes, and implied volatility given prices of options and the assumptions of Gaussian random walks in prices that are used to back estimate the volatility implied by actual option prices. In addition, procedures exist which posit some mathematical form for a feature such as volatility, such as truncated Levy, or Levy, or other distributions, then attempts to fit observed volatility distributions using these assumed underlying distributions and appropriate weighting of coefficients in the given mathematical form.

Still other attempts to predict expected volatility uses Black Scholes formalism but treats variance in price as

itself a random variable which changes over time, then

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attempts to estimate the rate of change of this random variable. Still other efforts to predict volatility are based on causal models of various kinds. For example, some workers postulate a "herding" effect in which clusters of 5 traders of various sizes form and trade in much the same way, causing small and large fluctuations in price, hence in volatility. Other attempts are based on Langevain equations which represent displacement of buy and sell orders at a moment from "equilibrium", then seek stochastic equations 10 describing the change of this displacement as a function of drift terms, price momentum terms, penalties for price variance, and volatility growth terms. Still other efforts are based on local linear models which embed a single stock's price series, or sometimes several price series, in a 15 multidimensional space of the past N periods and attempts to locally fit the next price move of one or several prices.

The predictive capability of each of these economic model can vary with the economic environment. Specifically, an economic model may exhibit a good predictive capability for one set of economic circumstances and a poor predictive capability for another set of economic circumstances. Since the economic environment changes with time, the utility of each economic model also changes with time.

A great many researchers in economics, finance, and related areas have investigated different aspects of financial markets or markets in general. Topics of interest to the researchers and of relevance to our project have included diffusion of information in markets (Kyle, Albert S. (1985): "Continuous Auctions and Insider Trading,"

30 Econometrica, v. 57, 1315-35, Grossman, Sanford J., and Joseph E. Stiglitz (1980): "On the Impossibility of Informationally Efficient Markets," The American Economic

Review, v. 70,393-408), efficiency and statistical modeling of markets (Foley (1982)), speculation and bubble formation (Tirole, Jean (1982): "On the Possibility of Speculation Under Rational Expectations, " Econometrica, v. 50, 1163-81.

5 ), and many others.

Other existing work in market microstructure theory (O'Hara Blackwell, Maureen, Market Microstructure Theory, Cambridge, MA, 1995.) suffers from a lack of means for experimental verification (with some important exceptions, such as (Rust, John, John Miner, and Richard Palmer (1993): "Behavior of Trading Automata in a computerized Double Auction Market", in The Double Auction Market). For example, Glosten-Milgrom (GM) model examines the relationship between Dealer spreads and the proportion of informed Investors in the market. But it is very difficult to quantify the fundamental concept of "proportion of informed investors in the market" Ideally, one would prefer a numerical and experimental framework in which one could examine the regions of validity of analytic models like the GM.

Another important shortcoming of the existing literature is the static nature of most of the models, i.e., results even for dynamic models are usually derived using some type of equilibrium assumptions. Such assumptions greatly limit one's ability to investigate dynamic,

25 potentially non-equilibrium behavior of the system, and also one's ability to model realistically the market participants and as the result the market itself.

Accordingly, there exists a need for a broad encompassing algorithmic framework to develop effective and routinely improvable models and predictions of economic markets including stock markets and non-securities markets. In addition, there exists a need for a broad and improvable

algorithmic framework to seek means to price securities such as options and other derivatives.

There exists a further need for a system for performing analysis and making predictions in a securities 5 market using an agent-based models of the dealers and investors.

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#### SUMMARY OF THE INVENTION

The present invention presents a system and method of economic analysis and prediction which dynamically adapts to a changing economic environment by selecting or synthesizing an economic model from a set of economic models based on the selected model's ability to make accurate predictions about an actual economic market. Specifically, the method and system of the present invention forms a space of different economic models, forms a fitness landscape by extracting observables from executions of the economic models, and performs model selection and composite model synthesis through optimization over the fitness landscape.

The present invention includes a method for 15 performing analysis and prediction of economic markets comprising the steps of:

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initializing a space of economic models;
executing one or more of said economic models to
generate a corresponding one or more predicted time series;

determining one or more fitnesses corresponding to said one or more economic models by comparing said plurality of predicted time series to actual data; and

searching for at least one of said economic models having a maximal fitness.

The present invention further includes a system for performing analysis and making predictions of a securities market comprising

a model of the securities market comprising:

a plurality of dealer agents representing a corresponding plurality of market makers in the securities market, each of said dealer agents having at least one of a

plurality of dealer strategies for setting a price of securities;

a plurality of investor agents representing a corresponding plurality of investors in the securities

5 market, wherein said investor agent determines whether to buy or sell one or more of the securities at a given price;

at least one market model comprising one or more rules for exchanging the securities; and

a simulator for executing said model to perform 10 analysis on the securities market.

The present invention further includes a method for creating a portfolio of assets comprising the steps of:

initializing at lease one current portfolio of assets having one or more desired properties;

generating at least one next portfolio of assets to form said current portfolio, said next portfolio having a smaller size then said current portfolio;

repeating said generating step after replacing said current portfolio with said next portfolio while said next 20 portfolio has the one or more desired properties;

defining a size range having an upper limit equal to the size of said current portfolio and a lower limit equal to the size of said next portfolio; and

searching for an optimal portfolio of assets to 25 within said size range.

The present invention further includes a method for optimizing a portfolio of assets comprising the steps of:

determining a fitness landscape representation over a space of portfolios;

determining at least one optimal searching distance in said fitness landscape representation; and

searching for optional ones of said portfolio of assets at said optimal distances.

The present invention further includes a method for creating a portfolio of a plurality of assets comprising the 5 steps of:

determining a plurality of anti-correlated families wherein each of said anti-correlated families contains two or more of said plurality of assets that are anti-correlated; and

determining one or a more perspective portfolios of said plurality of assets from said plurality of anti-correlated families.

The present invention further includes a method of modeling a portfolio of assets comprising the step of:

defining a probability distribution of the value of the portfolio of assets with two or more Gaussian distributions.

### BRIEF DESCRIPTION OF THE DRAWINGS

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FIG. 1 provides a data flow diagram describing a framework of the system and method of economic analysis and prediction of the present invention.

25 FIG. 2 shows a screen shot of the simulation of the dealer-mediated securities market model.

FIG. 3 shows the behavior of the population of Basic Dealers for different tick sizes.

FIG. 4 displays the results of the dealer mediated securities market model for a market consisting of 7 Basic Dealers and one parasite.

FIG. 5 displays the results of the dealer mediated securities market model for a market with a mixed population of dealers.

- FIG. 6 shows graphs of RMS(bid True Value) and 5 RMS(ask True Value) as a function of the tick size for different populations of Market Makers in the dealer-mediated securities market model.
- FIG. 7 shows the average value of the spread as a function of the tick size for different combinations of the 10 market makers in the dealer-mediated securities market model.
  - FIG. 8 shows a graph of the standard deviation of the spread size as a function of the tick size for different populations of Market Makers in the dealer-mediated securities market model.
- FIG. 9 displays the main simulation control window of the dealer-mediated securities market model.
  - FIG. 10 displays the Options menu of the dealer-mediated securities market model.
- FIG. 11 displays the Set Human Dealer Prices panel 20 and the Set Tick Size panel of the dealer-mediated securities market model.
  - FIG. 12 displays the "Show True Value" panel and the "trade history" panel of the dealer-mediated securities market model.
- FIG. 13 displays the "graphs menu" of the dealermediated securities market model.
  - FIG. 14 displays the "cash bar graph" panel of the dealer mediated securities market model.
- FIG. 15 displays the "Inventory Bar Graph" panel  $_{30}$  of the dealer-mediated securities market model.
  - FIG. 16 displays the "Supply and Demand Graph" panel of the dealer-mediated securities market model.

- FIG. 17 displays the "All Dealer Cash" graph of the dealer-mediated securities market model.
- FIG. 18 displays the "Dealer Assets" panel of the dealer-mediated securities market model.
- FIG. 19 shows the Dealer Inventory graph of the dealer-mediated securities market model.
  - FIG. 20 displays a panel showing how the dealers track the true value reasonably well in the dealer-mediated securities market model.
- 10 FIG. 21 displays a panel showing the simulation results for a smaller tick size in the dealer-mediated securities market model.
  - FIG. 22 displays a panel of results obtained by executing the dealer mediated securities market model.
- FIG. 23 provides a flow diagram of a method for evaluating and minimizing risk.
  - FIG. 24 provides the results of the method for evaluating and minimizing risk from executing on 500,000 random draws from this "toy" world.
- FIG. 25 displays the histograms that determine the number of children to draw from during execution of the method for evaluating and minimizing risk.
  - FIG. 26 displays a flowchart illustrating the method for portfolio modification.
- FIGs. 27, 28a and 28b display families of anticorrelated stocks that were generated by a method to create a portfolio of a plurality of assets with minimal risk.
- FIG. 29 displays a picture illustrating the anticorrelation relationship among family members that was 30 generated by a method to create a portfolio of a plurality of assets with minimal risk.

FIG. 30 discloses a representative computer system 3010 in conjunction with which the embodiments of the present invention may be implemented.

## DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

#### System Framework

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FIG. 1 provides a data flow diagram describing an overview of the system and method of economic analysis and 10 prediction of the present invention. In step 110, the method executes each economic model 105 in a set of economic models to form a corresponding family of predicted time series of desired features 115. Without limitation, the economic models 105 include a variety of different model types such as 15 parameterized models, agent-based causal models, aggregate causal models, and intermediate causal models. The economic models 105 further include models based on a variety of data mining tools such as time series analysis. The economic models 105 also include causal models based on features such 20 as the economic web model in which N stocks are located, hence the sensitivity of the values of the stock to the introduction of new goods and services and the extinction of old ones as described in copending patent application, "System and Method for the Synthesis of an Economic Web and 25 the Identification of New Market Niches", U.S. Application Number 09/080,040, filed 5/15/98, the contents of which are herein incorporated by reference. The economic web models are further described in "A System and Method for Coordinating Economic Activities Within and Between Economic 30 Agents", U.S. Application Number 60/091,656 and International Application number PCT/US99/15096, the contents of which are herein incorporated by reference.

The economic models 105 further include causal models based on detailed agent based models of the "players" in a stock market, such as dealers, traders, plus their order books, plans and facts concerning wishes to buy or sell stocks or derivatives as characterized by a finite list of features including price, volume, strike price, dates, underlying value of the stock by various estimates, and other factors. In addition, these agent based models may include strategy spaces for the different agents, means by which agents change strategies, and may include sets of hypotheses that agents hold with respect to other agents prospective actions, other agent's strategies, and other agents hypotheses. Specific examples of economic models 105 include AR(n), ARMA, ARV, ARCH, GARCH, BlackScholes,

models 105 is broad and indefinitely extendable.

The execution of step 110 yields time series data for models 105 having the same types and different parameter

values, models having different types, etc. For the agent
20 based models in the set of economic models 105, step 110
executes on models with different strategy spaces, different
inventory requirements, different preferences, etc. For the
agent based models where the agents have different models of
each other, step 110 executes with different sets of rules

- which define how the models of the agents change over time. Since the models change with time, step 110 executes the set of economic models 105 for different time periods. For example, step 110 could be executed for a time period beginning 10 years ago and running until the present time.
- 30 Likewise, step 110 could also be executed for a time period beginning 1 year ago and running to the present time.

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In step 120, the method extracts a set of observables from the predicted time series and corresponding time series of the actual economic market to create a fitness landscape 125 of the space of economic models 105. Execution 5 of step 120 yields metric distances between different models for different time periods. Specifically, execution of step 120 yields metric distances between models having the same type and different parameter values, models with different strategy spaces, models with different inventory requirements, different preferences, etc.

The method extracts a set of observables from the families of predicted time series and creates a fitness landscape using a wide variety of data mining techniques and dimension reduction techniques. Dimension reduction

- principal component analysis, independent component analysis and the sparse basis of landscapes as described in copending patent application, "A System and Method for Coordinating Economic Activities Within and Between Economic Agents", U.S.
- 20 Application Number 60/091,656 and International Application Number PCT/US99/15096, the contents of which are herein incorporated by reference.

In an alternate embodiment, step 120 computes probability distributions for the observables for the 25 families of predicted time series. In this embodiment, step 120 computes a comparison between different probability distributions to approximate metric distances between corresponding predicted time series. Preferably, the Randan-Nikodyn Thereom is used to approximate the metric distance.

 $_{
m 30}$  Alternatively, the Kulback-Liebler method could be used. However, as is understood by persons of ordinary skill in the

art, other techniques could be used to compare probability distributions and approximate their metric distances.

Execution of step 120 assesses a given state of an economic market. Without limitation, that current state

5 might be an embedding of the current and N past day's prices of M stocks in an (N+1)M dimensional state space showing by a single point the entire history of all M prices over the past N +1 periods. The current state of the market, however, may be broader, and include prices, volumes, and other desired

10 features of the stocks or goods sold and bought. The current state might be the present state, or a past historical state or a proposed future hypothetical or expected state of the market. More generally, the embedding might include the N+1 past moments and F future moments or periods, as sampled from 15 historical data such that the state space has (N+1+F) \* M dimensions.

Again at the highest level, the chosen model is utilized, together with an assessment of the current state of the market, to predict one or more successive states of the 20 market. This process may be used a single time to predict, for example, a time series of the M stocks for P succeeding periods, where P is 1 or more, and periods are chosen as desired for past and future analysis.

More generally, the predicted future time series

25 might be reformed deterministically, or stochastically, from
the current state based on features of the model's mapping of
past to future states. Thus, for a local linear method, the
statistical features of a mapping of a set of neighboring
past points to a set of future points in the (N + 1 + F)M

30 state space is used to pick, stochastically predicted future
points from the current state to, generally, a plurality of

different members of "walks" from the current state into the future.

The ensemble of these walks may then be used to measure features such as price. More particularly, the 5 ensemble of these walks, or partial differential equations based on the cumulants of the ensemble can be used to characterize the ensemble. Based on numerical study, or the partial differential equations, the ensemble can be used to assess hedging, risk minimization to a single option, or a 10 portfolio of holdings.

In addition to the use of one or an ensemble of predicted future price series, or time series of other features such as volume and otherwise to assess risk and proper prices for options and other instruments, the 15 predicted time series can be compared to the observed behavior of the real market 118 in order to test, modify and improve the initial choice of model for the market.

At the highest level, this testing procedure consists in the use of one or more comparisons between the predicted time series 115 and actual time series 118, as assessed by features as simple as direct visual comparison, to principal component analysis, independent component analysis and other sophisticated modes of comparison of data sets. These comparisons yield one or more "errors", that measure different aspects of the deviation of the predicted behavior of the market to the observed behavior of the market.

Given a set of errors, the highest level algorithm constructs a "fitness measure" of the model in step 120. This fitness measure may, in general, consist in a single number, or might be a vector with all of the different features of

errors noted by the comparison of fact and model predictions, or a still more general measure of fitness of the model.

Again at this highest level, the fitness measure or measures creates a fitness landscape 125 over the set of 5 models 105 of the market. Given any one of a plurality of means of defining "nearby models", the most general algorithm achieves a space of models of the market. Since each model has a fitness, given the space of models 105, the algorithm achieves a fitness landscape 125 over the space of models 10 105. In this fitness landscape 125, it is natural to represent minimization of errors by being fitter, and allow the error measures to be a height. Hence, in this formulation, "fitter" is lower, corresponding to lower errors. Without loss of generality, fitter can be taken as 15 higher by reformulating the error measures. Without loss of generality, let "high" be fitter than "low", so peaks represent high fitness and thus, low error. Then the fitness landscape 125 may, in general, be smooth and single peaked, rugged and many peaked but correlated, with correlations 20 lengths that differ in different directions, or random. Means to search a landscape, to characterize and to represent a landscape are described in copending patent application, "A System and Method for Coordinating Economic Activities Within and Between Economic Agents", U.S. Application Number

25 60/091,656 and International Application Number PCT/US99/15096, the contents of which are herein incorporated by reference.

In step 130, at the highest level, the algorithm utilizes, first, means to assess the statistical structure of the fitness landscape 125 over the space of models 105 of the market, such as its correlation lengths in different directions. The algorithm determines the optimal search

distance as a function of the current fitness of a model of the market and the correlation structure of the landscape, etc. as described in "A Method for Optimal Search on a Technology landscape", International Application

- 5 PCT/US99/19916, filed August 31, 1999, the contents of which are herein incorporated by reference. Then, based on these features, the highest level algorithm chooses, by mutation, recombination, or other methods, a new trial model of the market to test and assess the fitness of that model.
- In step 130, over a succession of trials, the highest level algorithm searches for fitter models of the market. In general, this search procedure may be a local walk via fitter neighbor variants that becomes trapped on a local fitness peak in the space of models of the market or a
- 15 more general search procedure that persistently searches in a space of models, generates new models, and continues to search for good models. This persistent search in the space of models in part reflects the fact that the market itself may be persistently non\_stationary. For example, its rules
- algorithm can tune the rate of search in the space of models to match the non\_stationarity of the market itself such that the search procedure persistently finds good models of the market.
- In addition, at this highest level, the economic models 105 may be algorithmically augmented by a variety of algorithmic procedures such as changes in the coefficients of a model or changes in the functional mathematical form of a model. For example, step 130 can alter a term in an equation from linear to squared, or generate entirely new models by mutation and recombination of terms and elements or agents

that are present in existing models.

In step 130, the method searches the space of economic models and synthesizes new economic models 135. The search and synthesis step 130 will also include the use of a stacking function. The stacking functions can be arbitrary functions of the models of the system. Genetic operators such as recombination and mutation operate over the space of stacking functions to produce new composite economic models 135. The stacking functions must have adequate diversity to span the dimensionality of the behavior space.

The scope of some of the searches from step 130 will be restricted to intra-class searches. These searches include the refinement of parameters for parameter type models by comparing the actual data 118 with the families of predicted time series data generated by the model. In other words, the fitness of each economic model 105 is the metric distance of its predicted time series 115 from the actual time series 118.

The search and synthesis step 130 will also include the use of biological functions. The use of biological functions produces hybrid economic models 105 which are composed of individual economic models. Each individual component economic models 105 contributes a portion of the predictive time series data produced by the hybrid economic model 105. The biological functions adjusts the permutation and percentage contribution of each component economic model 105 in the hybrid economic model 105.

The extraction of observables from ensembles of time series generated from hybrid economic models 105 and composite economic models 105 can be done in different

manners. In one exemplary technique, the method takes a weighted sum of each of the component economic models 105 and subsequently performs extraction of the observables. In an

alternate technique, the method performs extraction of the observables for each component economic model 105 and subsequently takes of weighted sum of these sets of observables.

The non-stationarity of economic markets will induce a flow in the behavior space created by step 120. Specifically, the values of the observables extracted through the data mining and dimension reduction process will change with the economic markets. The present invention can be used to analyze the non-stationarity of the economic markets by studying the flow in the behavioral space. In turn, the present invention can be used to predict the non-stationarity of the economic markets from the observed flow in the behavioral space.

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Algorithmic Procedures for Options, Hedging and Other Investment Decisions

Different economic models 105 can be used with the framework of the system and method of the invention shown in 20 FIG. 1. A set of past time series and matching statistics forms an exemplary economic model 105. This process begins, without limitation, with a time series at some fixed interval, say a day, or an hour, or a week, with the prices of one or more assets, say of N different stocks. For each 25 stock, there exists the past time values at the current price at time T, the price at T - I, T -2, .T -3, .....T - tau. In addition, there exists the future time prices T + 1, T + 2, T + 3, ....T + tau. In addition to merely including price information at these different times, it is possible to 30 include further information such as volume and price per trade at these different times, or lumped into small intervals of time "boxes". In addition, it is possible to

include other features such as measures of expectations of changes in interest rate, or the deviation of an index such as the DJIA above or below its average value for some past period or periods. It is possible in addition to include measures of concern over political events, economic events etc.

Without limitation, and for ease of description only, we now consider the case where only the prices of N assets for the past and future 2 x tau + 1 time moments are considered. This data is obtained from the actual historical data record for different moments, T, chosen, for example on different days in the past year or several years or more. The accumulation of these data yield a mathematical state space structure which has a "past" a "now" and a "future". The dimensionality of this state space is N (2xtau + 1). Thus, if tau is chosen to be 4, meaning using data on prices from the moment T, back to T - 1, T -2, T -3, T-4 and forward to T +1, ...T+ 4, then each asset corresponds to 9 prices, or 9 variables, and the total state space has 9N dimensions.

Accumulation of data over a past set of times, say the past several years at daily intervals, will yield a set of points, one for each moment in the past chosen as "now". In general, nearby "past" points will have more or less nearby "future" points. Thus these data clouds of lumped nearby past and future points convey some information about the mapping from past to future in this state space.

In particular, the mapping from a nearby set of "past" points to their corresponding "future" points will be used in the present algorithm to generate a stochastic process that, at each step from a "now" point, matches the local statistics of the past - future mapping.

In general, the number of sampled points in this state space will be sparse. Interpolation procedures will be useful for the present algorithm which will yield good approximations to the statistics of "past" - "future" 5 mappings for points in the state space that have not been sampled. In general, markov random fields and other procedures introduced below allow this interpolation before or during the stochastic process next constructed from this" "past", now, future high dimensional state space.

The next step in the algorithm begins at any chosen date, in particular, the actual current historical date, and utilizes the state space to generate a "walk" beginning at the actual or chosen "now", and choosing a "next price" randomly to fit the local statistics of "past", "Now,

15 "future" prices in its vicinity of the state space. This random choice moves generates at next "mock" price at mock T + 1, hence at a new point in the state space corresponding to

the new price, and the new change in price, i.e. price at T - price at T - 1, price at ....T - 2, ...T - tau. Thus, the new 20 mock price generates not only a new price, but locates the stochastic process at a new point in the "past" of the state space.

From the new point in the past of the state space, the stochastic process chooses at random, a mock future price matching the statistics of the future from this new point in the past in the state space. This stochastic process is iterated as many times as desired to yield a mock time series of "future" prices of the set of N assets from the initial position, "now" in the state space.

The next step in the algorithm generates a second "mock time series" from the same initial position, "now" in the state space. The algorithm then generates as many mock

time series from the same initial position, "now" in the state space.

The family of mock time series forms the basis for 5 all further evaluations of investment and hedging strategies, as well as measures of volatility, and means to obtain options prices. For example, using this family of mock time series, coupled with an assumed option, date of sale and strike price, one can numerically investigate the expected 10 return on that option for each member of the mock time series, hence can derive the average and the higher moments of the return on the option over the family of mock time series. Since there are a finite, but indefinitely large number, of members of the mock family of time series, it is always possible to obtain these expected values on the mean, variance, and higher moments.

More generally, the motions in the state space exhibit the correlations in price and price changes among the N assets. Thus the family of mock time series can be used to construct good hedging strategies. More, the use of genetic algorithms and other procedures known in the art can be used to choose optimal hedging strategies among the N assets and their derivatives, given performance criteria such as risk aversion, and other desired features of the instrument.

Further, in general, the real markets are nonstationary. Thus, in general, over real time the mapping
known "Past" to "Future" of the state space changes. These
changes can be thought of as a higher order map that
transforms the "Future" of the state space onto itself. This
higher order map can be created as a Tensor process mapping
the "Future" state space onto itself. In turn, the Tensor
mapping may not be stationary, and a still higher order

mapping of the Tensor onto itself can be created. These Tensor-Tensor maps are then used to modify the state space "over time" from the "initial now" to generate an improved family of mock/time series.

Indeed, the first construction of the state spare used historical data over, for example, the past several years. The market mapping of "past to future" is, in general, non-stationary over this historical past. Nearby points in the "past" in the state space correspond, in general to real time points that may be separated by months or years. Thus the "dispersion" of "Future" data points may reflect randomness of the market at any one time, or the non-stationarity over time.

The "Tensor" method of mapping the "future" of the state space onto itself can be used to analyze and improve the initial state space by partitioning the state space into real time segments, each having a modest length, (i.e. 1 month compared to several years - say 10 years). Then the 12 x 10 = 120 "past-future" state space maps can be compared via the "Future - Future" tensor matching procedure to find; estimate and modify the initial "past - now - future" state space to achieve an improved "Tensor" mapping and higher order mapping to use to generate families of mock time series upon which asset strategies and pricing can be based.

25

#### Modeling and Simulation

The space of economic models 105 of the present invention goes far beyond simply fitting time series to stochastic models. Such approaches, including AR[n], ARV, ARMA, ARCH, GARCH, LSSM, Levy, and truncated Levy models, merely fit the data (usually of a stock price, or of price

differences) to a mathematical model. Then that model is used in various ways for volatility prediction, risk assessment, option pricing, and optimal hedging. But those models generally have little or no basis in how markets really work, and treat the price data merely as a mathematical time series to be analyzed and fitted.

In contrast, causal models include ideas, represented in equations, about how markets really work, and about how agents in those markets make decisions. The observed data, such as the price as a function of time, is then understood in terms of its underlying causes, not just as a set of numbers. By refining and calibrating our causal models against real-world information and data on market and agent behavior, we can obtain a much better understanding of price series than models without any causal mechanisms. This better understanding in turn provides more predictive power, and thus improved volatility prediction, risk assessment, option pricing, and optimal hedging.

Our causal models of markets span three levels of 20 modeling detail:

- 1. Individual Agent Level
- 2. Agent Distribution Level
- 3. Aggregate Level

These are discussed in more detail below. The present invention uses models at all three levels. The present invention calibrates models at levels 1 and 2 against each other, and similarly at levels 2 and 3.

The division into three levels is actually somewhat arbitrary. In particular, there are many possible levels of detail within level 2, and many hybrid cases between levels 2 and 3 in which some variables are modeled as distributions and some as aggregates.

The individual agent level models represent (in the computer) individual agents who buy and sell securities.

These agents can include investors, brokers, specialists, and market makers. The security prices are determined by the sectivity of the agents, either through specific specialist or market-maker strategies, or through tatonnment rules in which the price of a security moves upwards when demand exceeds supply and downwards when supply exceeds demand.

The agents each have a current portfolio (or

10 "inventory") of holdings in each of a number of financial securities (stocks, bonds, options, etc), and also have available reserves of liquid assets ("cash"). They change their portfolio, buying and selling securities, according to a current "strategy". These strategies may be represented by parameterized rules, a neural network, or fuzzy logic. The strategies, however represented, may involve agents' internal predictions of the future behavior of the market and/or of other agents.

Each agent may contain a set of many different

20 strategies at the same time, using those that seem, on the basis of past experience, best under any particular circumstances. Alternatively a weighted average of the set of strategies may be used, weighting each according to its observed past success and generating composite or intermediate actions.

In general the set of strategies, and the individual strategies within the set, change through time as internal models are refined through learning, and as different approaches are found to be more or less successful.

30 Entirely new strategies are generated using genetic algorithm and similar evolutionary programming techniques. The new strategies replace old unsuccessful ones.

At the opposite extreme, the least detailed level, the models at the aggregate level compress the behavior of the agents into one or a few aggregate variables. There is no representation of individual agents, but their average or

- 5 aggregate behavior is represented. These are much simpler mathematically than the individual agent models. These models are further described in R. Cont and J.-P. Bouchaud, Herd Behavior and Aggregate Fluctuations in Financial Markets, preprint cond-mat197123i8, available from
- 10 http://xxx.J.anl.gov, 1998, the contents of which are herein incorporated by reference. The models at the aggregate level are further described in J.-P. Bouchaud and R. Cont, A Langevin Approach to Stock Market Fluctuations and Crashes, preprint cond-mat/9801279, available from
- 15 http://xxx.lanl.gov, 1998, the contents of which are herein incorporated by reference.

The models at the aggregate level usually consist of a small number of coupled nonlinear differential or difference equations, some of which involve stochastic

- forces. Overall, these are Langevin-type equations in the terminology of physics. Some terms in these equations may also involve integrals or averages over past behavior, usually in the form of weighted moving averages. Analytical methods of the Ito calculus, including construction of
- 25 Fokker-Planck equations, may be applied in some cases, but in general numerical solutions are used.

The aggregate variables that appear in the equations may include (but are not limited to):

aggregate demand-the total number of shares that
 the trader agents want to buy, minus the total
 number that they want to sell.

 inventory level-the total amount of inventory (counting short sales as negative) that the marketmaker or specialist agents currently hold.

- 3. average investor confidence-a "psychological"
  variable depending on the recent stability or
  predictability of the market, and affecting the
  agents' risk aversion (their balance between desire
  for expected profit and avoidance of loss).
  Similar variables may also be used for marketmakers or specialists.
  - 4. average net capital entry rate-the average rate at which new capital enters the market, less the exit rate.
- 15 Besides these and other agent-aggregate variables, there are of course pure market variables, including price, price trend, price volatility, price kurtosis, price correlation time, and the corresponding quantities for price differences and squared prices. There are also adjustable parameters in the model, including parameters to represent average growth rates, average shock and noise rates, strengths of couplings between various pairs of variables, etc.

Together the coupled equations produce a causal model of the agents' aggregate behavior and the market's response. In fact each drives the other; the market reflects the behavior of the agents, and the agents take their cues from the market.

At the intermediate level of detail of the models at the distribution level, the fundamental variables are distributions of aggregate quantities, such as those listed above for the aggregate level. These distributions are used in two ways:

to represent the variation of a quantity (such as average investor confidence) or a parameter (such as risk aversion, or trading lot size) across agents;

5 2. to capture the uncertainty of such a quantity or parameter through time, in the form of a probability distribution.

By using distributions rather than single aggregate quantities, we can model real agents and markets much more

- 10 realistically, without needing to go all the way to the individual agent level. It seems indeed almost essential to have a distribution of large and small trades in order to fit the observed non-Gaussian distribution of stock price changes. Having a fixed size leads (according to the central
- 15 limit theorem) to Gaussian price changes unless "herd" effects are invoked as described in R. Cont and J.-P. Bouchaud, Herd Behavior and Aggregate Fluctuations in Financial Markets, preprint cond-mat197123i8, available from http://xxx.J.anl. gov, 1998 (the contents of which are herein
- 20 incorporated by reference), and a herd acting together is effectively creating a large trading block in any case.

The equations for the distributions are derived from the corresponding Langevin-type equations for the variables whose distributions we are representing. This

- leads to coupled differential or difference Master Equations, with convolution integrals involved in the coupling between variables. In most cases, the present invention replaces these Master Equations by coupled differential or difference equations for the cumulant moments of the distributions
- 30 involved, truncating the cumulant expansion after the first few terms (keeping at least 4 terms, up to at least the kurtosis). This procedure leads to algebraic evolution

equations for the cumulants, enabling us to predict, for example, the price distribution of a stock.

At the individual agent level, and at the aggregate level, the causal models produce time series of securities

5 prices as a result of agent behavior and trading.

Preferably, the models are run many times in order to obtain an ensemble of such time series. This ensemble may be regarded as a sample from an underlying probability distribution for the whole stochastic process (the causal model) that generates it. The present invention usually fits such an ensemble of time series to a stochastic process model, such as (but not limited to) a truncated Levy flight.

Neural network techniques, including (but not limited to) the expectation-maximization (EM) algorithm and Bayes networks

15 may be used to perform the fitting.

In contrast, the intermediate level approach, working directly with distributions, generates a probability distribution for the stochastic process directly.

In all cases such a distribution is fundamentally what is required for accurate volatility prediction, risk assessment, option pricing, and optimal hedging.

The time-series ensembles, or their stochasticprocess fits, are compared with real data from actual
markets. The statistical differences between the model and
the real data are then used to refine the model parameters or
change the architecture of the model itself.

## A Dealer-Mediated Securities Market Model

The space of economic models 105 further includes a 30 dealer-mediated securities market model. The advantage of the agent-based models of this model is that a wider range of phenomena will become open to both investigation and

validation. For instance, an agent-based model allows us to incorporate learning on the part of Dealers and Investors, as well as to investigate dynamics, which otherwise may not be amenable to existing analytical techniques. Particularly when individual agents learn or adapt over time, the resulting co-evolution is normally completely intractable. The computer simulation becomes the scientific tool by which we may model, and begin to understand, such systems.

Preferably, this market model is implemented with a 10 platform in the Java programming language for simulation and investigation of such a market. The simulation consists of a computational Agent-Based Model (ABM) of a market that trades securities. We have used the model to investigate questions involving dealer strategies, especially parasitic strategies, 15 and their implications for real-world issues for stock market exchanges such as Nasdaq. The present invention investigates decimalization (the reduction of the minimum quote increment or tick-size to 1¢) and the market's effectiveness at performing price discovery under different proportions of 20 parasitic strategies. Our results indicate that a move towards decimalization may have a significant negative impact on price discovery in the presence of parasitic strategies, and perhaps slightly impede it in a non-parasitic market. The model can also be used to investigate other issues.

25 These models, and the need to validate them experimentally, arise out of very practical considerations about the microstructure of security exchanges such as Nasdaq. In recent years, Nasdaq has changed the way it works, e.g., the new order handling rules and the recent proposal to decimalize the system by reducing the tick size to a penny. Every one of these structural changes has the potential to produce sweeping effects in the structure of the

market - consequences not necessarily intended by their implementers.

To this end, the present invention includes an agent-based model of a dealer-based market. This computer

5 simulation represents the players in the market, Dealers and Investors, as "agents." Agents are computational objects that behave so as to maximize some fitness criterion. In the case of a market, the fitness is (at zeroth order) profitability, with additional criteria, such as risk

10 aversion, appearing as higher-order corrections. This model provides an "economic laboratory" to explore the behavior of the market and the consequences of modifying its institutions and rules.

The main questions we address concern the effects

15 of tick-size, parasitism and their interaction with the
market rules and structures. In addition, these models are
quite capable of providing research tools for many other
topics. The models are particularly adapted to provide reasonably robust answers to the focal questions of our

20 investigation.

parasitism is broadly defined as a strategy which attempts to make a profit without contributing to the process of price discovery. We will also use parasitism with a slightly different, albeit intuitively clear meaning - as an ability to take advantage of other players' actions. As discussed later, in the latter sense some players may behave as parasites, even without "consciously" realizing or attempting to do it where "consciously" means that its rules may not explicitly imply any parasitic behavior. An example of an explicitly parasitic strategy might be a strategy in which the trader hangs back (behaves non-competitively) until market conditions are ripe for exploitation and then trades

inside the spread, making a quick profit. In the context of double-oral auction markets, such strategies were observed to be highly effective, outperforming all others as indicated in Rust, John, John Miner, and Richard Palmer (1993): "Behavior

5 of Trading Automata in a computerized Double Auction Market",

The Double Auction Market: Institutions, Theories and

Evidence, Reading, Massachussetts: Addison-Wesley, the

contents of which are herein incorporated by reference.

The main intention of the model of the present

10 invention is to create a population of interacting agents

(Investors and Market Makers/Dealers) that together produce

price discovery in the marketplace. The Java simulation we

have implemented is very powerful, and can incorporate

additional features of the real world, such as a limit-order

15 board, trading of multiple shares, or trading in a wide range

of volumes etc.

The market contains a plurality of securities whose value is exogenously specified: the underlying value of the security is assumed to fluctuate according to a random walk with a drift. The market consists of a finite population of players trading in that single security. We have two types of players: Dealers (Market Makers) and Investors.

value of the underlying security adjusted by an idiosyncratic error, which in turn is determined by the investor's degree of informedness. The simulations were run with errors distributed by a Gaussian law. The simulations can also investigate information time lags as well as errors.

Dealers, on the other hand, do not have any prior information about the "true" price. To a certain extent, competition drives Dealers to discover the price through market interactions (this is the process of price discovery

which markets mediate). Dealers are obliged at every moment to post their current bid and ask prices, and their volumes, on the public board. Investors decide whether they consider a purchase or sale of the security beneficial to them (by 5 comparing their knowledge of the true value with the current market quotes), and, if so, they execute a trade at the best available price.

The timing of the simulation is determined by a scheduling agent, which assigns to every player (dealer or investor) a period of time in which the player is able to take his next action. An action for a dealer is to choose his bid and ask price, and for an investor is to buy or sell at the best currently available price. A dealer can also update his quotes after every transaction he performs. There is much flexibility in the model with respect to the relative frequency with which each dealer and investor acts. In most simulation runs, dealers acted at a fast rate, with investors having a larger range of rates, from very fast to quite slow. The scheduling process could be adjusted to model the order flow of different kinds of security.

Each player is endowed with a fixed quantity of money and a fixed initial inventory. The total number of units of the security can be fixed in the simulation. If at any time a player's total assets fall below a negative

25 constant (fixed at -\$1000 in most of our runs), that player is removed from the simulation and replaced by another who's strategy parameterization is randomly selected. The old player's inventory (positive or negative) is redistributed to the remaining players (who are charged/compensated

30 accordingly). Since the new player has an initial endowment of cash, money flows into the system as a consequence of player bankruptcy.

The model market consists of a framework in the Java programming language. This framework includes the model market, which is populated with Dealer and Investor agents who trade in one security; an agent scheduler, and a 5 graphical user interface that allows one to control the microstructure of the market and monitor the progress of the simulation from both macroscopic (statistical) and microscopic (agent) points of view. The core simulation code can also be run separately from the graphical user interface 10 (in "batch mode").

At the highest level, the simulation consists of four types of software objects: Price, Dealers, Investors, and the Market itself. At the next level down, all of these objects have member objects that provide communication and bookkeeping capabilities. A detailed breakdown of the simulation and its component objects is given later. FIG. 2 shows a screen shot of the simulation of the dealer-mediated securities market model. Each menu and chart shown is described in detail later.

The models represent agents' fitness functions and strategies. We have two types of strategies: Dealer strategies and Investor strategies. Both types of agents are concerned with making money. However, Dealers, as the mediators of all trading, have much more latitude in their strategies. Dealers must set both bid and offer prices and volumes. Investors must decide only on the course of action at any given moment, namely, whether to buy or sell at a given price and how many shares.

The underlying value follows a stochastic dynamic.

30 At each opportunity to trade, an Investor is given this value plus some amount of error corresponding to his degree of "informedness." If a Dealer's current prices are below

(above) the Investor's perception of value, then the Investor will buy (sell) one or two shares of the security. Using this strategy, we can easily set the proportion of informed Investors, as in the GM model, while retaining a much more realistic model of market dynamics. The present invention also comprises investors who wish to trade a range of volumes.

The core of our current work focuses on Dealer strategies, where there is a very rich environment for re
10 search. Our main goal was to investigate the effects of parasitism, tick size, and the combination of both on the market. For that, we have developed two broad classes of dealer strategy: one that makes price discovery happen, and another that uses information created by the rest of the

15 population (parasitic strategies). As discussed later, there is not a clear distinction between the two. With this goal in mind, we developed and implemented several specific Dealer strategies:

- A "Basic Dealer" only reacts to trades which come his own way. He maintains his quotes until he receives a certain number of trades on the buy (or sell) side, and then adjusts the quote on that side appropriately. It is a simple strategy which manages to track price very effectively, in the absence of parasites.
- A "Price Volume Dealer" tries to deduce from the market data the current demand and supply schedules and thus decides whether the current price is above or below of the "true" value. From that data the dealer decides what bids and asks to quote. For this particular type of dealer it is also very easy to decide what volume to

sell, which may be a very valuable feature for a market, where volume is determined endogenously.

- A "New Volume Dealer," is a modification of the previous type. He looks on the past discounted volume only, 5 without explicitly taking the price into account. If the New Volume Dealer observes that there were more buys in the past, he concludes that the price is probably above the true value. The simplest version of this dealer reacts by increasing the ask price above the current 10 market price. If the converse holds (there were more sells in the past), the dealer reacts by lowering his bid price. A slightly more sophisticated version of this dealer adjusts both bid and ask as a reaction to excess demand or excess supply (there is a parameter 15 that allows to fine tune this dealer). When excess demand/supply is small enough (a Volume Dealer has a benchmark to determine this), the dealer concludes that the price is right and jumps inside the spread, essentially acting as a parasite. Surprisingly enough, 20 even such a simple rule allows the population of the New Volume Dealers to track the prices really well.
- A very important strategy for our model is the
   "Parasitic Dealer" strategy. Parasitic Dealers do not actively participate in the price discovery process; rather, they "hang back," waiting until a sufficiently narrow spread with sufficient volume appears on the board. They then "steal the deal," buying and selling the security inside the spread. Such strategies have been shown to be both effective for the dealer employing them, and destructive to the market's function of price

discovery as explained in Friedman, Daniel, and John Rust, eds. (1993): The Double Auction Market:

Institutions, Theories and Evidence, Reading,

Massachussetts: Addison-Wesley. On at least one major

exchange, this strategy is well understood and strongly,
albeit unofficially, discouraged. On the AMEX, this

process is known as "steenthing the market", named from
the practice of shaving a sixteenth of a point off the
existing spread to steal the deal. While it is not

officially outlawed, it is unofficially forbidden and
occurs very rarely in practice.

- A somewhat more sophisticated version of a parasitic dealer, called "New Parasite," also looks at the excess supply/demand and decides whether it makes sense to jump inside the spread or not. This version of the parasite performs quite well in most of the markets we have experimented with.
- A "Matching" dealer who contains a collection of observations and actions. He learns connections between observations and actions which are profitable. Examples of observations are: "my inventory is high", "the spread is large", "my bid is below the market", "my inventory is near zero". "trade volume is high". Examples of actions are more obvious: "raise my quotes", "increase my bid", "narrow my spread".
- A "Classifier" dealer is similar to the Matching dealer,
   except he learns over patterns of observations. For instance, instead of just matching one of the aforementioned observations. The classifier dealer might

learn that "when volume is high" and "my inventory is near zero" and "my spread is large" it is profitable to "narrow my spread". This space is much richer, clearly, but therefore much larger and harder to learn in.

5

A "Dynamical System" dealer uses a discrete dynamical system to set his bid-ask spread and mean price. If one regards mean price, P. as a source or a sink of inventory, I, and the bid-ask spread, S, as a source or a sink of cash flow, C, then generically a system of the form:

$$\frac{dP}{dt} = -f(I)$$

$$\frac{dS}{dt} = g\left(\frac{dC}{dt}\right)$$

where f is monotonically increasing in I and g is increasing in C, will yield dynamics that are similar to those used by a real dealer. This can be seen in the P equation by considering the effect of changing inventory. If f(I<sub>0</sub>) = 0, then P will remain fixed; as I increases past I<sub>0</sub>, P will start to decrease, which will generically lead to more sells than buys, reducing inventory until the equilibrium value I<sub>0</sub> is again reached. Similarly, as cash flow increases, this implies that there are additional profit opportunities,

so the dealer should increase his spread;  $g\left(\frac{dC}{dt}\right)$  will also

increase, causing the dealer to raise spread to capitalize on

the increasing market volume. Clearly, one can make this simple formula more sophisticated by using a predictive model of C or I based on the order flow and pricing observed in the real market.

The names of these strategies are somewhat arbitrary and even misleading: for instance, the "New Volume" dealer turned out to be a very effective parasite.

There are two senses in which evolutionary agents have been investigated in this model. First, in the simpler sense, running the simulation for long periods of time, while incorporating mutation of the parameters inside dealers' strategies, allows one to discover good values of those parameters (although the actual good values of these parameters may depend upon the other dealers in the simulation).

Second, one can use evolutionary approaches at a higher level to discover good strategies. Two of our dealer strategies are of this form: the "Matching Dealer" and the "Classifier Dealer." These are significantly more

- 20 sophisticated types of strategies: the dealer has a whole repertoire of possible strategy building blocks, and by trying them out attempts to learn what the optimal strategies are. Our "Classifier Dealer" uses an approach very similar to classifier systems in the machine learning literature.
- These strategies must be run for very long periods of time to allow the agents to learn the connections between observables (quote changes, trade volume, inventory level,...) and useful responses (changes to bid and offer) in the market.

Our results indicate that the choice of strategy

30 building blocks is of vital importance in allowing
evolutionary learning approaches to function effectively
(analogous results are well known in the fitness landscape

and optimization literature). The literature supports our result that a sophisticated strategy is by no means certain to be more successful. For instance, the Double Auction Market explained in Rust, John, John Miner, and Richard

- 5 Palmer (1993): "Behavior of Trading Automata in a computerized Double Auction Market" found that the simplest parasitic strategy was the most effective. Furthermore, as suggested by Darley, Vincent M., and Stuart A. Kauffman (1997): "Natural Rationality" in The Economy as an Evolving,
- 10 Complex System II, ed.by W. Brian Arthur, David Lane and Steven N. Durlauf, Reading, Massachussetts: Addison-Wesley(the contents of which are herein incorporated by reference), there may be some bound on the sophistication of a strategy for it to be effective in a system of co-evolving

15 agents. We will discuss the issue of more complex, sophisticated Dealer strategies later.

Our primary results concern the influence of tick size and parasitic strategies on the market's effectiveness at price discovery. Within the current model, the underlying value of the single stock is exogenously specified, which allows a precise measurement of how effectively the market follows that underlying value, as we will discuss later.

Our particular focus has been to investigate the effects of introducing parasitic dealers into the market, to determine what level of parasitism the market can support before its functionality becomes degraded. We then investigate how that degradation occurs at varying tick sizes.

Our first observations are for systems consisting
30 entirely of non-parasitic strategies. It has been discovered in the simulations that these systems track the underlying value somewhat more closely with larger tick sizes. FIG. 3

shows the behavior of the population of Basic Dealers for different tick sizes. Visually, we can see that the three curves plotted (best bid, best offer, and true value) are closer together at a larger tick size, although the difference is small (more precise quantitative measurements are given later).

The second set of observations concerns the introduction of parasites into the system. A number of different parasitic dealer strategies have been investigated,

10 of varying sophistication. These results hold for each parasitic type. We observe that price discovery is largely unimpeded at large tick sizes, but dramatically affected for small tick sizes. FIG. 4 displays the results of the dealer mediated securities market model for a market consisting of 7

15 Basic Dealers and one parasite.

FIG. 5 displays the results of the dealer mediated securities market model for a market with a mixed population of dealers (we will call it a mixed market in the future); some parasitic and some not. This market contains a much higher proportion of parasites than the preceding ones, including some of the more extreme types of parasite.

Since we are using a "true" value for the price, we are able to quantify the impact of different strategies and market structures. In particular we have examined data on the statistical distribution of (best bid - true value)<sup>2</sup>, (best offer - true value)<sup>2</sup>, average value of the spread and standard deviation of the spread over time as estimates of the market's ability to track price.

The statements about price discovery and tracking

the market in the preceding discussion are intuitively clear.

A quantitative criterion, nevertheless, would be useful,

especially to distinguish similar cases. We will define market tracking as consisting of two different components:

- The market bid and ask prices are close to the true value, and
- As one can see, these two conditions do differ: it is possible for the market to "follow" the true price while the true price is outside the spread. It is also possible to observe that the market reacts very slowly to the true price although the true price stays inside the bid-ask spread, essentially because the spread size is large. Obviously, some regimes of tracking the price are more beneficial for Dealers and others for Investors.

With this in mind, we quantified the market's ability to track prices by four different parameters:

- the square root of the average squared (bid True Value). We will denote it RMS(bid-True Value) where RMS means Root-Mean-Square.
- 2) the square root of the average squared (ask True

  Value), which we will denote as (RMS(ask-True

  Value))
  - 3) average value of the spread
  - 4) standard deviation of the spread.

While a combination of these variables is not necessarily the 25 best measure of market success (for one thing, it does not gives us a proportion of time when the true value was inside of the spread), it gives us a very good idea of market performance.

FIG. 6 shows graphs of RMS(bid - True Value) and 30 RMS(ask - True Value) as a function of the tick size for different populations of Market Makers in the dealer-mediated securities market model. It can be clearly seen that both

variables generally increase with the addition of the parasites to the market, and decrease with the tick size.

FIG. 7 shows the average value of the spread as a function of the tick size for different combinations of the 5 market makers in the dealer-mediated securities market model. There is one simulation where the spread was negative; that happened probably because of a very large tick size and of the fact that the market makers make their decisions simultaneously, therefore there is a possibility to 10 "overshoot".

FIG. 8 shows a graph of the standard deviation of the spread size as a function of the tick size for different populations of Market Makers in the dealer-mediated securities market model. The results are mixed, but quite surprisingly one can see that the standard deviation increases somewhat with the tick size. We can also see that the introduction of parasites into the market can increase the standard deviation of the spread.

The model is reasonably complex, and a number of

20 other interesting phenomena have been noted (like patterns of
wealth distribution among dealers, different market regimes).

Our ability to measure how well the market is executing the
process of price discovery under different circumstances can
also help us to understand the interaction of inventory,

liquidity (implied by price-volume combinations listed on the
board), and volatility.

Further, we note that when investors are largely uninformed (i.e., their knowledge of the underlying value of the stock is very poor), any collection of dealers has great difficulty in tracking the true price. Empirically, the reason for this is clear: when most investors are uninformed, no matter where the market bid and offer are located, roughly

equal numbers of investors will buy and sell, so very little can be learned by the dealers.

One relatively obvious way in which parasitism

affects market behavior is that, by their mere existence,
5 parasites decrease incentives for the market participants to
aid in the process of price discovery (Rust, John, John
Miner, and Richard Palmer (1993): "Behavior of Trading
Automata in a computerized Double Auction Market", in The

Double Auction Market). A less obvious observation, however,

- 10 is that parasites can produce useful information just by jumping inside the spread. The quantity and quality of this information does depend on the tick size. For example, if a parasite has undercut the market by a significant amount, the effects of that undercut (for instance, on market volume on
- 15 the buy or sell side) tell the market participants much more about the liquidity, demand, underlying fundamentals, etc., than when the price increment is negligible. Undercutting by a significant amount also carries more risk and less profit. It is this effect, we hypothesize, which allows price
- 20 discovery to continue reasonably well at a large tick size, even in the presence of large numbers of parasites: by jumping inside the spread by a large amount, a parasite causes a significant change in the volume of trades on that side of the spread, which provides useful information to the
- 25 market. When tick-size is small, the marginal impact of jumping inside the spread on trade volume is negligible, and hence parasites operate without providing useful information to the market. A decreasing tick size will make parasitic behavior more profitable, since the points shaved represent higher profit for the parasite.

If changes in the underlying market are quite large (i.e., the volatility of the security is large), it may be

difficult for the market to track price effectively. In this case, it may be true that a larger tick size encourages better price discovery because the coarse-graining effect of the tick size allows for more rapid price tracking. One

5 would anticipate that this result holds true at least for simple strategies, but that more sophisticated strategies could perhaps follow price changes equally well with a large or a small tick size. Our results so far support the idea that simple strategies can follow price slightly more

10 effectively with a large tick size. They also suggest that, even if sophisticated strategies could track price well at all tick sizes, in the presence of parasites this tracking would be highly impaired at a small tick size.

We further conjecture that a somewhat unexpected

15 relationship between the tick size and the spread may hold if
the ability of the system (and therefore of an individual
dealer or investor) to adjust depends on the tick size.

Under that condition, the dealers' profit (which depends upon
their ability to adjust) will depend upon the tick size;

20 since dealers will often adjust their spread to account for
profit/risk tradeoffs, their spread will in turn depend upon
the tick size.

The present invention includes an Agent-Based Model of a stock market with a reasonably diverse population of dealer strategies which has allowed us to investigate the focal questions of tick size and parasitism quite effectively. Our main findings at the present stage pertain to the effects of tick size and of parasitism on the market's performance and on its ability to carry on the process of price discovery. It has been shown in the simulations that

 the ability of the market to track price increases somewhat with tick size, and

2. parasitic strategies impede the process of price discovery, especially for a small tick size.

While unexpected and somewhat counterintuitive, these results seem to be very robust in the present model. They have been repeated time and again for different combinations of Dealers, different levels of Investor informedness, and different parameters of price fluctuations.

The market structure further comprises: a public limit order board must be included, together with a simulated 10 electronic execution system; transaction costs must be included; and the typical statistical volume and size of trade must be configurable (to represent different types of Nasdag stocks). This in turn will require a more complex range of investor and dealer strategies. First, investors of 15 varying types should be modeled: from small consumers to institutional investors, and of course day-traders (who would probably represent the main parasitic source in the more realistic market). Here an interesting addition to the concept of investor "informedness" would be information time 20 lags: some investors are watching trading screens; others just read the Wall Street Journal. Second, dealer strategies account for the larger market environment (limit orders, greater range of trade size, etc.). Other possibilities which could be incorporated in the model are to allow the investors 25 to choose between the single stock and a surrogate of the

There are two basic modes of operation for the simulation: graphical and batch. The batch mode is most useful for data-gathering purposes. It runs the simulation entirely without a graphical user interface, outputting to a file whichever data the user requests. These files are in a standard text format and can be read by any data/graphing

market index.

application for analysis and plotting. The batch version runs several orders of magnitude faster than the graphical version, and hence is ideal for the data-gathering purposes necessary to obtain statistically significant, robust 5 experimental results.

This section will first explain the control of the simulation via the graphical user interface, followed by the batch mode features.

The graphical version of the simulation is run by

10 double-clicking on the "BiosMarketII" icon. This will bring

up the main simulation control window. FIG. 9 displays the

main simulation control window of the dealer-mediated

securities market model.

The main window is split into two main areas: the

"Quote Montage" on the left, and a recent historical view of
the best quotes and trades as they occur on the right The
quote montage contains each dealer's bid and each dealer's
offer, ranked vertically from best to worst (so the largest
bid and smallest offer are at the top of the montage).

- Dealers are identified by a name (a three-letter acronym) and a unique color. The graphs of the dealer's cash, assets, or inventory (discussed later) are also color-coded for easy identification. The first two letters of the acronym represent the dealer's strategy type (for example 'BD' for Basic Dealer, 'NV' for New Volume dealer, 'PD' for Parasitic Dealer, ...)
- The plot on the right contains, by default, a trace in pink of the best offer at each time-step, a trace in yellow of the best bid at each time-step, and asterisks in green of the trades that occur. Since, within each individual time-step, the available best bid/offer may change as trades

come in, not all of the trades plotted will lie directly on either the bid or the offer traces.

There are five other parts to the main window: the current time indicator in the top left (since the simulation 5 does not consider the opening-closing trading cycle, the units of time are somewhat arbitrary); the four control buttons in the bottom right; a display of market observables in the bottom left; the menus across the top of the window; and the ticker tape across the bottom that records recent 10 trades.

The four control buttons are as follows: "Quit" terminates the simulation; "Step" runs the simulation for a single time-step; "Run" runs the simulation continuously; "Stop" pauses the simulation (pressing either "Step" or "Run" will continue from that point).

The main simulation control panel contains four menus. First, the "File" menu currently contains a single item, "Exit," which terminates the simulation. FIG. 10 displays the Options menu of the dealer-mediated securities 20 market model. The "Options" menu has four choices. FIG. 11 displays the Set Human Dealer Prices panel and the Set Tick Size panel of the dealer-mediated securities market model. "Set Human Dealer Prices" will, if the current market contains a "human dealer," open a control window that allows 25 the user to control that dealer and thus join in the simulation. By clicking with the mouse, the user can adjust either bid, offer, or both up or down by a single tick. Clicking multiple times will adjust by progressively large amounts. To run a simulation with a human dealer, double 30 click on the 'HumanDealerMarket' icon. Due to the memory consuming nature of Java interfaces, the simulations will tend to run faster if only one is running at a time, so we

recommend quitting the current simulation before starting a new one.

"Set Tick Size" brings up a small window which allows the user to adjust the tick size of the current simu5 lation on the fly. It is used by moving a slider to the desired position (from \$1 on the left, to \$1/100 = 1 cent on the right), and then pressing the "Save" button.

FIG. 12 displays the "Show True Value" panel and the "trade history" panel of the dealer-mediated securities 10 market model. "Show True Value" toggles the display of a trace showing the true underlying value of the stock in the main display window. By default the display of the true value is off, so that a "human dealer" is not given information to which he is not entitled. Selecting "Trade 15 History" from the menu brings up a scrolling window of recent trades. Each line in the window contains, in order, the time, investor, action that took place, volume, dealer involved, and price of the transaction. Each investor is given a three-letter lowercase name. Each dealer is in 20 uppercase. We can see here that dealers "NVT" and "BDF" are dominating the market A characteristic of our markets is that often a small number of dealers provide most of the liquidity (much as in the real market). In this case, "NVT" is in fact using a parasitic strategy (of the "New Volume" variety).

FIG. 13 displays the "graphs menu" of the dealermediated securities market model. In addition to the main
trade/bid/offer display, the simulation allows the user to
graph a number of other observables. There are six other
built-in graphs. In addition, the simulation can be
configured to save data to a file. This data can later be
plotted or analyzed using any graphing/statistics package.

FIG. 14 displays the "cash bar graph" panel of the dealer mediated securities market model. The "Cash Bar Graph" displays a histogram of each dealer's current cash position. The color of each column identifies the dealer, and the 5 height shows the current amount of cash the dealer has.

FIG. 15 displays the "Inventory Bar Graph" panel of the dealer-mediated securities market model. The "Inventory Bar Graph" displays a histogram of each dealer's current inventory position. The color of each column

10 identifies the dealer, and the height shows the current volume of stock the dealer has in his possession (which could be negative if the dealer is short in the market).

FIG. 16 displays the "Supply and Demand Graph" panel of the dealer-mediated securities market model. The "Supply and Demand Graph" displays the supply and demand curves implied by the dealers' current quotes. The true value of the stock is also displayed. If the dealers are tracking the true value effectively, the graph should look something like the one in FIG. 16.

- FIG. 17 displays the "All Dealer Cash" graph of the dealer-mediated securities market model. The "All Dealer Cash" graph contains a color-coded trace for each dealer's current cash holding. It allows the user to compare the cash positions of the different dealers over a recent historical
- 25 period. FIG. 18 displays the "Dealer Assets" panel of the dealer-mediated securities market model. The "All Dealer Assets" graph contains a color-coded trace for each dealer's current assets. It allows the user to compare the total assets of the different dealers over a recent historical
- 30 period. The assets are calculated by adding the dealer's cash position to the value of its inventory. This value is calculated using the instantaneous true value of the

underlying stock, and hence fluctuates as that stock value fluctuates. The dealers themselves are of course not privy to this information.

FIG. 19 shows the Dealer Inventory graph of the
5 dealer-mediated securities market model. The "All Dealer
Inventory" graph contains a color-coded trace for each
dealer's current inventory position. It allows the user to
compare the inventory of the different dealers over a recent
historical period. In the example in FIG. 19, the "NVG"

10 dealer went very short in the market, but then bought
significant amounts of stock in the 84-100 time frame to
balance his books.

This section describes a simple example run that illustrates how the market's price discovery process fails in 15 the presence of parasitic dealers when the tick-size is small. To start the simulation, double-click on the icon "BiosMarketExample." After a brief delay, the simulation interface appears. Before running the simulation, to see the process of price discovery in action, it is best to display 20 the underlying value in the bid/offer/trade graph to the right of the main control panel. To do this, go to the "Options" menu and select "Show true value." To see the results most dramatically, it is best to change the tick-size first to a very large value, and then to a very small value.

25 So, on the "Options" menu, select "Set Tick Size" and click on the blue slider to move it to the extreme left, so that

- on the "Options" menu, select "Set Tick Size" and click on the blue slider to move it to the extreme left, so that the text entry reads "1." Now click on "Save." The tick-size in the market will now be set to \$1; i.e., a very large value.
- Now click on the "Run" button in the main control window, and watch the simulation unfold. This simulation contains a single parasitic dealer, of the "New Volume"

variety. FIG. 20 displays a panel showing how the dealers track the true value reasonably well in the dealer-mediated securities market model.

Once you are content that price discovery is

5 functioning well, set the tick-size to a very small value.

There is no need to stop the simulation to do this; simply go back to the "Set Tick Size" window and move the slider to its rightmost end so that the text entry reads "100" (or something near 100). Again, you need to click on the "Save"

10 button for the change to take effect. FIG. 21 displays a panel showing the simulation results for a smaller tick size in the dealer-mediated securities market model. Price discovery is not as effective. With larger numbers of parasites, or a single more extreme parasite, the tracking of true value fails almost completely.

Almost all of the data we examined to draw our conclusions were generated by running the simulation in batch mode. This has several advantages: first and foremost, the simulation runs several orders of magnitude faster; it is also possible to pre-specify a total number of time-steps for which to run it (anywhere from 5000 to 500,000 were used in practice), and it is easier to run several simulations in parallel.

It is possible to run the simulation in these two
different ways because the core of the simulation is highly
modular. It is necessary simply to connect that core with
either the GUI or the batch code to run the simulation. To
run a simulation in batch mode, one simply types (from the
command line):

30

java BatchMarket [prefix] [duration]

where "[prefix]" is a character prefix the simulation uses to identify input and output files for this run, and "[duration]" is the number of time-steps for which to run the simulation (if omitted, this defaults to 10,000 time-steps).

5 For instance, to run a simulation without the GUI for 5000 time-steps, using the same input files as the example run described earlier, one types:

java BatchMarket EG 5000

10

The files that describe the initial conditions (dealer mix, etc.) for the example run are called "EGdealerMix.dat,"
"EGoutputParms.dat," and "EGplayerParins.dat."

The user can configure the initial conditions for 15 the simulation by editing those files. The "outputParms" file contains "name value" pairs in the following format:

outputDealerCashData true
outputlnvestorInventoryData false

20

The possible parameters to configure are as follows:

- base\_filename: the suffix to use for all data files created by this simulation run
- outputData: true/false flag that globally turns data output on or off. If off, it overrides all other data output flags.
  - OutputInvestorCashData: if true, investor cash holdings are output to file at each time-step
- OutputDealerCashData: if true, dealer cash holdings are output to file at each time-step

- OutputInvestorInventoryData: if true, investor inventory holdings are output to file at each time-step
- OutputDealerlnventoryData: if true, dealer inventory holdings are output to file at each time-step
- OutputValueDebugData: if true, best bid, best offer, and true value are output whenever a trade takes place.
  - OutputObjectFilesRate: rate at which to save (using Java's serialization capabilities) all Dealer objects to file for later examination
- 10 OutputAssets: if true, dealer assets are output to file at each time-step
  - OutputBids: if true, each dealer's bid is output to file at each time-step
- OutputOffers: if true, each dealer's offer is output to

  15 file at each time-step
  - OutputBankruptcy: if true, data on which dealers and
    Investors go bankrupt is output to file
  - UniformRandomWalk: if true, using a uniform random walk with drift, otherwise a log-normal random walk
- 20 FoolishnessMax: the standard deviation of the investors' knowledge-error in the true value
  - DisallowArbitrage: if true, then disallow dealer quotes that would allow obvious arbitrage opportunities
- RandomWalkSeed: can be used to fix the seed for the random number generator used by the random walk
  - TickSize: sets the initial tick size.

The "dealerMix" file contains the list of dealers which take part in the simulation. Usually we fix this at eight

30 dealers. The file simply contains a list of the names of the Java classes which implement the different dealer types. For example "EGdealerMix.dat" contains the following list:

BasicDealer
BasicDealer
BasicDealer
5 BasicDealer

BasicDealer

BasicDealer NewVolumeDealer

NewVolumeDealer

10 The third file, "playerParms" contains default initial parameters (including the inventory and cash holdings) for the different dealer types. It contains a number of lines, the first item on the line being the name of the dealer type, followed by the number of arguments required by the object's constructor, followed by the arguments themselves. For example, the line for the basic Parasitic Dealer is:

ParasiteDealer 5 1000.0f 100 3 2.0f 3

- 20 So the dealer is initialized with \$1000 in cash, 100 units of stock, a responsiveness of 3 (the scheduler will allow the dealer to act every three time steps on average), a risk aversion of 2.0 and will accept a maximum of 3 trades inside the spread before moving his quotes outside.
- 25 This aspect of the present invention has been developed using an object-oriented simulation of a single-security market with the Java programming language. Three principal classes make up the simulation: the Market class, the Dealer class, and the Investor class. In addition, there is a support class, the GuiMarket class, which provides a user interface and ties the other objects together in an

actual simulation. Individual instances of these classes are objects.

- Market: The Market class provides a venue where the
   Dealer and Investor agents can interact. The Market provides the following functionality:
  - A time-step method, which runs the simulation forward one step in time.
  - Methods for matching Investors who wish to buy or sell the security with the Dealers who are trading the security at the Investors' desired price.

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- A Quote Montage object, which displays the current bid and ask prices and volumes of all Dealers in the market. It also provides a method for displaying the current best bid and ask and their volumes.
- A Scheduler object. The scheduler determines the order and frequency of trades made by each Dealer and Investor. It allows each player waiting on a queue to trade, and then puts them back onto the queue to wait for their next opportunity.
- Dealers and Investors: These are both subclasses of a Player superclass. The Player class provides interfaces for keeping track of inventory and capital and executing trades. Dealers have the additional ability to interact with the Market's Quote Montage object, while Investors are able to query the Market for the current "true" value of the security. Both Dealers and Investors have strategy functions that determine their trading desires. Investors decide whether to buy or sell the security,

while Dealers decide what bids and asks to post on the Market's Quote Montage.

- GuiMarket: The GuiMarket provides the user interface,
   and the GuiMarket object is the entry point into the simulation when run in graphical mode. The main functions of the GuiMarket object are:
  - Instantiation of the Market object with desired initial conditions.
- Display of the Market's Quote Montage object as trades occur. This panel displays pertinent information about the time and spread. It also displays all the dealers, the volume, and the bid price on the left side, and the dealers, volume, and price offered on the right side.
  - Display of Buy/Sell graph as trades occur. The volume of stock for current bid prices is graphed against the volume of stock at the current offer price.
- Buttons for running/stopping/stepping/quitting the simulation.
  - Instantiation of a Ticker object, which currently displays to the scrolling ticker tape at the bottom of the main control window. The ticker records market activity, i.e., time, Investor name, buy or sell, volume, dealer name, and price.
    - Initialization of a Config object
- Config: this object provides the following
   functionality:

25

 Market parameter set-up, which includes initialization of the number and types of dealers

(BD - basic dealer, PD - parasitic dealer, etc) and number and types of investors (Fl - foolish investor, etc.); setting the number of time iterations for a simulation, setting initial cash and inventory for investors and dealers and their response time statistics; setting the "true" price of the stock. These parameters are accessed through the three parameter files discussed above.

BatchMarket: This provides the non-graphical entry point to the simulation. It initializes a Config object which reads in the input files (simulation run parameters), sets the market running for the specified number of steps, and then exits. The input files specify which data is to be saved during the run.

When the market is run (either via "java GuiMarket" or "java BatchMarket") another command line parameter is required. This parameter, as described previously, is the prefix used for the three input files. So, to create a new simulation, one simply edits those files, and then executes the command "java GuiMarket <prefix>" or 'java BatchMarket <prefix> <duration>".

FIG. 22 displays a panel of results obtained by executing the dealer mediated securities market model.

# Predicting Market Volatility

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The space of economic models 105 further include models which are particularly adapted to predict volatility.

30 It is clear that current efforts to predict market volatility based on the Black-Scholes formula for option pricing do not work particularly well.

As is well-known the implied volatility obtained by running the formula backwards, using stock and option prices, varies nonlinearly with the difference between the current price of the underlying and its exercise price, instead of 5 being independent, so there is something wrong with the structure of the Black-Scholes model.

It is also well-known (and possibly related) that parameterising market returns by the lognormal density does not work very well for short term data, i.e. the density

10 p(s'/s) where s is the asset value now and s' its value in the future, is not lognormally distributed if the future is not more than about two weeks, but follows a Pareto-Levy distribution.

It follows that better formulas are need to predict volatility both within the framework of implied volatility, by developing better models of the variation of stock returns than the simple Markov process which underlies the Black-Scholes equation, but also by developing better ways to analyze the data provided by market time series.

We propose to start the process of finding better market volatility predictors by constructing a nonlinear state space model (NLSSM) of the market. Such a model contains hidden state variables and parameters. To estimate these variables and parameters we propose to use a version of the expectation-maximization or EM-algorithm. Such an algorithm has two steps (a) an expectation or E-step in which hidden variables are estimated from given parameters, and (b) a maximization or M-step in which parameter estimates are updated given hidden variables. The E-step can be carried out using a Kalman filter, which can be viewed as a generalization of the backpropagation algorithm of neural networks.

It is clear by now that in applying such algorithms to markets, data should be as low dimensional as possible.

There are now a number of differing techniques for dimension reduction which can be used. There is a class of

- 5 unsupervised learning algorithms (as distinct from backpropagation which is a supervised learning algorithm) embodied in neural networks available for this purpose, e.g. the principal components analysis algorithm (PCA) and various variants (localised PCA, nonlinear PCA), and a
- 10 close relative, the independent components analysis algorithm (ICA). These algorithms can be used to find optimal representations of the data before setting up the NLSSM.

Several other issues associated with this approach suggest themselves.

- 15 (a) What is the relation of the hidden variables in an NLSSM to those found in causal or agent based models of the market? Evidently better market models can give rise to better state space descriptors. Such descriptors could include cooperative interactions between traders, such as herding.
- 20 (b) There are also many new developments associated with parametric approaches to market modeling that use Pareto-Levy distributions etc, or nonlinear Langevin models, e.g. Bouchoud et.al. and Farmer. These can also give rise to better state space representations.
- 25 (c) Finally it is also possible that ways can be found to optimize NLSSMs using search algorithms, e.g. genetic algorithms (Gas) to find better hidden state variables and their combinations. This will require a measure of improvement in the ability of such models to predict market data or properties such as volatility.

#### Optimization

Once the causal models have been evolved and adapted to fit real market data, they are used to generate data more widely for a multitude of situations, including what-if scenarios. In particular, they can be used:

- 5 1. for predicting volatility;
  - for evaluating and predicting risk for any desired portfolio, allowing ranking of different portfolios;
  - 3. for optimization of portfolios;
- 10 4. for pricing of options and other derivatives;
  - 5. for choice of optimal hedging strategies.

Because the models produce non-Gaussian distributions of return, a single simple measure of risk such 15 as volatility is not adequate to characterize risk, rank portfolios, optimize portfolios, price options, and hedge risks. Practical risk measures that we use include the probability of loss greater than a specified threshold, the expected worst drawdown in a given period, the expected time between significant drawdowns, and the value at risk (VaR) at a given confidence level. We extract these quantities from our models using combination of analytic and statistical means.

25

#### Minimizing Values at Risk

The present invention includes techniques to minimize the value at risk of a portfolio. Value at risk is a single, summary, statistical measure of possible portfolio losses. Specifically, value at risk is a measure of losses due to "normal" market movements. Losses greater than the

value at risk are suffered only with a specified small probability.

Using a probability of x percent and a holding period of t days, a portfolio's value at risk is the loss 5 that us expected to be exceeded with a probability of only x percent during the next t-day holding period.

The technique to minimize the value at risk uses historical simulation. Historical simulation is a simple, atheoretical approach that requires relatively few

10 assumptions about the statistical distributions of the underlying market factors. In essence, the approach involves using historical changes in market rates and prices to construct a distribution of potential future portfolio profits and losses, and then reading off the value at risk as

15 the loss that is exceeded only x percent of the time.

The distribution of profits and losses is constructed by taking the current portfolio, and subjecting it to the actual changes in the market factors experienced during each of the last N periods. That is, N sets of hypothetical market factors are constructed using their current values and the changes experienced during the last N periods. Using these hypothetical values of market factors, N hypothetical mark-to-market portfolio values are computed. From this, it is possible to compute N hypothetical mark-to-market profits and losses on the portfolio.

The following discussion describes the technique for isolating low value at risk portfolios. Let us consider a single instrument portfolio, in this case stocks traded on the New York Stock Exchange and Nasdaq markets. For this instrument, there exists tremendous amounts of data. If we assume a one day time horizon (t=1), then the data we are interested in are the daily closing prices of every publicly

traded stock on the two markets. Such data exists for thousands of stocks for tens of thousands of days. From these data, it is possible to construct an m x n matrix (where mis the number of stocks, and n is the number of days) 5 of prices.

Let us assume that within this collection of stocks, there are pairs, triplets, quadruplets, etc., of stocks whose values at risk are lower as a group than any of the stocks individually. This occurs because sets of stocks whose price changes are anti-correlated will have low values at risk. When the price of one stock goes down, the price of the other tends to go up. The chance that both stocks go down together is lower than the chance that two stocks chosen at r~random would go down together because the stocks are anti-

The optimal portfolio would group anti-correlated stocks in the optimal proportions to minimize value at risk. Because there are so many stocks, however, the space of all possible portfolios is too large to search exhaustively.

20 Genetic algorithms are well suited to finding good solutions to just this type of problem in reasonable amounts of time.

The algorithm works as follows:

Step 1:

Start with m portfolios. Each portfolio can be represented as a vector of length m. Each bit  $(m_i)$  in the vector is either a 1 or a 0 signifying that the i<sup>th</sup> stock is either included or excluded from the portfolio. This can later be extended to letting each bit specify the number of shares held rather than simply inclusion or exclusion. To each portfolio, assign a random number of stocks to hold such that every possible

a random number of stocks to hold such that every possible portfolio size is covered (at least one portfolio excludes all but one stock, at least one portfolio excludes all but

two stocks, ... at least one portfolio includes all the stocks). Once the number of stocks to hold has been assigned, let each portfolio randomly pick stocks until it has reached its quota.

## 5 Step 2:

Go back in time n/2 days (halfway through the data). For each of the m portfolios, compute the value at risk for the n12 days that precede the halfway point.

## Step 3:

- 10 Randomly pair portfolios. For each pair of portfolios, let the portfolio with the higher value at risk copy half of the bits of the lower value at risk portfolio (i.e. randomly select half of the bits in the more successful portfolio. If a bit is different, the less successful portfolio changes its
- 15 bit to match the more successful portfolio). The portfolio with the lower value at risk remains unchanged.

#### Step 4:

Repeat steps 2 and 3 until some threshold for value at risk is achieved.

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In this way, clusters of anti-correlated stocks will tend to spread through the population of portfolios. The hope is that this method will ultimately select for most or all of the good clusters. Notice that this method may also alight upon

- the optimal number of stocks to hold in a portfolio. For example, if the minimum value at risk portfolio contains only three stocks, three-stock portfolios will tend to propagate through the population.
- 30 Additional Techniques for the Analysis of Risk

The present invention includes additional techniques for the analysis of risk. The general

understanding of portfolio risk requires an understanding of three contributing problems. The current understanding of these three problems is insufficient to accommodate the challenges posed by modem portfolios. The first problem is 5 volatility. It has long been known that Gaussian approximations to volatility do not correctly describe the behavior of markets, and that price fluctuations show long tails. This means that large deviations are much more likely than conventional theory suggests. The second issue is that 10 of interdependence. In many areas of interest, elements of a portfolio do not move independently of each other, but rather influence each other in ways both subtle and complex. Current methods only uncover a minimal rendering of this complex structure. The third issue is that of time dependence. Many 15 portfolios contain elements that do not mature on the same time scale, but are nonetheless dependent. Again, conventional portfolio analysis and optimization techniques do not address the subtleties of interacting time scales.

that price fluctuations in speculative markets follow a particular class of fat-tailed (relative to Gaussian) distribution known as a Lévy distributions. Levy distributions can be created by correlated random walks, and have been studied in statistical physics under the rubric of anomalous diffusion. In the last two years, these distributions have been revisited in the area of option pricing, but not yet in the area of portfolio management. Since Lévy price fluctuations do not add together in the same way as Gaussian fluctuations, results for expected portfolio risk and associated volatility will in general be different. The present invention incorporates an underlying Levy model

of volatility for portfolio risk analysis which accounts for the different additivity characteristic.

In the construction of portfolios, it is experimentally known that the prices of certain stocks are 5 correlated, and this correlation is typically measured using a covariance matrix. The covariance matrix has two implicit assumptions which we believe are wrong: Fluctuations in prices are Gaussian (see above) and correlations between stocks are describable with pair-wise interactions.

- 10 The present invention modifies this approach in two ways:
  - 1. The covariance matrix requires a large amount of data for accurate results. Extending the covariance matrix method to higher order interactions (three- or four-point interactions) requires an exponentially increasing
- amount of data. We separate the analysis of interdependence into effect and magnitude. The effect aspect is obtained by encoding price fluctuations as (+,-) instead of numerical values. Now we have prices encoded as binary strings instead of numerical
- sequences. Since the fundamental activities of a market are buying and selling, and their attendant effects are the raising and lowering of prices, we believe that the binary encoding is a more fundamental signature of market microstructure than the actual prices. The
- magnitude of gains and losses are obtained by the statistics of large numbers of players making "atomic" buy and sell decisions.

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Once we have encoded the market dynamics of individual instruments as bit strings, we have essentially a telegraph representation of information. This is amenable to the tools of information theory, a field developed to analyze the dynamics of information

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transfer in telephony. Information theory allows us to measure correlations at arbitrary levels of interconnectedness, and although the data requirements scale exponentially as interconnectedness increases, the constant in front of the exponent is much smaller than the covariance case because of the binary nature of the data. Interconnectedness is measured by a quantity called mutual information, and the assumptions associated with it are less stringent than the assumptions required to measure covariance, and in particular are not dependent on the assumption of a normal distribution.

The present invention uses the measure of mutual information to construct a phylogeny of interdependence, 15 using the technique of minimal spanning trees coupled with higher order information correlations to remove degeneracies. (multiple solutions satisfying the same constraints) Once we have constructed a phylogeny (a tinkertoy like structure showing connections of 20 influence), we can use time-structured data to obtain directions of influence. This directed map allows us to model the propagation of financial disturbance through a web of connections. This is an important tool for constructing a portfolio of minimum risk, because it 25 decomposes portfolio risk into an ensemble of interconnected contributing factors which can then be optimized to obtain the desired results. The connections discussed above can be

·.

endogenously or exogenously generated. If the portfolio

in question consists of internal assets, (R&D portfolio, for instance) there is some control as to the degree and

nature of the interconnection. Hence the optimization procedure is somewhat different, as the interconnections are no longer viewed as given but are now variables over which we have some control.

In many areas of interest, different time scales are an important consideration. Examples include bonds with different dates of maturity, and internal portfolios with different payback profiles. Optimizing over such portfolios requires understanding the spectrum of possible paths that a portfolio can take over time, and again interdependencies and large fluctuations make standard approximations of Gaussian uncertainties inaccurate. The present invention uses techniques borrowed from non-standard statistics (large deviation theory, sampling theory) and quantum field theory (path integrals) to generate a forward curve of the behavior of a complex portfolio over time. Not only is the end result important, but the shape of the curve over time is important, as there are many quantities of interest which are dependent on the local shape of the curve.

20

### Evaluating and Minimizing Risk

The present invention includes additional techniques for portfolio optimization using sampling and selection to evaluate and minimize risk for a portfolio of assets with uncertain returns. Consider the general setting in which a holder owns portfolio of assets. The assets may be financial instruments (such as stocks, bonds, options, or other derivatives) or investments in research and development with unknown future payoffs (e.g. the drug leads pursued by a pharmaceutical company). In this setting, where the future rewards are uncertain, there are two important concerns of the holder of the portfolio. Firstly, it is important to

quantify the risk (the amount of money that could be lost) over some time horizon. Secondly, the holder wishes to structure the portfolio so as to minimize the risk. In this document we will focus on answering these questions for portfolios of financial instruments but the ideas are more generally applicable.

Let  $x_i$  (t) represent the value at time t of the ith asset in the portfolio. If there are N assets in the portfolio let  $\mathbf{x}(t)$  be the N-vector representing the values at 10 time of all components of the entire portfolio. The value of the entire port folio to the holder is specified as some function  $\mathbf{f}(\mathbf{x})$  of the values of the assets. Typically, this function might lie a linear combination of the asset volumes times the asset prices. i.e.  $\mathbf{f}(\mathbf{x}) = \sum_{i=1}^N \mathbf{v}_i \mathbf{x}_i$ . Furthermore let

P(x',t'|x,t) represent the probability that the asset prices are x' at time t'>t given that the asset prices were x at time t. If t indicates the present time and x represents the present value of the assets then the expected value of the portfolio at some time t' in the future is

$$V(t'|x,t) = \int dx' f(x') P(x',t'|x,t)$$
.

This value indicates the expected worth of the portfolio but does nothing to tell us what the risk is, *i.e.* what we might conceivably lose. To get at this quantity we realize that from P(x', t'|x, t) we can also determine the probability P(v|t) that the value at. rime t is v:

30 
$$P(v|t) = \int dx' \circ (v'-f(x')) P(x'|x,t)$$
.

This probability is the fundamental quantity which allows us to assess risk since it gives the probabilities for all potential outcomes. Thus for example we can say things like "with 95% confidence the most money that will be lost, is 5 v\*." In this case v\* is determined from the requirement that only 5% of the time will more money be lost, i.e.

 $\int_{\infty}^{v_{i}} dv \ P(v|t) = 0.05.$ 

10 Other measures of risk are similarly based on P(v|t).

The risk will depend sensitively on the precise form of P(x',t'|x,t). To see this, imagine that a pair of assets i and j are anti-correlated with each other (i.e. when the price  $x_i$  increases the price  $x_j$  usually decreases). If we

- 15 invest equally in both stocks then the risk will be small since if the value of one stock goes down the other compensates by going up. On the other hand if the price movements of assets are strongly correlated then risks are amplified. To evaluate and manage risk it then becomes
- 20 paramount to identify set of assets that are correlated/anticorrelated with each other. This observation forms the basis of traditional *value at risk* analyses (VaR) in which the risk is assessed in terms of the covariance matrix in asset prices. The covariance matrix includes all the possible
- 25 pairwise correlations between assets.

While traditional VaR captures pairwise variations in asset prices it completely ignores higher order relationships between variables, e.g. when assets i and j go up asset k goes down. Moreover the Gaussian assumption

30 inherent in VaR is known to be false. What is needed is a more general approach. The present invention describes new

risk management techniques which move beyond pairwise VaR. We propose two methods by which this can be accomplished.

The core of the new ideas is to recognize that information about higher order relationships can be uncovered 5 by looking at the VaR of subsets of assets from the portfolio.

Imagine for a moment that a specific set of assets covaries with each other in some predictable way. Knowledge of this co-variation can be used to devise a risk averse

10 combination of these particular stocks. Since the variation involves all four stocks it can never be determined by only looking at pairs of assets. How might important, clusters of stocks like these be discovered?

The first point to note is that the historical record of asset prices and portfolio values provides a training set from which we can discover these clusters of stocks. The historical record provides a data set which includes the true VaR because the future value of the portfolio is known from the historical data. Let v represent the true VaR for a particular portfolio x at a point T into the future. From the historical record we can form the data set  $D = \{x_i, v_i\}$  and thus estimate the VaR for the assets in the chosen portfolio, i. e. P(v|x). If we assume that the stochastic process that generated D is stationary then the future. Once the mapping from a set of stocks to a VaR has been determined we can search over subsets of stocks to find a combination that gives particularly low VaR.

We begin by making the simple assumption that  $30\ P(v|\mathbf{x}) = \delta\ (v - \mu(\mathbf{x}))\,, \ i.e., \ \text{it is characterized entirely by}$  its mean value  $\mu(\mathbf{x})\,.$  This mean value will differ for different subsets of stocks. Without much additional

complication we could also include the variance around this mean and assume that fluctuations around the mean are Gaussian:  $P(v|x) = N(\mu(x), \sigma^2(x))$ . Obviously from the data D we could try to infer much more complicated 5 relationships but for the moment we stick with simple case.

Given that we can determine the true average VaR for any set of stocks we can identify those assets within a portfolio of N assets that form good combinations. Computationally the following scheme can be used to identify

- 10 good subsets of assets. We assume that the optimal subset of assets is of size n « N. Starting from the original portfolio randomly form portfolios of half the size by sampling stocks (without replacement) from the entire portfolio. The probability that any one of these randomly
- 15 generated profiles contains all n assets is approximately  $1/2^n$ . Thus as we examine significantly more random portfolios than this it is likely we will obtain at least one subset containing all n assets. For each of the randomly generated portfolios of N/2 assets we determine its VaR by
- 20 calculating it from *D* and keep those portfolios with high VaR. In this way we filter out only the most promising portfolios, *i.e.* those that contain the subset that we are seeking. This process can then be iterated further. From these remaining portfolios of size *N*/2 we randomly generate
- make portfolios of half the size (no N/4). Assuming that, at least one of the size N/2 portfolios contained the desired cluster the probability that one of the size N/4 portfolios contains the full subset, is again  $1/2^N$ . We can keep iterating this process of generating and filtering portfolios and each time come closer to good subsets of stocks.

After m iterations of this procedure the portfolio size is  $N/2^m$ . Let  $\overline{m}$ be the largest value of m such that  $N/2^m$ 

≥ n (i.e., the largest portfolio that contain all n assets) and let m = m̄ +1. If our hypothesis is correct then we should see an abrupt increase in the VaR from m̄ to m since we can no longer form a risk averse combination of all the n
5 assets at m. This fact alerts us to the important fact that n must lie between N/2m and N/2m. At this point we can then sample from the portfolio of size N/2m to form new portfolios of size (N/2m + N/2m)/2. The extremal VaR values of these new portfolios will either be comparably to the N/2m in which case (N/2m + N/2m)/2≤ n ≤ N/2m or comparable to N/2m in which case (N/2m ≤ n ≤ (N/2m + N/2m)/2. Iterating this procedure we can determine the optimal subset size n. Knowing the optimal n we can look at many different subsets of this size to eventually pick out the precise combination of the n assets.

15 FIG. 23 provides a flow diagram of a method for evaluating and minimizing risk. In step 2305, the method selects N assets and initializes the portfolio size. In step 2310, the method generates portfolios of the specified size from the selected subsets. On the first iteration of the loop, the selected subset will be the set of N assets. In step 2315, the method computes the value at risk for each portfolio generated in step 2310. In step 2320, the method selects the optimal portfolios (subsets) from those generated by step 2310.

In step 2325, the method determine whether any portfolio contains the desired properties. If at least one portfolio contains the desired properties, control proceeds to step 2330. In step 2330, the method decreases the subset size before generating new portfolios in step 2310 in the next iteration of the loop. If the method determines in step 2325 that no portfolio contains the desired properties,

control proceeds to step 2335. In step 2335, the method iteratively searches for an optimal subset size.

There are many variations to this basic method that might improve its efficiency. It may not be optimal to halve 5 the portfolio size at each step since we might want to have a higher probability of retaining the subset intact. The best number of random portfolios to generate and test can also be fine-tuned to make the search more efficient. Simple analytical model can be built to optimize these algorithm 10 parameters.

Another important extension is to realize that the sample and select method outlined above can be used to determine subsets with any desired properties. Nothing in the above procedure restricts its use to minimize VaR. The 15 method can be used to extremize any figure of merit. Along these lines what happens in practice is that there are actually more than one objective in designing a portfolio: we want to minimize risk but also maximize a profit. Is there a way of modifying the above procedure to account for 20 more than a single objective? At the very least we must be able to balance risk/reward the way it is conventionally done.

There is however a very simple extension of the above method to handle the case of multiple objectives. Subsampled portfolios are generated as usually but the selection criteria amongst portfolios is modified. Now Instead of picking sub-sampled portfolios which have the best VaRs we measure a number of objectives for each of the particular sub-sampled portfolio and keep those sub-sampled portfolios which Pareto dominate all other portfolios (generated at the present iteration or all previously generated portfolios). With this simple change in the selection criteria everything

else proceeds the same way. At the end of the process we obtain a subset which is hopefully good on all objectives.

There are also a host of issues involving sampling to form the new portfolios. In the above I have assumed that 5 the sampling is uniform. Of course this need not be the case. The distribution can be altered over time (much as in boosting) based on the VaR (or distributions over VaR) over previous samples. This also ties into pooling in that the samples may be constructed in a much more deterministic 10 fashion.

There are also a number of possible extensions based upon the fact that the mapping from the asset subset can be determined. At this point it remains unclear how to exploit this fact. The basic procedure might also have to be modified slightly to fit the context.

One of the main difficulties of the procedure may occur in the initial phases of the algorithm. Initially we must filter out subsets that contain the desired small subset. There arises the signal/noise ratio issue on whether the small optimal subset can be detected in the larger portfolio. An estimate of this would be useful to know how many subset samples to generate. This has been tested and the results will be discussed below.

In order to test the algorithm, a random number generator was used to create a "toy" set of stock data in which all of the clusters were known a priori.

FIG. 24 provides the results of the method for evaluating and minimizing risk from executing on 500,000 random draws from this "toy" world. The world consists of 32 stocks in which an investor may invest. The solid square plot is a histogram of VaRs for portfolios which include exactly 16 stocks. The mean VaR for these portfolios is

-0.96 (where negative means the investor loses money). The smaller histogram of hollow circles shows the VaRs only for those portfolios which, through random sampling, failed to include any of the good clusters. The mean for the nostocks-in-clusters (SIC = 0) portfolios is -1.08, clearly worse than for the population as a whole. This is exactly the signal we need to separate the good portfolios from the SIC=0 portfolios.

At the next iteration, the best 16-stock portfolios

10 are selected and 8-stock children are made from them. All

16-stock portfolios which lie outside the 99% confidence
interval of the SIC=0 portfolio distribution are selected.

The number of children to draw from each is determined by the
histograms shown in Figure 25.

- 15 There are three features worth noticing in FIG. 25.

  First, the total number of portfolios that contain zero stocks in clusters has increased dramatically. This is because as you remove stocks, your chance of breaking up clusters increases exponentially. Second, the entire
- 20 distribution has shifted to the left, meaning that the VaRs have gotten worse (mean -1.66). This is because their is value in diversity and diversity must decrease as portfolio size goes down. Third, the distribution of SIC=0 portfolios is still worse (mean = -1.72) than the distribution of all portfolios.

This third feature allows the modeler to determine the number of child portfolios necessary to ensure that some children still contain intact clusters. The number of children containing clusters is negatively binomially

30 distributed as  $\binom{n}{r} p^r (1-p)^{n-r}$ 

where n is the number of children, r is the number of children that contain clusters, and p is the probability of randomly selecting a portfolio which is to the right of the 99% confidence interval of the SIC=0 histogram.

Using these facts, a preliminary model has been calibrated and successfully finds clusters on more than 95% of the runs.

The present invention also includes a method for portfolio modification. There are other methods to try to identify beneficial changes to a portfolio. Traditional VaR theory measures the effects of modifying (i.e. increasing or decreasing the holding) a position in one of the assets. As we have seen, if higher order combinations of assets are important then the effects of a single asset might be minor 15 There is an important practical reason why traditional VaR focuses on the changes of only a single asset. If the portfolio is of size N and we consider changes involving m assets then on the order of N<sup>m</sup> stocks must be examines. Consequently, for practical reasons attention is usually restricted to m=1 or single asset changes.

In contrast, the present method determines the optimal number of assets to change while searching for an optimal portfolio. FIG. 26 displays a flowchart illustrating the method for portfolio modification. In step 2610, the

- method infers a fitness landscape from historical data. The landscape can be inferred from historical data using techniques described in the co-pending application titled, "An Adaptive and Reliable System and Method for Operations Management", U.S. Application No. 09/345,441, filed July 1,
- 30 1999, International Application No. PCT/US99/15096, filed July 2, 1999, the contents of which are herein incorporated by reference.

In step 2620, the method determines the optimal searching distance as described in co-pending international application No. PCT/US99/19916, titled, "A Method for Optimal Search on a Technology Landscape", filed August 31, 1999, the contents of which are herein incorporated by reference. Once m is known, the method searches for optimal portfolios at the optimal searching distance in step 2630. For example, the method shown in FIG. 23 could be used to find an optimal portfolio after the method of FIG. 26 determines the optimal searching distance.

In this case, the landscape is defined over portfolios. The fitness is the VaR measurement of the portfolio and two portfolios are neighbors if they differ in the holding of a single asset. So for example a portfolio of five assets might be represented as [2, 1, 1, 3, 1] meaning that the portfolio consists of two units of asset one, one unit of assets two, thee and five, and three units of asset four.

## 20 Portfolio Management - Optimization of Risk-Revenue

The present invention further includes additional techniques to optimize both risk and revenue for portfolio management. Portfolio optimization (management) normally includes two-fold problem, the control of risk which is usually associated with the volatility (and as it's recently understood with higher moments of the multivariate distribution of the return of the assets constituting the portfolio). This is a formidable problem and a variety of methods have been already proposed to treat it, mention for instance one-dimensional measures of risk in terms of the Value-at-risk (VAR). Also the problem of the so-called heavy

tails has been discussed in the literature in order to manage higher order yet less probable risk.

Mathematically the problem is reduced to minimization of the variance and kurtosis of the weighted sum

$$y = \sum_{i=1}^{n} \lambda_{i} x^{i}$$

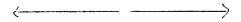
10 of specified stocks under the wealth condition

$$\sum_{i=1}^{n} \lambda_{i} = 1$$

15

5

In what we propose the problem posed is to first search for "good" families of stocks on the basis of all stocks available at the market. For instance a family of two stocks perfectly anticorrelated will simultaneously minimize variance as well as kurtosis (which defines the higher risk contribution) properly created from these stocks. Their image in the vector space of zero-mean deviations is



25

and the angle is given by the correlation coefficient

$$\rho_{ij} = \frac{\operatorname{cov}(x_i x_j)}{\|x_i\| \cdot \|x_j\|}$$

with  $\|x_i\|$  being the standard deviation, the norm in that space, and a vector

 $x_i = \{x_i^1, x_i^2, ..., x_i^m\}$  represents detrended time series of the 5 stock "i".

By calculating the correlation matrix of the stock available at the market we can pick up the families consisting of a reference vector (stock) "a father" and strongly

10 anticorrelated with it members "sons". These members could be statistically independent:  $\rho_{ij} = 0$  such that they are perpendicular to each other. Using standard window techniques robustness of the families is checked and most persistent members are chosen to constitute the basis from 15 which optimal portfolios should be built. Minimization of the portfolio variance inside the family is achieved by means of standard procedure of linear programming or some other known technique. As a result, we have a set of "good" portfolios suitable to make search in order to optimize and expected return.

Given requirements for risk and return the techniques described allows to build up corresponding portfolios. The whole procedure is comprised of three phases:

- Search for good families.
  - a) Creation of the correlation space, including shifted correlations.
    - b) Looking for "anticorrelated" families.
    - c) Checking robustness of the families.

30

Building perspective portfolios

a). Creating two, three and four stock clusters with minimal variance.

- b) Evaluating their risk
- 5 Optimization of expected return (revenue) of a portfolio chosen from the perspective ones.
- The first most difficult part of the program has been checked on the samples consisting of 32 and 100 time

  10 series with intentionally created clusters in the first 32 of them. There were four 2-point clusters, four 3-point clusters, and three 4-point clusters comprising all the first 32 series. Applying the method described we identified all the clusters in the sample of 32 as well as in the sample of 100 series. Corresponding families are listed in FIG. 27, FIG. 28a and FIG. 28b for

$$\rho_{ii} \leq -0.3$$

20

and on FIG. 29, where are also shown lesser couplings between the clusters and some other series. As far as the method is geometrical in character, identification of clusters for the both samples (32 and 100) only differs in time needed to build the correlation matrix, it is proportional to n(n-1)/2.

## Portfolio Risk Management Using Multi-Gaussian Distributions

Portfolio Risk Management (PRM) is essentially 30 based on the techniques applied to estimate probability of "bad events". For that one should know the corresponding probability distribution. During several years after Black

and Scholes in finance business became widespread the VAR machinery which used Gaussian distribution, even though market data showed quite noticeable deviation from it. As a result, the so-called problem of fat tails arose along with a new fashion to treat it on the ground of Levy distribution (later on the truncated Levy distribution). Underline there is no evident reason to regard the latter the only possible cure. Moreover even its relation to the problem from the market point of view, has still remained foggy.

This invention addresses the problem by using a very well-known two-time scale formalism going back to Van der Paul and then Bogolubov and Mitropolskii.

In our case the method gives rise to the two-gaussian distribution (2-GD)

15

(1) 
$$\rho_k(x) = \frac{n_1}{\sqrt{2\pi T_1}} e^{\frac{x^2}{2T_1}} + \frac{n_2}{\sqrt{2\pi T_2}} e^{\frac{x^2}{2T_2}}$$

20 For the sake of simplicity we consider the symmetric distribution with zero mean and the normalization

(2) 
$$n_1 + n_2 = 1$$

25

$$(3) n_1 T_1 + n_2 T_2 = 1$$

This approach allows us to represent market dynamics at a level of description intermediate between macroscopic modeling (one-factor models) and microscopic modeling (individual agent models or multi-factor models, general stochastic processes). Two-gaussian approach being the

simplest exactly solvable model yet can catch certain specific features of the fat tails behavior. It describes two groups of investors acting at the market with different time scale behavior.

For comparison we are using the standard normalized distribution (the Black-Scholes approach)

(4) 
$$g(x) = \frac{1}{\sqrt{2\pi}} e^{\frac{x^2}{2}}$$

that implies the variance is measured in units of the  $\sigma$ . Let us consider the probability, sometimes called VAR, of negative deviations larger than a specified value "a"

$$(5) \qquad P\left(x \le -a\right) = \int_{-\infty}^{-a} \rho(x) dx$$

20 and the difference

(6) 
$$\delta P_r(x \le a) = \int_{-\infty}^{-a} \delta \rho(x) dx = \int_{-\infty}^{-a} (\rho_k(x) - g(x)) dx$$

Since the first two moments are same for the both distributions the difference is proportional to the kurtosis of 2-GD (1):

(7) 
$$\delta P_r(x \le a) \propto K = \frac{\langle x^4 \rangle}{\langle x^2 \rangle^2} - 3 = 3n_1 n_2 (T_2 - T_1)^2$$

30

It can be shown that under conditions (2) and (3) the difference while expanding in the series over moments is

5 (8) 
$$\delta P_L \approx \frac{1}{\sqrt{2\pi}} e^{\frac{x^2}{2}} \frac{K}{24} (x^3 - 3x) + O(\langle x^6 \rangle)$$

This difference can be incorporated by the so-called implied volatility (variance) through considering the effective

10 (implied) gaussian process

$$g(x) = \frac{1}{\sqrt{2\pi\sigma_{im}}} e^{\frac{x^2}{2\sigma_{im}}}$$

15

where  $\sigma_{im}$  = 1 +  $\delta\sigma$  is the implied variance:

(9) 
$$\sigma_{im} = 1 + \frac{1}{24} K(a^2 - 3)$$

20

In order to check out formula (8) we calculated δP by using
the exact distribution (1) and (8) with the kurtosis given by
(7). The approximate formula using implied volatility gives
sufficiently good qualitative description and for certain
values of K and "a" even quantitative one. But there is the
region of a's where the approximate formula (8) along with
the notion of implied volatility (9) works bad. Since the 2GD is a very simple model containing enough parameters to fit
the market data it can be used as an exact tool to calculate
the "fat tail VAR". Moreover as far as pricing formulas for
all the derivatives available at the market linearly depend

on the distribution function the model (1) is exact solvable in the sense that all results are straightforward. For instance the option pricing formula is

5
$$C = e^{-r(T-t)} \int_{x}^{\infty} (S_{T} - X) g(S_{T}) dS_{T} = SN(d_{1}) - Xe^{-r(T-t)}N(d_{2})$$

where S is the current (stock) price of the underlying asset, 10  $S_T$  is the maturity asset price and X is the strike (exercise) price. We see that the price is linear (proportional) over the distribution density and in the case of two gaussians it will contain four terms with the cumulative gaussian functions N(d) instead of two:

15

$$C = e^{-r(T-t)} \int_{x}^{\infty} (S_{T} - X) [n_{1}g(T_{1}; S_{T}) + n_{2}g(T_{2}; S_{T}) dS_{T} + n_{2}N(T_{2}; d_{2})]$$

$$= S[n_{1}N(T_{1}; d_{1}) + n_{2}N(T_{2}; d_{1})] - Xe^{-r(T-t)} [n_{1}N(T_{1}; d_{2})]$$

20

To make the model less restrictive one can consider three (and even more) gaussian distributions

$$g_{m}(n_{i}, T_{i}) = \sum_{i=1}^{m} n_{i}g(1, T_{i})$$

with the normalization conditions

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$$\sum_{i=1}^{n} n_i T_i = 1$$

$$\sum_{i=1}^{n} n_i T_i^2 = 1$$

5

such that the difference

$$\delta P_{m}^{r} = \int_{-\infty}^{-a} \left[ g_{m} \left( n_{i}, T_{i} \right) - g \left( 1 \right) \right] dx$$

10

can be made proportional to any specified moment.

Finally we give the next term in the expansion (8):

15

$$\delta P = \frac{e^{\frac{x^2}{2}}}{\sqrt{2\pi}} \frac{x}{24} \left[ K(x^2 - 3) + \frac{\langle \delta x^6 \rangle}{2} (15 - 10x^2 + x^4) \right]$$

20 with

$$\langle \delta x^6 \rangle = n_2 \left( T_2^2 - T_1^2 \right) \left( T_2 - 1 \right) + K/3$$

25

for the 2-GD.

FIG. 30 discloses a representative computer system 3010 in conjunction with which the embodiments of the present invention may be implemented. Computer system 3010 may be a personal computer, workstation, or a larger system such as a minicomputer. However, one skilled in the art of computer

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systems will understand that the present invention is not limited to a particular class or model of computer.

As shown in FIG. 30, representative computer system 3010 includes a central processing unit (CPU) 3012, a memory 5 unit 3014, one or more storage devices 3016, an input device 3018, an output device 3020, and communication interface 3022. A system bus 3024 is provided for communications between these elements. Computer system 3010 may additionally function through use of an operating system such 10 as Windows, DOS, or UNIX. However, one skilled in the art of computer systems will understand that the present invention is not limited to a particular configuration or operating system.

Storage devices 3016 may illustratively include one
15 or more floppy or hard disk drives, CD-ROMs, DVDs, or tapes.
Input device 3018 comprises a keyboard, mouse, microphone, or
other similar device. Output device 3020 is a computer
monitor or any other known computer output device.
Communication interface 3022 may be a modem, a network
interface, or other connection to external electronic
devices, such as a serial or parallel port

While the above invention has been described with reference to certain preferred embodiments, the scope of the present invention is not limited to these embodiments. One skill in the art may find variations of these preferred embodiments which, nevertheless, fall within the spirit of the present invention, whose scope is defined by the claims set forth below.

30

## Claims

- 2. A method as in claim 1 further comprising the steps of:

  repeating said executing one or more os said economic models step, said determining one or more fitnesses

step, and said searching step to adapt said space of economic

20 models to changes in the actual data.

- 3. A method for generating models of an economy as in claim 1 further comprising the steps of: modifying said one or more economic models to
  25 increase said corresponding one or more fitnesses.
  - 4. A method as in claim 1 further comprising the steps of:

combining at least two of said economic models to

30 create at least one new economic model; and
adding said at least one new economic model to said
space of economic models.

5. A method as in claim 4 wherein said combining step further comprises the step of:

defining a space of stacking function of said economic models; and

- applying one or more genetic operators over said space of stacking functions to create said at least one economic model.
- 6. A method as in claim 1 wherein said space of 10 economic models comprise one or more members of the group consisting of AR(n), ARV, ARCH, GARCH, Black Scholes, Langevain equations, Levy and truncated Levy.
- 7. A method as in claim 3 wherein said space of economic models comprises one or more hybrid models wherein said hybrid models comprise one or more hybrid models wherein said hybrid models comprise one or more components, each of said components contributing at least one portion of said predicted time series.

20

8. A method as in claim 7 wherein said modifying said one ore more economic models step comprises the steps of:

adjusting a permutation of said components of said 25 hybrid models; and

adjusting said contribution of said components of said hybrid models.

10. A method as in claim 9 wherein said determining one or more fitnesses step further comprises the step of:

comparing said observables to said actual data.

5

- 11. A method as in claim 9 wherein said extracting step uses one or more techniques from the group consisting of visual analysis, principal component analysis, data mining, localized principal component analysis and independent 10 component analysis.
  - 12. A method as in claim 9 further comprising the step of determining a fitness landscape of said one ore more fitnesses overs said space of economic models.

. 15

13. A method as in claim 12 wherein said searching step comprises the step of:

searching over said fitness landscape for said at least one economic model having the maximal fitness.

20

14. A method as in claim 12 further comprising the step of:

computing at least one probability distribution for said plurality of observables.

25

15. A method as in claim 14 further comprising the step of:

comparing said probability distribution for said plurality of observables to a corresponding probability distribution of said actual data;

determining a distance between one of said economic models and another of said economic models ons said fitness

landscape by computing a comparison between said probability distribution of said one economic model and said probability distribution of said another economic model.

- 16. A method as in claim 15 wherein said determining a distance step uses one or more techniques from the group consisting of the Randan-Nikodyn Thereom and the Kulback-Liebler method.
- 10 17. A method as in claim 1 further comprising the step of:

determining at least one state of the economy from said actual data.

- 18. A method as in claim 17 wherein said state of the economy comprises a current data and a plurality of past data for a plurality of assets in the economy.
- 19. A method as in claim 18 wherein said current 20 data and said past data comprise prices of said plurality of assets.
- 20. A method as in claim 17 further comprising the step of repeating said determining at least one state of the economy step over time to assess a measure of stationarity or non-stationarity of the economy.
- 21. A method as in claim 20 further comprising the step of repeating said executing one or more os said economic models step, said determining one or more fitnesses step, and said searching step to adapt said space of economic models to changes in said state of the economy.

22. A method as in claim 21 further comprising the step of tuning a rate of said searching for at least one of said economic models having maximal fitness in accordance with said measure of stationarity or non-stationarity of the 5 economy.

- 23. A method as in claim 17 wherein said predicted time series are determined from executing said one or more economic models in accordance with said state of the economy.
- 24. A method as in claim 1 further comprising the
  step of:

performing risk minimization from said predicted time series.

15

25. Computer executable software code stored on a computer readable medium, the code for performing analysis and prediction of economic markets, the code comprising: code to initialize a space of economic models;

code to execute one or more of said economic models to generate a corresponding one or more predicted time series:

code to determine one or more fitnesses
corresponding to said one or more economic models by
comparing said plurality of predicted time series to actual
data; and

code to search for at least one of said economic models having a maximal fitness.

26. A programmed computer system for performing analysis and prediction of economic markets comprising at least one memory having at least one region storing computer

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executable program code and at least one processor for executing the program code stored in said memory, wherein the program code comprises:

code to initialize a space of economic models;

code to execute one or more of said economic models

to generate a corresponding one or more predicted time

series:

code to determine one or more fitnesses
corresponding to said one or more economic models by
10 comparing said plurality of predicted time series to actual
data; and

code to search for at least one of said economic models having a maximal fitness.

15 27. A system for performing analysis and making predictions of a securities market comprising

a model of the securities market comprising:

a plurality of dealer agents representing a corresponding plurality of market makers in the securities 20 market, each of said dealer agents having at least one of a plurality of dealer strategies for setting a price of securities:

a plurality of investor agents representing a corresponding plurality of investors in the securities are market, wherein said investor agent determines whether to buy

or sell one or more of the securities at a given price;

at least one market model comprising one or more rules for exchanging the securities; and

a simulator for executing said model to perform analysis on the securities market.

28. A system as in claim 27 wherein said plurality of dealer agents set a bid price, bid volume, offer price and offer volume of a security.

- 29. A system as in claim 27 wherein said plurality of dealer strategies comprise static strategies.
- 30. A system as in claim 27 wherein said plurality of dealer strategies comprise learning strategies.

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- 31. A system as in claim 27 wherein said plurality of dealer strategies comprise price discovery strategies.
- 32. A system as in claim 27 wherein said plurality 15 of dealer strategies comprise parasitic strategies.
- of dealer strategies comprise a basic dealer strategy, said basic dealer strategies maintain its price on a security until it receives a predetermined number of trades on the buy or sell side wherein it decreases or increases its price on the security respectively.
- 34. A system as in claim 27 wherein said plurality
  25 of dealer strategies comprise a price volume dealer strategy,
  said price volume dealer strategy deduces demand and supply
  for a security from market data and sets its price for the
  security in accordance with said demand and said supply.
- 35. A system as in claim 27 wherein said plurality of dealer strategies comprises a new volume dealer strategy wherein said new volume dealer strategy, said new volume

dealer strategy raises or lowers its price on the security when it observes more buys or more sells respectively for the security.

5 36. A system as in claim 27 wherein said plurality of dealer strategies comprise a parasitic dealer strategy, said parasitic dealer strategy waits for a sufficiently narrow spread with sufficient volume for a security before buying or selling the security inside the spread.

10

- 37. A system as in claim 27 wherein said plurality of dealer strategies comprises a new parasite strategy, said new parasite strategy decides whether to buy or sell the security inside the spread based on observed excess supply and/or excess demand for the security.
- 38. A system as in claim 27 wherein said plurality of dealer strategies comprise a matching dealer strategy, said matching dealer strategy learns connections between one ore more observations and one or more actions and makes decisions based on said learned connections.
- 39. A system as in claim 38 wherein said observations comprises one or more of the group consisting of inventory level, spread size, bid price relative to market value and trade volume.
- 40. A system as in claim 38 wherein said actions comprises one or more of the group consisting of raising a 30 price, increasing a bid and narrowing the spread.

41. A system as in claim 27 wherein said plurality of dealer strategies comprise a classifier dealer strategy, said classifier dealer strategy learns pattern connections between one or more patterns of observations and one or more actions and makes decisions based on said learned pattern connections.

- 42. A system as in claim 27 wherein said plurality of dealer strategies comprise a dynamical system dealer, said 10 dynamical system dealer uses a discrete dynamical system to set its bid price, ask price and mean price.
- 43. A system as in claim 27 wherein said plurality of investor agents comprises a degree of informedness

  15 representing a measure of said investor agents knowledge of a true value of a security.
- 44. A system as in claim 27 wherein said one or more rule for exchanging securities comprises at least one 20 tick price.
  - 45. A system as in claim 27 further comprising a plurality of parameters that quantify an ability of the market to track prices of the securities.

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46. A system as in claim 45 wherein said
parameters comprises one or more members of the group
consisting of the root mean square of the difference between
a bid price and a time value, a root mean square of the
difference between an ask price and a true value, an average
value of a spread and a standard deviation of the spread.

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47. Computer executable software code stored on a computer readable medium, the code for performing analysis and making predictions of a securities market, the code comprising:

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code to model the securities market comprising:

code to represent a plurality of market makers
in the securities market including a plurality of dealer
strategies for setting a price of securities;

code to represent a plurality of investors in

10 the securities market and to determine whether to buy or sell
one or more of the securities at a given price;

code to represent the market including one or more rules for exchanging the securities; and

code to simulate the model to perform analysis on 15 the securities market.

48. A programmed computer system for performing analysis and making predictions of a securities market comprising at least one memory having at least one region storing computer executable program code and at least one processor for executing the program code stored in said memory, wherein the program code comprises:

code to model the securities market comprising:

code to represent a plurality of market makers

25 in the securities market including a plurality of dealer strategies for setting a price of securities;

code to represent a plurality of investors in the securities market and to determine whether to buy or sell one or more of the securities at a given price;

30 code to represent the market including one or more rules for exchanging the securities; and

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code to simulate the model to perform analysis on the securities market.

49. A method for creating a portfolio of assets 5 comprising the steps of:

initializing at lease one current portfolio of assets having one or more desired properties;

generating at least one next portfolio of assets to form said current portfolio, said next portfolio having a 10 smaller size then said current portfolio;

repeating said generating step after replacing said current portfolio with said next portfolio while said next portfolio has the one or more desired properties;

defining a size range having an upper limit equal 15 to the size of said current portfolio and a lower limit equal to the size of said next portfolio; and

searching for an optimal portfolio of assets to within said size range.

20 50. A method as in claim 49 wherein said generating at least one next portfolio comprises the steps of:

25

sampling said assets from said at least one current portfolio to form a plurality of candidate portfolios; and selecting said at least one portfolio from said candidate portfolios.

51. A method as in claim 50 wherein said selecting said at least one next portfolio step comprises the step of choosing said candidate portfolios that are optimal with respect to the one or more desired properties.

- 52. A method as in claim 50 wherein said selecting said at least one next portfolio step comprises the step of:

  choosing at least one of said candidate portfolios that is pareto optimal with respect to the one or more

  5 desired properties.
  - 53. A method as in claim 50 wherein said sampling of said assets has a uniform distribution.
- 10 54. A method as in claim 50 wherein said sampling of said assets has a distribution that varies with time.
  - 55. A method as in claim 54 wherein said sampling step further comprises the steps of:
- altering said distribution over time based on said one or more desired properties over previous choices of said candidate portfolios.
- 56. A method as in claim 55 wherein said altering 20 said distribution over time step boosting.
  - 57. A method as in claim 49 wherein said searching for an optimal portfolio of assets step comprises the steps of:
- determining an intermediate size within said size range;
  - generating a lease on intermediate portfolio of assets of said intermediate size from said current portfolio; and
- $_{
  m 30}$  if said intermediate portfolio has the one or more discreet properties

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modifying said upper limit of said size range to equal said intermediate size;

else

modifying said lower limit of said size range 5 to equal said intermediate size.

- 58. A method as in claim 57 wherein said searching for an optional portfolio of assets to step further comprises the step of:
- repeating said steps of claim 53 to converge to said optimal portfolio of assets.
- 59. A method as in claim 49 wherein said size of said current portfolio is defined as the number of said 15 assets in said current portfolio.
  - 60. A method as in claim 49 wherein said size of said next portfolio is a fraction of said size of said current portfolio.

20

- 61. A method as in claim 60 wherein said fraction is %.
- 62. A method as in claim 60 wherein said
  25 generating at least one next portfolio of assets step
  comprises the step of:

tuning said size of said next portfolio.

63. A method as in claim 49 further comprising the 30 step of:

determining the number of said at least one next portfolios to generate.

- 64. A method that as in claim 63 form the comprising the step of timing said number of said at least on next portfolios to generate.
- 5 65. A method as in claim 49 wherein said one or more desired properties comprise a low value at risk.
- 66. Computer executable software code stored on a computer readable medium, the code for creating a portfolio 10 of assets, the code comprising:

code to initialize at lease one current portfolio of assets having one or more desired properties;

code to generate at least one next portfolio of assets to form said current portfolio, said next portfolio 15 having a smaller size then said current portfolio;

code to repeat said generating step after replacing said current portfolio with said next portfolio while said next portfolio has the one or more desired properties;

code to define a size range having an upper limit
20 equal to the size of said current portfolio and a lower limit
equal to the size of said next portfolio; and
code to search for an optimal portfolio of assets

to within said size range.

- 25 67. A programmed computer system for creating a portfolio of assets comprising at least one memory having at least one region storing computer executable program code and at least one processor for executing the program code stored in said memory, wherein the program code comprises:
- 30 code to initialize at lease one current portfolio of assets having one or more desired properties;

code to generate at least one next portfolio of assets to form said current portfolio, said next portfolio having a smaller size then said current portfolio;

code to repeat said generating step after replacing

5 said current portfolio with said next portfolio while said
next portfolio has the one or more desired properties;

code to define a size range having an upper limit equal to the size of said current portfolio and a lower limit equal to the size of said next portfolio; and

- 10 code to search for an optimal portfolio of assets to within said size range.
  - 68. A method for optimizing a portfolio of assets comprising the steps of:
- determining a fitness landscape representation over a space of portfolios;

determining at least one optimal searching distance in said fitness landscape representation; and

searching for optional ones of said portfolio of 20 assets at said optimal distances.

- 69. A method as in claim 68 wherein said portfolio of assets is defined as a vector corresponding to said assets wherein each element of said vector identifies the umber of said corresponding assets in said portfolio.
- 70. A method as in claim 69 wherein said distances between a first of said portfolio and the second one of said portfolios is defined as the difference between said vector of said first portfolio and said vector of said second portfolio.

- 71. A method as in claim 68 wherein said fitness of said landscape representation comprises a value at risk.
- 72. A method as in claim 68 wherein said

  5 determining a fitness landscape representation step comprises
  the step of inferring said fitness landscape from historical
  data.
- 73. Computer executable software code stored on a 10 computer readable medium, the code for optimizing a portfolio of assets, the code comprising:

code to determine a fitness landscape representation over a space of portfolios;

code to determine at least one optimal searching

15 distance in said fitness landscape representation; and

code to search for optional ones of said portfolio

of assets at said optimal distances.

74. A programmed computer system for optimizing a 20 portfolio of assets comprising at least one memory having at least one region storing computer executable program code and at least one processor for executing the program code stored in said memory, wherein the program code comprises:

code to determine a fitness landscape

25 representation over a space of portfolios;

code to determine at least one optimal searching distance in said fitness landscape representation; and code to search for optional ones of said portfolio of assets at said optimal distances.

30

75. A method for creating a portfolio of a plurality of assets comprising the steps of:

determining a plurality of anti-correlated families wherein each of said anti-correlated families contains two or more of said plurality of assets that are anti-correlated; and

- determining one or a more perspective portfolios of said plurality of assets from said plurality of anticorrelated families.
- 76. A method in claim 75 further comprising the 10 step of:

receiving one or more time series corresponding to one or more of said plurality of assets.

77. A method as in claim 76 further comprising the 15 step of:

determining correlations among said plurality of assets.

78. A method as in claim 75 wherein said 20 determining a plurality of anti-correlated families step comprises the steps of:

selecting at least one of said plurality of assets to be a first member of one of said anti-correlated families; determining one or more of said plurality of assets

25 having a value of said correlation with said first member of said anti-correlated family that is less than a negative limit; and

including said one or more assets having a correlation value that is less than the limit as additional members in said anti-correlated family.

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79. A method as in claim 78 further comprising the step of separating said steps of claim 4 for another one of said plurality of assets to determine another of said plurality of anti-correlated families.

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80. A method as in claim 77 further comprising the step of:

eliminating drift from said one or more time series to create corresponding one or more detrended time series.

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- 81. A method as in claim 80 wherein said correlations among said plurality of assets is determined from said one or more time series.
- 15 82. A method as in claim 77 wherein said correlations are shifted in time.
- 83. A method as in claim 75 wherein said determining one or more perspective portfolios step comprises 20 the step of selecting one of said plurality of anticorrelated families;

determining percentages of said assets from said selected family to include in one of said perspective portfolios.

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84. A method as in claim 83 further comprising the steps of repeating said selecting step and said determining a percentage of each of said assets step with different ones of said anti-correlated families to determine said one or more perspective portfolios.

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85. A method as in claim 83 wherein said percentages of said assets from said selected family are determined from said perspective portfolio with a minimal variance.

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- 86. A method as in claim 75 further comprising the step of choosing at least one of said perspective portfolios as said portfolios of assets.
- 10 87. A method as in claim 86 for the comprising the step of optimizing an expected return of said portfolio of assets.
- 88. Computer executable software code stored on a 15 computer readable medium, the code for creating a portfolio of a plurality of assets, the code comprising:

code to determine a plurality of anti-correlated families wherein each of said anti-correlated families contains two or more of said plurality of assets that are anti-correlated; and

code to determine one or a more perspective portfolios of said plurality of assets from said plurality of anti-correlated families.

25

89. A programmed computer system for creating a portfolio of a plurality of assets comprising at least one memory having at least one region storing computer executable program code and at least one processor for executing the program code stored in said memory, wherein the program code comprises:

code to determine a plurality of anti-correlated families wherein each of said anti-correlated families

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contains two or more of said plurality of assets that are anti-correlated; and

code to determine one or a more perspective portfolios of said plurality of assets from said plurality of anti-correlated families.

90. A method of modeling a portfolio of assets comprising the step of:

defining a probability distribution of the value of 10 the portfolio of assets with two or more Gaussian distributions.

91. A method as in claim 90 wherein said two or more Gaussian distributions comprise at least one parameter.

15

92. A method as in claim 91 further comprising the step of:

receiving historical data on the value of the portfolio of assets; and

- determining values for said at least one parameter from said historical data.
- 93. A method as in claim 91 wherein said defining a probability distribution a probability distribution step comprises the step of:

defining said probability distribution as a sum of said two or more Gaussian distributions.

94. A method as in claim 93 wherein said defining 30 said probability distribution as a sum step comprises the step of defining said probability distribution as:

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$$g_{m}(n_{i}, T_{i}) = \sum_{i=1}^{m} n_{i}g(1, T_{i})$$

- $n_i$  represent normalization parameters
- $T_i$  represent variance

5

- 95. A method that as in claim 94 wherein said defining said probability distribution as a sum step further comprises the step of:
- defining a plurality of normalization conditions
  as:

$$\sum n_1 = 1$$

$$\sum n_1 T_i = 1$$

$$\sum n_1 T_i^2 = 1$$

15

- 96. A method as in claim 90 for further comprising the step of:
- computing a value at risk from said probability distribution of said two or more Gaussian distributions.

20

97. A method as in claim 90 for further comprising the step of:

computing an option price from said probability distribution of said two or more Gaussian distributions.

25

98. A method as in claim 97 wherein said computing an options price step comprises the steps of:

determining an option pricing formula as:

$$c = e^{-r(T-t)} \int_{x}^{\infty} (S_{T} - X) g(S_{t}) dS_{T}$$

$$= S[n_{1}N(T_{1}; d_{1}) + n_{2}N(T_{2}; d_{1})] - Xe^{-r(T-t)}[n_{1}N(T_{1}; d_{2})]$$

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#### wherein:

- T represents variance
- N represents normal density function
- 5 t represents time
  - 99. Computer executable software code stored on a computer readable medium, the code for modeling a portfolio of assets, the code comprising:
- code to define a probability distribution of the value of the portfolio of assets with two or more Gaussian distributions.
- 100. A programmed computer system for modeling a

  15 portfolio of assets comprising at least one memory having at
  least one region storing computer executable program code and
  at least one processor for executing the program code stored
  in said memory, wherein the program code comprises:
- code to define a probability distribution of the 20 value of the portfolio of assets with two or more Gaussian distributions.

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## WORLD INTELLECTUAL PROPERTY ORGANIZATION International Bureau



### INTERNATIONAL APPLICATION PUBLISHED UNDER THE PATENT COOPERATION TREATY (PCT)

(51) International Patent Classification 7:
G06F 17/60

(11) International Publication Number:

(43) International Publication Date:

WO 00/38094

A2

29 June 2000 (29.06.00)

(21) International Application Number:

PCT/US99/30640

(22) International Filing Date:

22 December 1999 (22,12,99)

(30) Priority Data:

60/113,502

22 December 1998 (22.12.98) US

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(81) Designated States: AE, AL, AM, AT, AU, AZ, BA, BB, BG, BR, BY, CA, CH, CN, CR, CU, CZ, DE, DK, EE, ES, FI, GB, GD, GE, GH, GM, HR, HU, ID, IL, IN, IS, JP, KE, KG, KP, KR, KZ, LC, LK, LR, LS, LT, LU, LV, MA, MD, MG, MK, MN, MW, MX, NO, NZ, PL, PT, RO, RU, SD, SE, SG, SI, SK, SL, TJ, TM, TR, TT, UA, UG, US, UZ, VN, YU, ZA, ZW, ARIPO patent (GH, GM, KE, LS, MW, SD, SL, SZ, TZ, UG, ZW), Eurasian patent (AM, AZ, BY, KG, KZ, MD, RU, TJ, TM), European patent (AT, BE, CH, CY, DE, DK, ES, FI, FR, GB, GR, IE, IT, LU, MC, NL, PT, SE), OAPI patent (BF, BJ, CF, CG, CI, CM, GA, GN, GW, ML, MR, NE, SN, TD, TG).

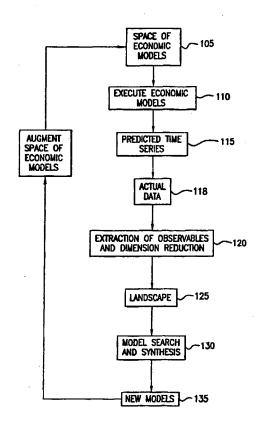
#### Published

Without international search report and to be republished upon receipt of that report.

#### (54) Title: A SYSTEM AND METHOD FOR THE ANALYSIS AND PREDICTION OF ECONOMIC MARKETS

#### (57) Abstract

The present invention presents a system and method of economic analysis and prediction which dynamically adapts to a changing economic environment by selecting or synthesizing an economic model from a set of economic models based on the selected model's ability to make accurate predictions about an actual economic market. Specifically, the method and system of the present invention forms a space of different economic models, forms a behavorial landscape by extracting observables from executions of the economic models, and performs model selection and composite model synthesis through optimization over the behavioral landscape.



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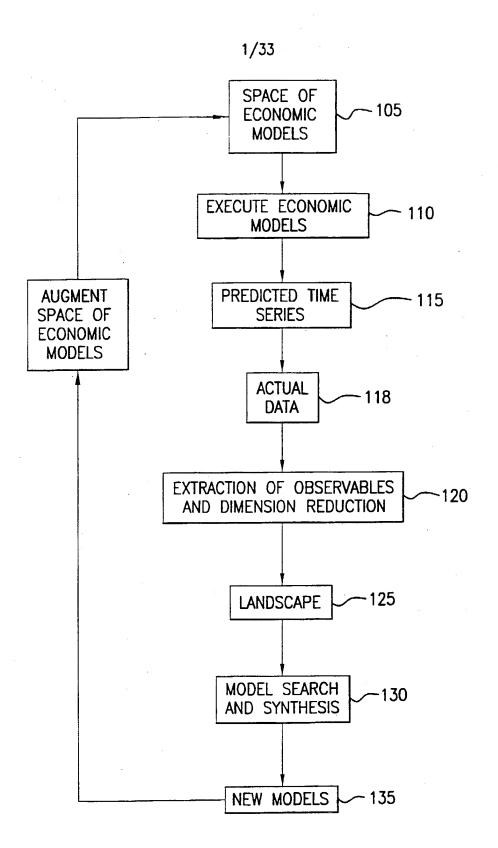
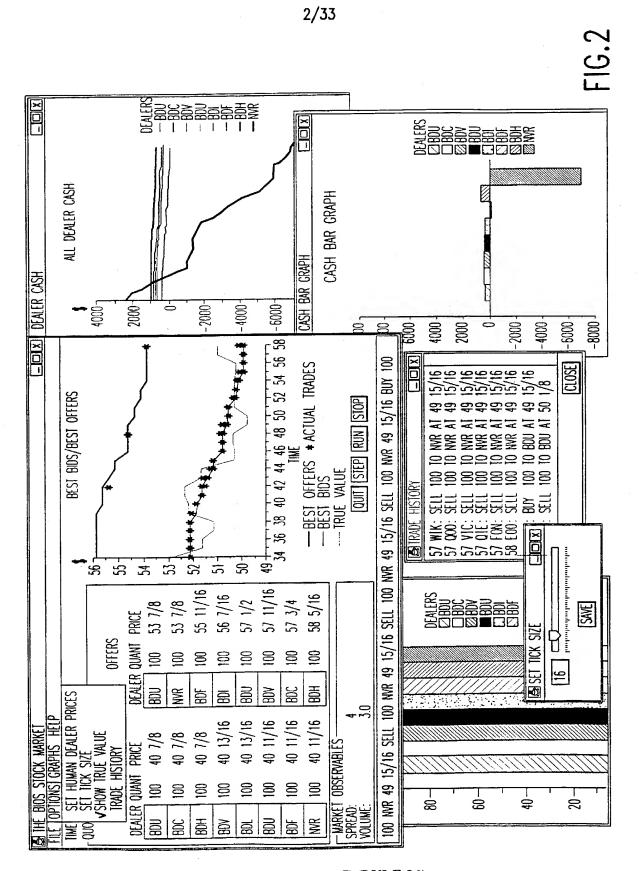
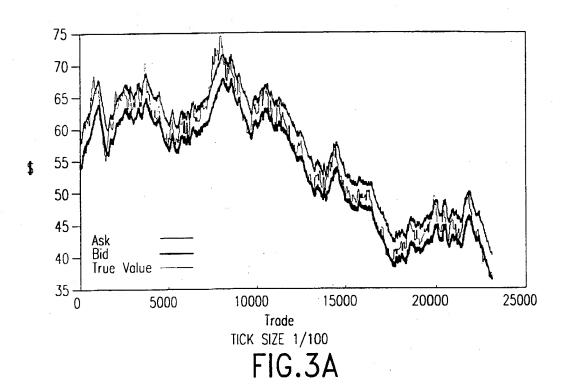


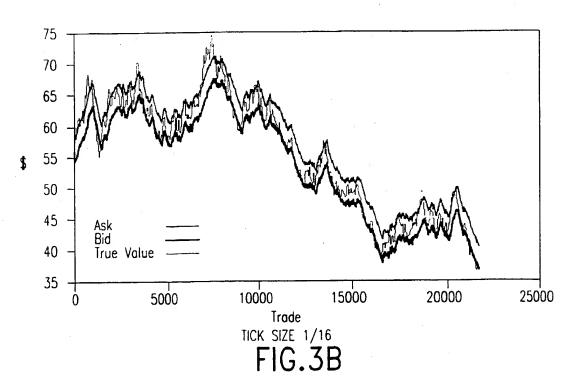
FIG.1



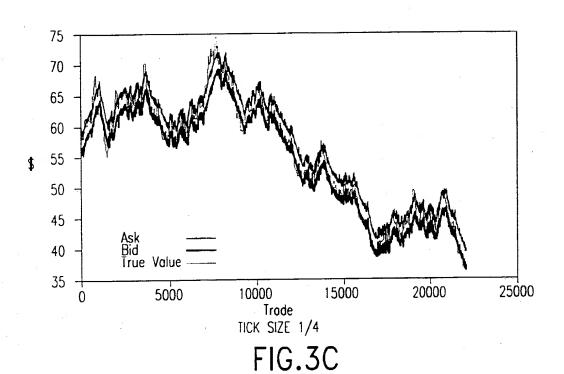
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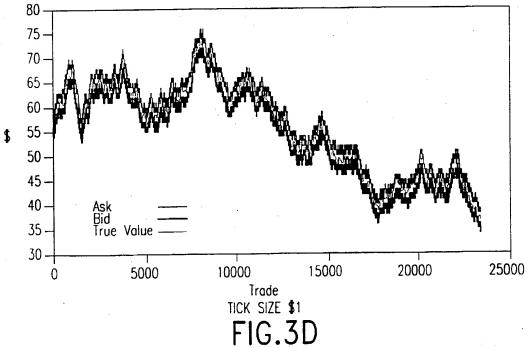
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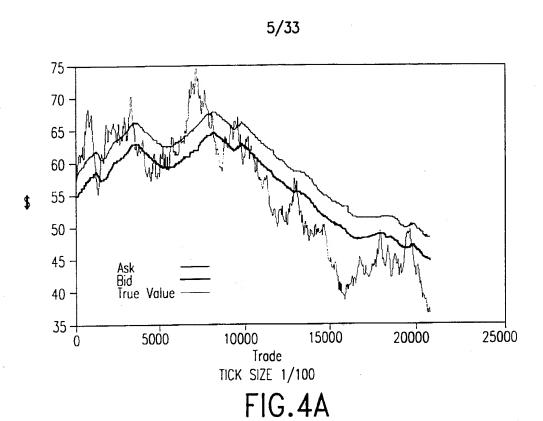


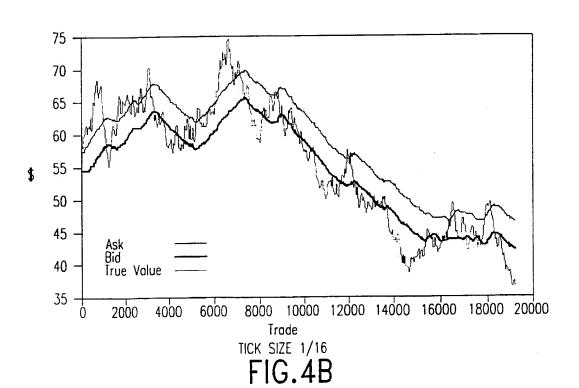
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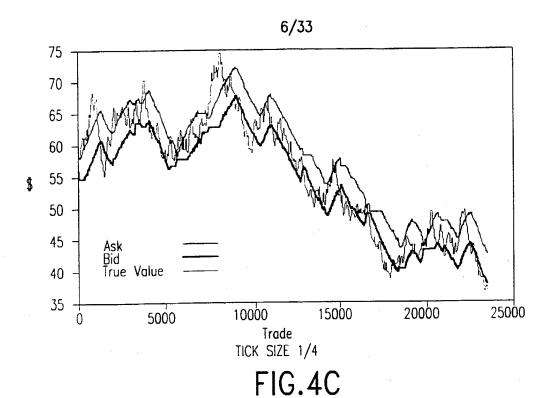


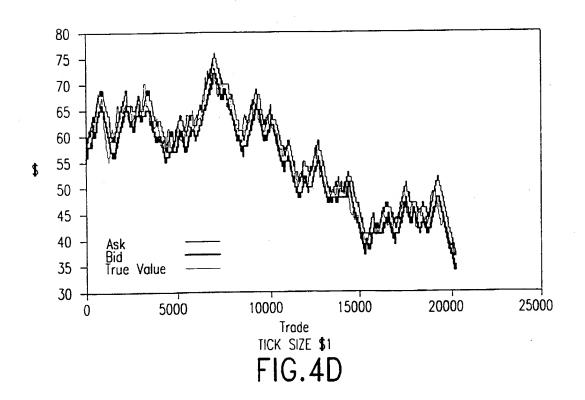
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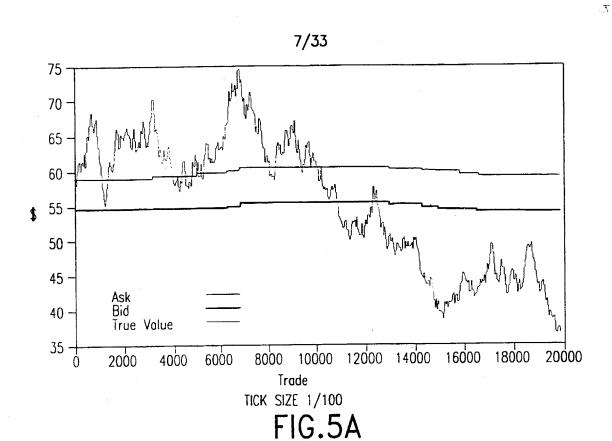




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75 70 65 60 55 \$ 50 45 Ask Bid 40 -True Volue 35 20000 10000 15000 25000 5000 Trade TICK SIZE 1/16 FIG.5B

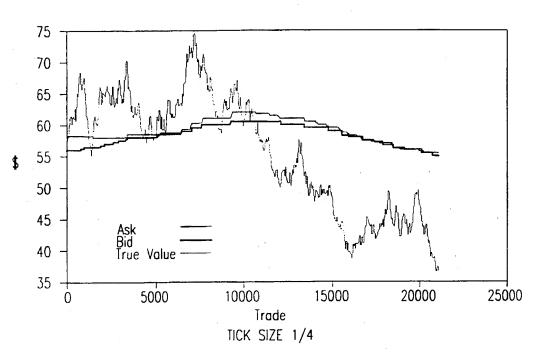


FIG.5C

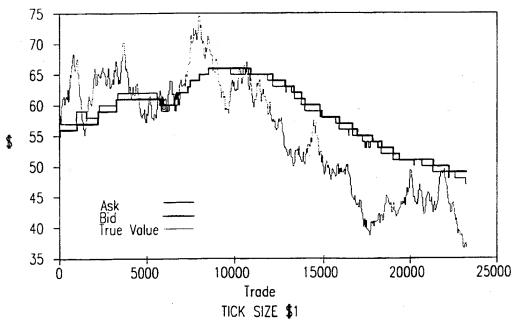
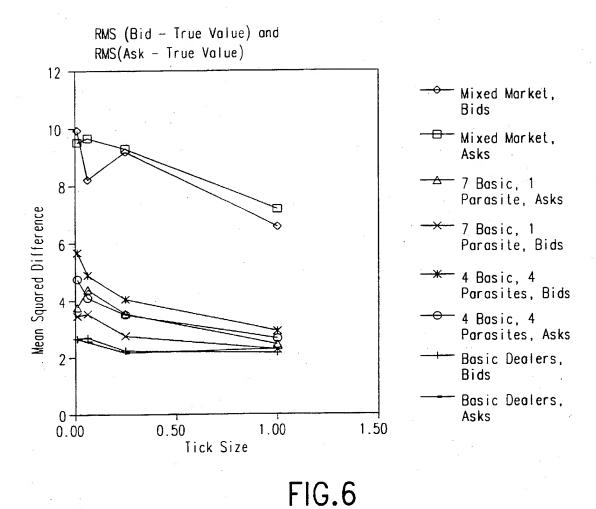


FIG.5D

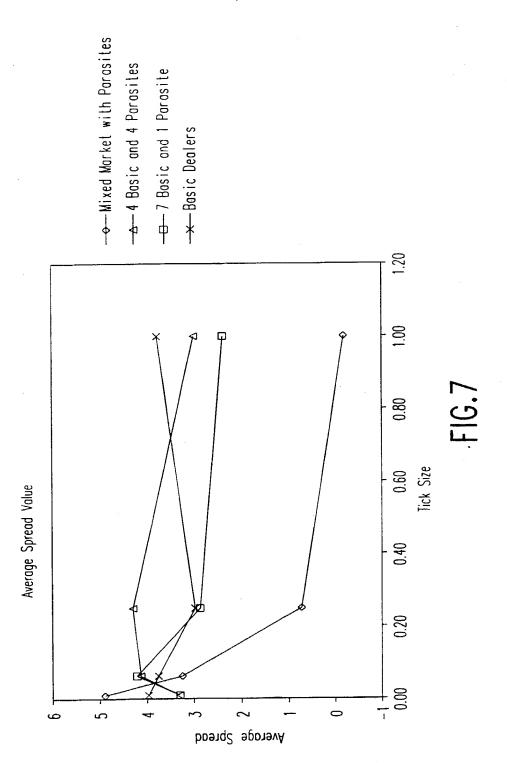
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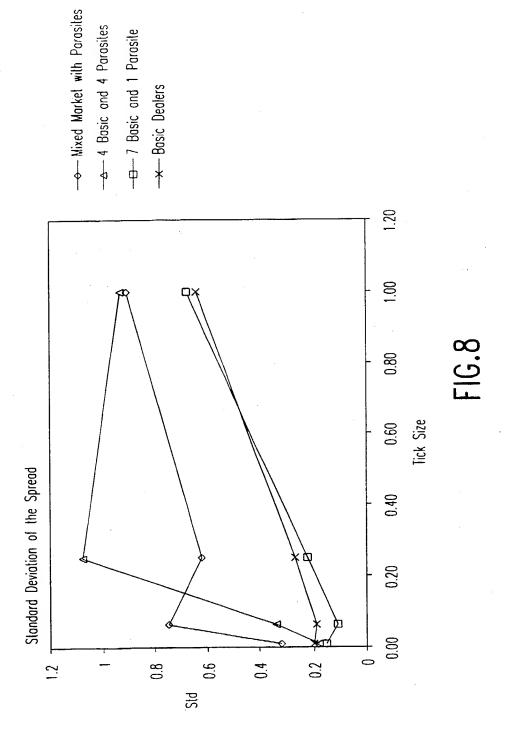


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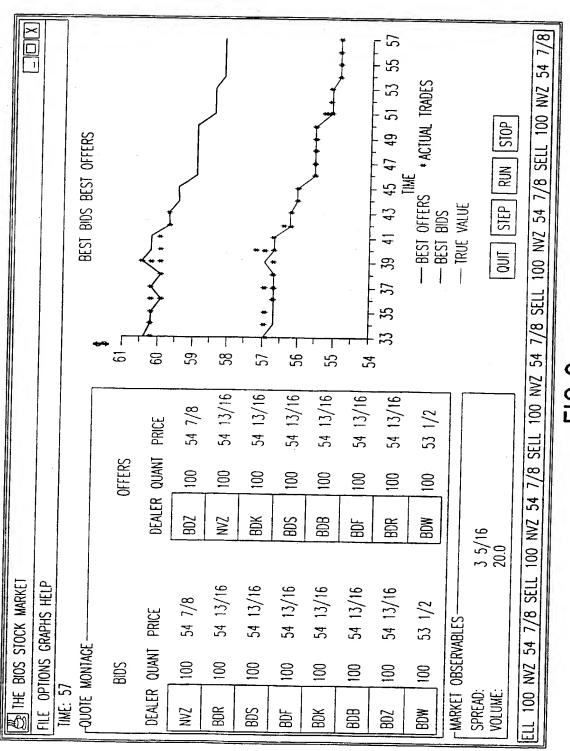
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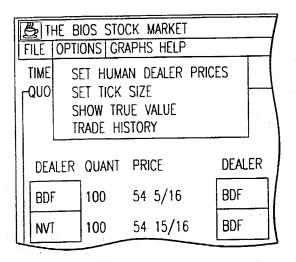


FIG.10

SET HUMAN DEALER PRICE		
		NEW BID: 53.8125 NEW OFFER: 57.9375
RAISE QUOTES	RAISE BID	RAISE OFFER
LOWER QUOTES	LOWER BID	LOWER OFFER

FIG.11A

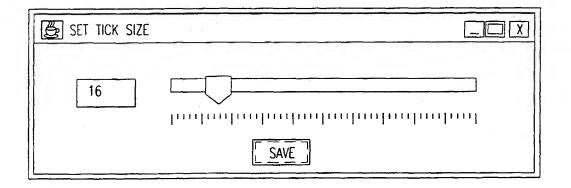


FIG.11B

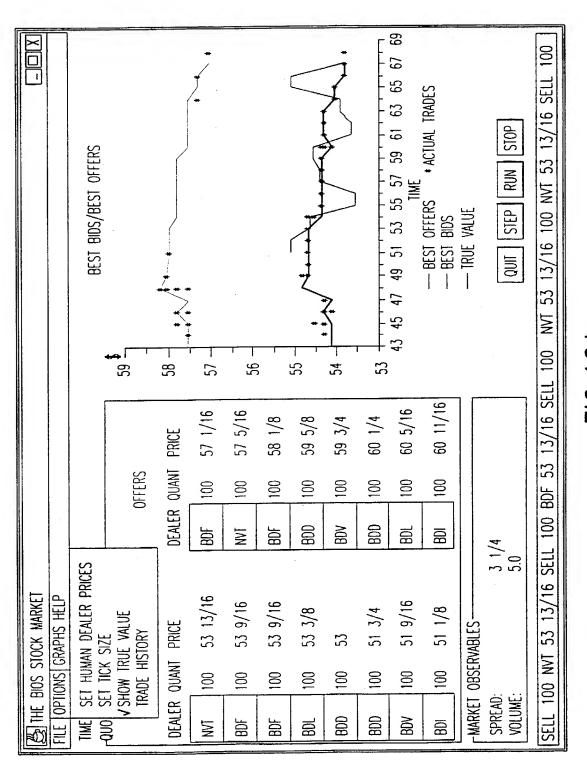


FIG. 12A

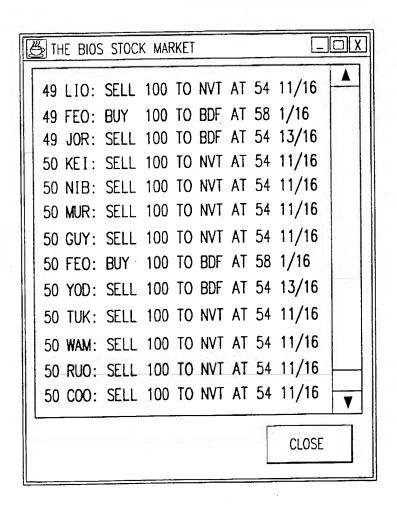


FIG.12B

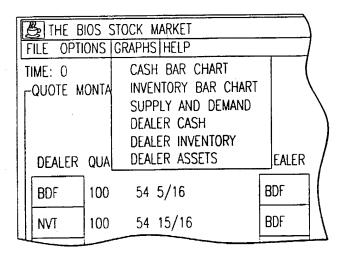


FIG.13

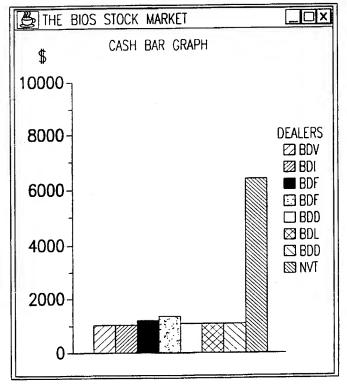


FIG.14

WO 00/38094

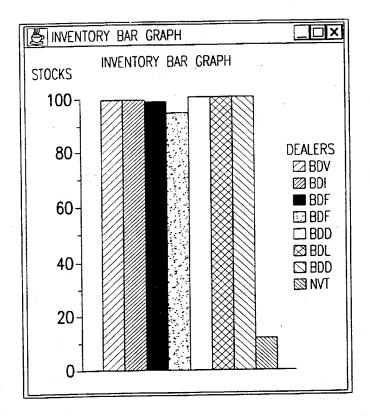


FIG.15

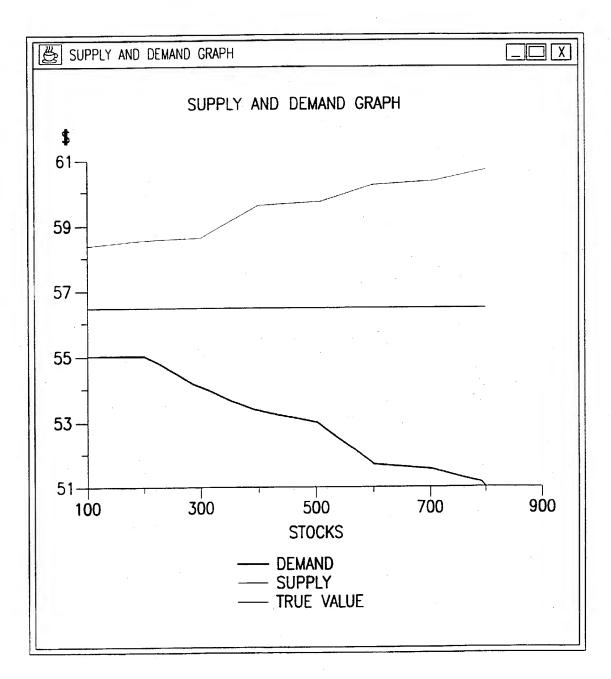


FIG.16

PCT/US99/30640

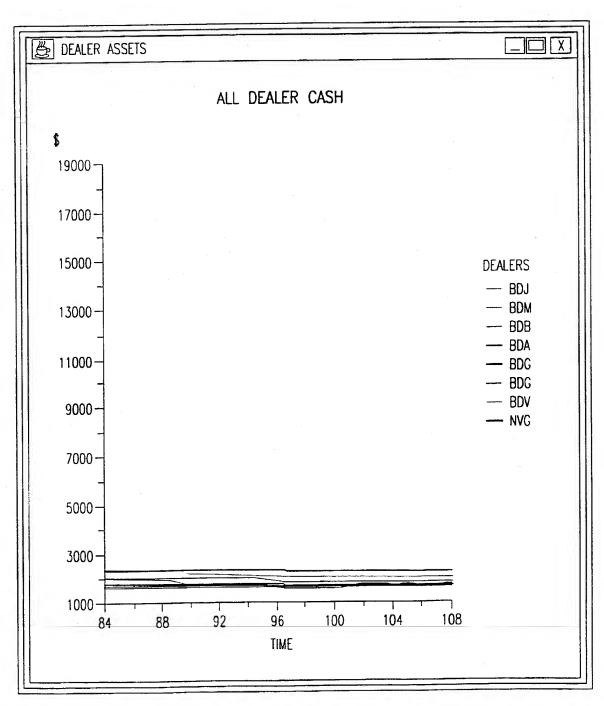


FIG.17

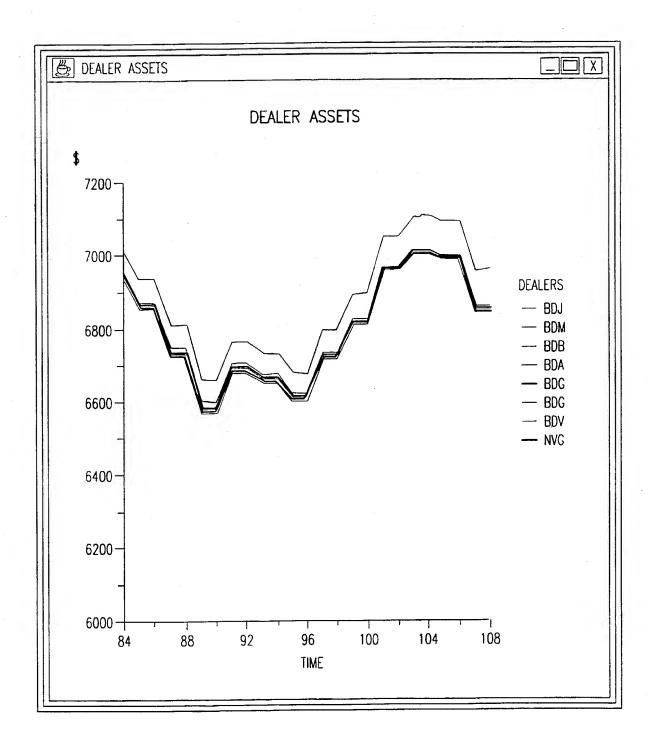


FIG.18

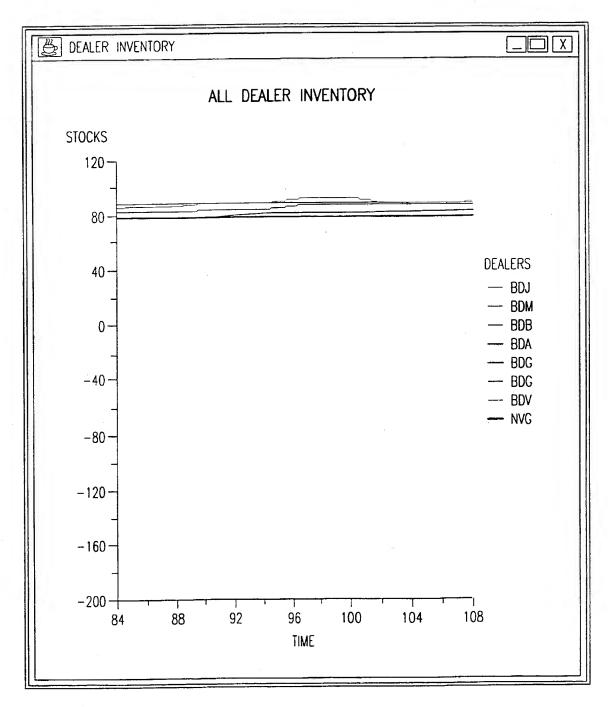
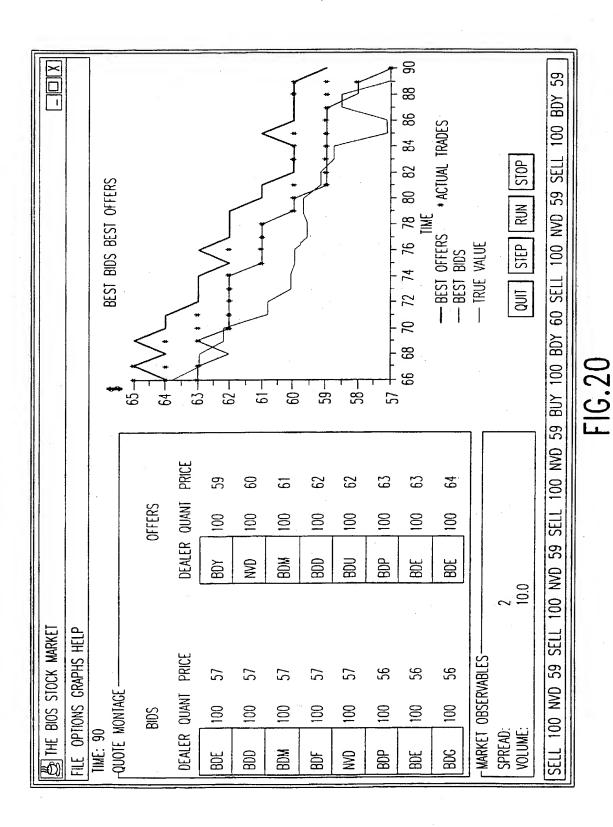


FIG.19

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**SUBSTITUTE SHEET (RULE 26)** 

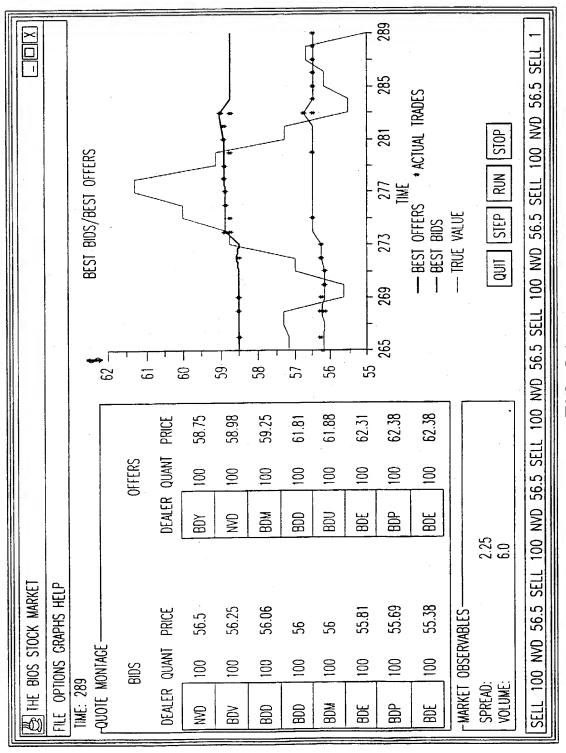


FIG. 21

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						· 						
) TRUE VALUE	4 PARASITES AND 4 NEWVOLUME BASIC DEALERS MKT	BID-TRUE ASK-TRUE VAL	2.29	2.17	7.56	2.66			0.64	0.27	0.19	0.2
			2.16	2.24	2.71	2.66		MEAN Std	3.78	2.99	3.76	3.97
	4 NEWVOLUME	RUE VAL	3.66	3.5	4.1	4.75			0.93	1.08	0.34	0.18
S AND ASKS, AN	4 parasites and Bid-true ask-t	BID-TRUE ASK-TRUE VAL	2.92	4.05	4.89	5.68		MEAN Std	3.02	4.31	4.15	3.32
AVERAGE MEAN SQUARED DIFFERENCE OF BIDS AND ASKS, AND TRUE VALUE			2.27	2.76	3.54	3.46			0.68	0.22	0.11	0.15
	C AND 1 NEW	BID-TRUE ASK-TRUE VAL	.45	3.54	4.	11.		Std	7.	2.88	.21	.32
	7 BASI BID-TR	2	~	4	<u>د</u>		MEAN	2				
	MIXED MARKET WITH PARASITES 7 BASIC AND 1 NEWVOLUME BID-TRUE ASK-TRUE VAL BID-TRUE ASK-TRUE VAL	: VAL	7.18	9.29	9.67	9.52			0.91	0.62	0.75	0.32
		BID-TRUE ASK-TRUE   VAL	6.56			9.94	SPREAD	MEAN Std		0.71		
	ICK	SIZE	1.00	0.25	90.0	0.01			1.00	0.25	0.0	0.0

FIG. 22

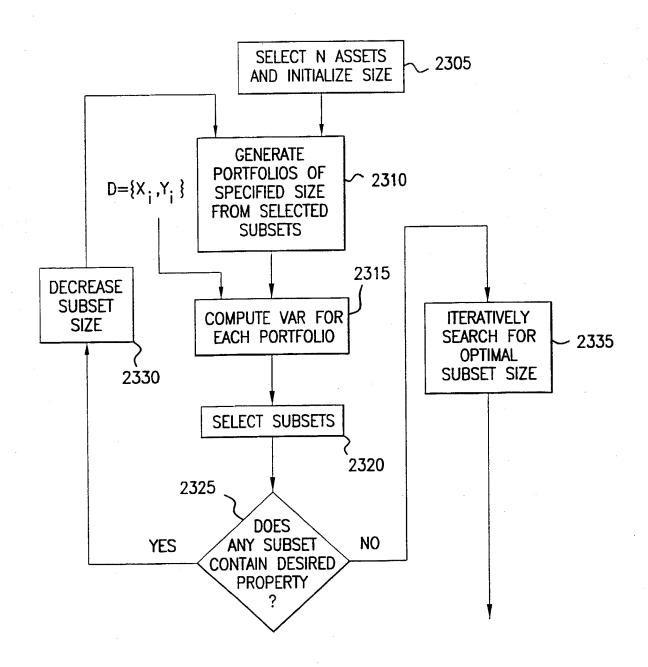
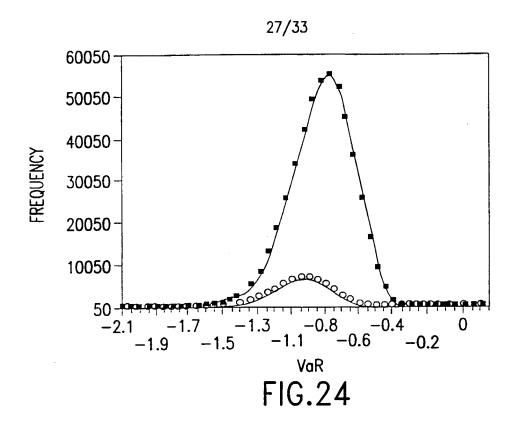
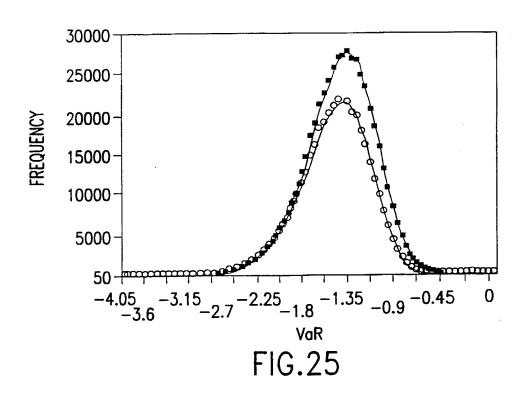


FIG.23





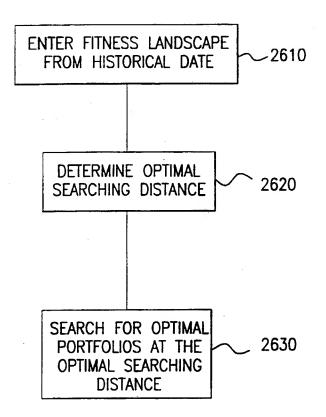


FIG.26

```
\{1, 1, \{2, -1.\}\}
                         \{1, 2, \{1,-1.\}\}
                     {1, 3 {5, -0.629195{{
                     {1, 4, {5, -0.749052{{
 \{3, 5, \{3, -0.629195\}, \{4, -0.749052\}, \{24, -0.350841\}\}
                      }1, 6, {8, -0.3866}}
           \{2, 7, \{8, -0.434322\}, \{9, -0.514114\}\}
   {3, 8, \{6, -0.3866\}, \{7, -0.434322\}, \{9, -0.332176\}}
           \{2, 9, \{7, -0.514114\}, \{8, -0.332176\}\}
             \{2, 10, \{11, -1.\}, \{17, -0.333359\}\}\
              }2, 11, {10, -1.}, {15, -0.311709}}
                   {1, 12, {14, -0.889441{{
                   {1, 13, {14, -0.411215{{
         \{2, 14, \{12, -0.889441\}, \{13, -0.4112215\}\}
\{3, 15, \{11, -0.311709\}, \{17, -0.593436\}, \{18, -0.602979\}\}
          \{2, 16, \{17, -0.503126\}, \{18, -0.52658\}\}
\{3, 17, \{10, -0.333359\}, \{15, -0.593436\}, \{16, -0.503126\}\}
           \{2, 18, \{15, -0.60979\}, \{16, -0.52658\}\}
                       {1, 19, {20, −1.{{
                       \{1, 20, \{19, -1.\}\}
                   {1, 21, {23, -0.770342}}
                   { 1, 22, {23, -0.696416}{
          \{2, 23, \{21, -0.770342\}, \{22, -0.696416\}\}
                    }1, 24, \{5, -0.350841\{\}
          \{2, 25, \{26, -0.491271\}, \{27, -0.459285\}\}
          \{2, 26, \{25, -0.491271\}, \{27, -0.49478\}\}
          \{2, 27, \{25, -0.459285\}, \{26, -0.49478\}\}
                        {1, 28, {29, -1.{{
                       \{1, 29, \{28, -1.\}\}
                    {1, 30, {32, -0.794733}}
                    {1, 31, {32, -0.53383{{
          \{2, 32, \{30, -0.794733\}, \{31, -0.53383\}\}
```

FIG.27

```
\{3., 1\}, \{2., -1.\}, \{47., -0.31\}, \{87., -0.3\}\}
                             \{2., 2., \{1., -1.\}, \{46., -0.31\}\}
                           {2., 3., {5., <u>-0.63</u>}, {80., -0.34}}
{1., 4., {5., <u>-0.75</u>}}
                   \{3., 5, \{3., -.063\}, \{4., -0.75\}, \{24., -0.35\}\}
                                    \{1., 6., \{8., -0.39\}\}\
                            \{2., 7., \{8., -0.43\}, \{9., -0.51\}\}
          \{4., 8., \{6., -0.39\}, \{7., -0.43\}, \{9., -0.33\}, \{44., -0.35\}\}
   \{5., 9., \{7., -0.51\}, \{8., -0.33\}, \{54., -0.3\}, \{75., -0.3\}, \{98., -42\}\}
                  \{3., 10, \{11., -1.\}, \{17., -0.33\}, \{39., -0.36\}\}
                           \{2., 11., \{10., -1\}, \{15., -0.31\}\}
                 \{3., 12., \{14., -0.89\}, \{62., -0.35\}, \{90., -0.3\}\}
        {2., 13., {14., -0.41}, {61., -0.31}} 
{4., 14., {12., -0.89}, {13., -0.41}, {82., -0.32}, {89., -0.35}}
\{5., 15., \{11., -0.31\}, \{17., -0.59\}, \{18., -0.6\}, \{39., -0.31\}, \{80., -0.31\}
                  \{3., 16., \{17., -0.5\}, \{18., -0.53\}, \{82., -0.32\}
        \{4., 17., \{10., -0.33\}, \{15., -0.59\}, \{16., -0.5\}, \{36., -0.38\}\}
                          {2., 18., {15., <u>-0.6</u>}, {16., <u>-0.53</u>}}
{2., 19., {20., <u>-1.</u>}, {42., -0.3}}
                                    {1., 20., {19., <u>-1.</u>}}
                 \{3., 21., \{23., -0.77\}, \{45., -0.32\}, \{94., -0.3\}\}
                          \{2., 22., \{23., -0.7\}, \{97., -0.32\}\}
                          {2., 23., {21., <u>-0.77</u>}, {22., -0.7}} 
{1., 24., {5., -0.35}}
                          \{2., 25., \{26., -0.49\}, \{27., -0.46\}\}
                          {2., 26., {25., -0.49}, {27., -0.49}}
                          2., 27., 25., -0.46, 26., -0.49
                  \{3., 28., \{29., -1.\}, \{48., -0.31\}, \{76., -0.31\}\}
                            \{2., 29., \{28., -1.\}, \{77., -0.3\}\}
                                  {1., 30., {32., <u>-0.79</u>}}
                          {2., 31., {32., <u>-0.53</u>}, {89., -0.31}}
                \{3., 32., \{30., -0.79\}, \{31., -0.53\}, \{46., -0.31\}\}
                         \{2., 33., \{35., -0.46\}, \{39., -0.31\}\}
                                  {1., 34., {36., -0.39}}
        \{4., 36., \{17., -0.38\}, \{34., -0.39\}, \{35., -0.51\}, \{54., -0.33\}\}
                                    {1., 37., {38., <u>-1.</u>}}
                                    {1., 38., {37., <u>-1.</u>}}
        \{4., 39., \{10., -0.36\}, \{15., -0.31\}, \{33., -0.31\}, \{41., -0.49\}\}
                                  {1., 40., {41., <u>-0.79</u>}}
                         \{2., 41., \{39., -0.49\}, \{40., -0.79\}\}
                                   \{1., 42., \{19., -0.3\}\}
                 \{3, 43, \{44, -0.43\}, \{45, -0.4\}, \{69, -0.31\}\}
                 \{3., 44., \}8., -0.35\}, \{43., -0.43\}, \{45., -0.53\}
                 \{3., 45., \{21., -0.32\}, \{43., -0.4\}, \{44., -0.53\}\}
                   \{3., 46., \{2., -0.31\}, \{32., -0.31\}, \{47., -1.\}\}
                            $2., 47., $1., -0.31}, $46., <u>-1.</u>}}
                         \{2., 48., \{28., -0.31\}, \{50., -0.74\}\}
                                  \{\}1., \, 49., \, \{\}50., \, \, \_{\}2\}\\
                          $2., 50., $48., <u>-0.74</u>}, $49., <u>-0.74</u>}}
```

FIG.28A

```
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               {2., 51., {53., <u>-0.62.</u>, {54., <u>-0.57}}</u>}
                                }0, 52.{
               {2., 53., {51., <u>-0.62</u>}, {94., -.38}}
  {4., 54., {9., -0.3}, {36., 0.33}, {51., <u>0.57</u>}, {72., 0.31}}
                         {1., 55., {56., <u>-1.</u>}}
                         {1., 56., {55., <u>-1.</u>}}
               {2., 57., {59., <u>-0.61</u>}, {91., -0.47}}
                       {1., 58., {59., <u>-0.79</u>}}
               {2., 59., {57., <u>-0.61</u>}, {58., <u>-0.79</u>}}
                       {1., 60., {63., -0.45{{}
       \{3., 61., \{13., -0.31\}, \{62., -0.3\}, \{63., -0.36\}\}
       \{3., 62., \{12., -0.35\}, \{61., -0.3\}, \{63., -0.61\}\}
      \{3., 63., \{60., -0.45\}, \{61., -0.36\}, \{62., -0.61\}\}
                         {1., 64., {65., <u>-1.</u>}}
                         {1., 65., {64., <u>-1.</u>}}
                       $1., 66., $68., -0.39}
                       {1., 67., {68., <u>-0.97</u>}}
               {2., 68., {66., -0.39}, {67., <u>-0.97</u>}}
                       $1., 69., $43., -0.31}}
                       {1., 70., {72., -0.45}}
                       {1., 71., {72., <u>-0.63}}</u>
       \{3., 72., \{54., -0.31\}, \{70., -0.45\}, \{71., -0.63\}\}
                         {1., 73., {74., <u>-1.}</u>}
                         {1., 74., {73., <u>-1.</u>}}
                 {2., 75., {9., -0.3}, {77., <u>-0.74}}</u>
               {2., 76., {28., -0.31}, {77., <u>-0.71}}</u>
       \{3., 77., \{29., -0.3\}, \{75., -0.74\}, \{76., -0.71\}\}
        \{3., 78., \{80., -0.65\}, \{81., -0.6\}, \{99., -0.31\}\}
                 $2., 79., $80., <u>-0.5</u>} $81., -0.44}}
\{4., 80., \{3., -0.34\}, \{15., -0.31\}, \{78., -0.65\}, \{79., -0.5\}\}
                {2., 81., {78., <u>-0.6</u>}, {79., -0.44}}
        {3., 82., {14., -0.32}, {16., -0.32}, {83., <u>-1.}</u>}
                         {1., 83., {82., <u>-1.</u>}}
                        1., 84., \{86., \(-0.59\}\)
                        {1., 85., {86., <u>-0.85</u>}}
               {2., 86., {84., <u>-0.59</u>}, {85., <u>-0.85</u>}}
                         \{1., 87., \{1., -0.3\}\}
                                 {0, 88.}
       \{3., 89., \{14., -0.35\}, \{31., -0.31\}, \{90., -0.92\}\}
                 {2., 90., {12., -0.3}, {89., <u>-0.92}</u>}
                        \{1., 91., \{57., -0.47\}\}
                                 }0, 92.}
                                 {0, 93.}
                 \{2., 94., \{21., -0.3\}, \{53., -0.38\}\}
                                 10. 95.
                                 \{0, 96.\}
                        \{1., 97., \{22., -0.32\}\}
                         {1., 98., {9., -0.42}{
                        {1., 99., {78., -0.31}}
                              \{0, 1.0 \times 10^{2}\}
```

FIG.28B

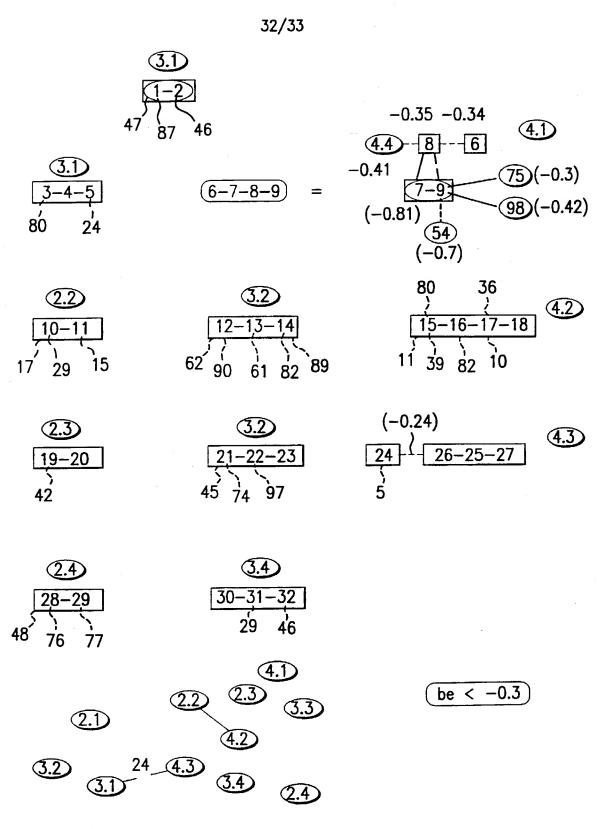
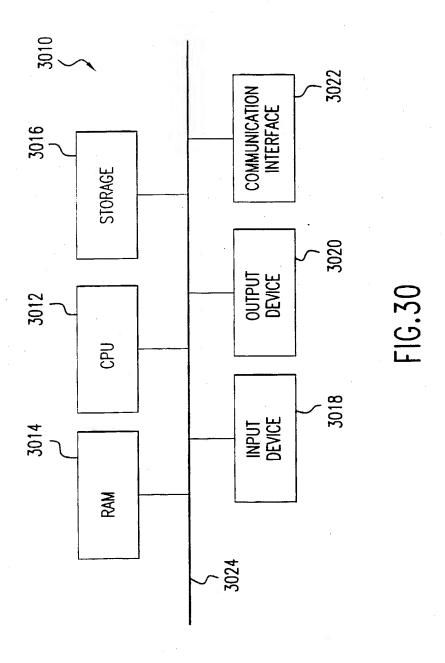


FIG.29



## DECLARATION FOR NON-PROVISIONAL PATENT APPLICATION

As a below named inventor. I hereby declare that:

My residence, post office address and citizenship are as stated below at 201 et seq. beneath my name.

I believe I am the original, first and sole inventor if only one name is listed at 201 below, or an original, first and joint inventor if plural names are listed at 201 et seq. below, of the subject matter which is claimed and for which a patent is sought on the invention entitled

# A SYSTEM AND METHOD FOR THE ANALYSIS AND PREDICTION OF ECONOMIC MARKETS

and for which a patent application:

□ is attached hereto and includes amendment(s) filed on (if applicable)

was filed in the United States on June 22, 2001 as Application No. 09/868,981 (for declaration not accompanying application)

with amendment(s) filed on (if applicable)

was filed as PCT international Application No. PCT/US99/30640 on December 22, 1999 and was amended under PCT Article 19 on of

I hereby state that I have reviewed and understand the contents of the above identified application, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose information known to me to be material to patentability as defined in Title 37, Code of Federal Regulations, §1.56.

I hereby claim foreign priority benefits under Title 35, United States Code, §119(a)-(d) of any foreign application(s) for patent or inventor's certificate listed below and have also identified below any foreign application for patent or inventor's certificate having a filing date before that of the application on which priority is claimed:

EARLIEST FOREIGN APPLICA	TION(S), IF ANY, FILED PR	OR TO THE FILING DATE	OF THE APPLICATION
APPLICATION NUMBER	COUNTRY	DATE OF FILING (day, month, year)	PRIORITY CLAIMED
			YES - NO -
			YES D NO D
			YES - NO -

I hereby claim the benefit under Title 35, United States Code, §119(e) of any United States provisional application(s) listed below.

PROVISIONAL APPLICATION NUMBER	FILING DATE
60/113,502	December 22, 1998
1	·
-	

I hereby claim the benefit under Title 35, United States Code, §120 of any United States application(s) listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States application in the manner provided by the first paragraph of Title 35, United States Code §112, I acknowledge the duty to disclose information known to me which is material to patentability as defined in Title 37, Code of Federal Regulations, §1.56 which became available between the filing date of the prior application and the national or PCT international filing date of this application:

NON-PROVISIONAL APPLICATION SERIAL NO.	FILING DATE	STATUS			
THE ELECTRON SERVER NO.		PATENTED	PENDING	ABANDONED	
PCT/US99/30640	December 22, 1999		X		

Groups only when the application is assigned to a company, partnership or other organization

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		SIGNATURE OF INVENTOR 205		DATE	

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	POST OFFICE ADDRESS	STREET 794 Calle Altamira	CITY Santa Fe	STATE OR COUNTRY	ZIP CODE 87501
		SIGNATURE OF INVENTOR 204	9=3	DATE (1)/10/2	o1)
	FULL NAME OF INVENTOR	LAST NAME	FIRST NAME	MIDDLE NAME	
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	POST OFFICE ADDRESS	STREET	CITY	STATE OR COUNTRY	ZIP CODE
•		SIGNATURE OF INVENTOR 205		DATE	

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	FULL NAME OF INVENTOR	LASY HAME KAUPFMAN	FORT NAME STUART	MEDDLE NAME A.	
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	FULL NAME OF INVENTOR	LAST NAME PALMER	FILET NAME Richard	MLDOCUS HANGE G.	
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		Dand Titel	-	10.04.200	

P

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	FULL NAME OF INVENTOR	LAST NAME KAUFFMAN	FIRST NAME Stuart	MIDDLE NAME A.	
2 0 1	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSHI United States	P
	POST OFFICE ADDRESS	street 1811 S. Camijno Cruz Blanca	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
'		SIGNATURE OF POVENTOR 201		DATE	<u> </u>
		Stelle	A. T.	9-28-20	c/
	FULL NAME OF INVENTOR	LAST NAME MACREADY	FIRST NAME William	MIDDLE NAME G.	
2 0 2	RESIDENCE & CITIZENSHIP	спу Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSHI Canada	P
	POST OFFICE ADDRESS	street 339½-Delgado	Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 202		DATE	
	FULL NAME OF INVENTOR	LAST NAME PALMER	FIRST NAME Richard	MIDDLE NAME G.	
2 0 3	RESIDENCE & CITIZENSHIP	city Durham	STATE OR FOREIGN COUNTRY NC	COUNTRY OF CITIZENSHI United Kingdom	P
	POST OFFICE ADDRESS	STREET 4030 Forestdale Drive	CITY Durham	STATE OR COUNTRY NC	ZIP CODE 27712
	e .	SIGNATURE OF INVENTOR 203		DATE	
	FULL NAME OF INVENTOR	LAST NAME COWAN	FIRST NAME Jack	MIDDLE NAME D.	
2 0 4	RESIDENCE & CITIZENSHIP	CITY Chicago	STATE OR FOREIGN COUNTRY IL	COUNTRY OF CITIZENSHI United States	P
	POST OFFICE ADDRESS	5448 Ridgewood Court	CITY Chicago	STATE OR COUNTRY  IL	ZIP CODE 60615
		SIGNATURE OF INVENTOR 204  Jeele D. C	iowa)	DATE 11/30/01	
	FULL NAME OF INVENTOR	LAST NAME TEILTELBAUM	first name Daniel	MIDDLE NAME	
2 0 5	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSHI United States	p
	POST OFFICE ADDRESS	STREET 618 Old Santa Fe Trail #G	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 205		DATE	



#### IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

Application of: Stuart A. KAUFFMAN et al.

U.S. Application No.: 09/868,981

U.S. Application Filing Date: June 22, 2001

Group Art Unit: To be assigned

on Application Fining Date, June 22, 2001

International Application No.: PCT/US99/30640

Examiner: To be assigned

International Application Filing Date:

Decamber 22, 1999

For: A SYSTEM AND METHOD FOR THE

ANALYSIS AND PREDICTION OF

ECONOMIC MAILKETS

Attorney Docket No.: 9392-016-999

#### CONSENT BY THE ASSIGNEE UNDER 37 C.F.R. 6 1.497(d)

Assistant Commissioner for Patents Washington, D.C. 20231

Sir:

Bios Oroup, Inc., having a place of business at 317 Pasco de Perulta, Santa Fe, New Mexico 87501, as Assignee of the enthre right, title and interest in, to and under the U.S. application filed on June 22, 2001 entitled "A SYSTEM AND METHOD FOR THE ANALYSIS AND PREDICTION OF ECONOMIC MARKETS" hereby consents to the addition of Vince M. Darley as a named inventor in U.S. application no. 09/868,981.

Bios Group, Inc., certifies that it is the Assignee of the entire right, title and interest in, to and under U.S. Application, 09/868,981 pursuant to the assignment executed by Stuart A. Kauffman, William G. Macready, Richard G. Palmer, Jack D. Cowan, Daniel Teitelbaum, Alexander Outkin, Bruce K. Sawhill, Vladimir G. Makhankov and Vince M. Darley. Documentary evidence of a chain of title from the original owner to the assignee is indicated by the enclosed copy of the assignment.

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and

fluther that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the Patent.

Signed this 18 day of January 2001.

Bios Group, Inc.

Pobert P. MecDonald

Title: President

#### IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

Application of: Stuart A. KAUFFMAN et al.

U.S. Application No.: 09/868,981

Group Art Unit: To be assigned

U.S. Application Filing Date: June 22, 2001

International Application No.: PCT/US99/30640

Examiner: To be assigned

International Application Filing Date:

December 22, 1999

For: A SYSTEM AND METIIOD FOR THE

ANALYSIS AND PREDICTION OF

ECONOMIC MARKETS

Attorney Docket No.: 9392-016-999

## STATEMENT OF VINCE M. DARLEY UNDER 37 C.F.R. 6 1.497(d)

Assistant Commissioner for Patents Washington, D.C. 20231

Sir:

l, Vince M. Darley, hereby state that I was mistakenty not included as a mained inventor of international application US99/30640 and that this error in inventorship in this international application occurred without any deceptive intention on my part.

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true, and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment or both, under section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the patent.

Date: 21 Jan 2002

Vince M. Darley

DC1 - 312124 1

#### ASSIGNMENT

WHEREAS, WE,

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Stuart A. KAUFFMAN, a citizen of the United States, residing at 1811 S. Camino Cruz Blanca, Santa Fe, New Mexico 87501;

William G. MACREADY, a citizen of Canada, residing at 339½ Delgado, Santa Fe, New Mexico 87501:

Richard G. PALMER, a citizen of the United Kingdom, residing at 4030 Forestdale Drive, Durham, North Carolina 27712;

Jack D. COWAN, a citizen of the United States, residing at 5448 Ridgewood Court, Chicago, Illinois 60615;

Daniel TELETELBAUM, a citizen of the United States, residing at 618 Old Santa Fe Trail #G, Santa Fe, New Mexico 87501; TELEBAUM

Alexander OUTKIN, a citizen of Russia, residing at 1548 Avida de Las Americas, Santa Fe, New Mexico 87501;

Bruce K. SAWHILL, a citizen of the United States, residing at 1028 Don Cubero, Santa Fe, New Mexico 87501;

Vladimir G. MAKHANKOV, a citizen of Russia, residing at 4148 Chaparron Place, Santa Fe, New Mexico 87501; and

Vince M. DARLEY, a citizen of the United Kingdom, residing at 794 Calle Altamira, Santa Fe, New Mexico 87501;

are the inventors of the invention in A SYSTEM AND METHOD FOR THE ANALYSIS AND PREDICTION OF ECONOMIC MARKETS for which we have executed an application for a Patent of the United States

	which is executed on		even date herewith or		
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which is identified by Pennie & Edmonds 

docket no. 9392-016-999

which is identified by Pennie & Edmonds

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which is identified by Pennie & Edmonds

pur docket no. 9392-016-999

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which was filed on June 22, 2001, Application No. 09/868,981

and WHEREAS, Bios Group, Inc., having a business address of 317 Paseo de Peralta, Santa Fe, New Mexico 87501, ASSIGNEE is desirous of obtaining our entire right, title and interest in, to and under the said invention and the said application:

NOW, THEREFORE, in consideration of the sum of One Dollar (\$1.00) to us in hand paid, and other good and valuable consideration, the receipt of which is hereby acknowledged, we, the said ASSIGNORS, have sold, assigned, transferred and set over, and by these presents do hereby sell, assign, transfer and set over, unto the said ASSIGNEE, its successors, legal representatives and assigns, our entire right, title and interest in, to and under the said invention, and the said United States application and all divisions, renewals and continuations thereof, and all Patents of the United States which may be granted thereon and all reissues and extensions thereof; and all applications for industrial property protection, including, without limitation, all applications for patents, utility models, and designs which may hereafter be filed for said invention in any country or countries foreign to the United States, together with the right to file such applications and the right to claim for the same the priority rights derived from said United States application under the Patent Laws of the United States, the International Convention for the Protection of Industrial Property, or any other international agreement or the domestic laws of the country in which any such application is filed, as may be applicable; and all forms of industrial property protection, including, without limitation, patents, utility models, inventors' certificates and designs which may be granted for said invention in any country or countries foreign to the United States and all extensions, renewals and reissues thereof;

AND WE HEREBY authorize and request the Commissioner of Patents and Trademarks of the United States, and any Official of any country or countries foreign to the United States, whose duty it is to issue patents or other evidence or forms of industrial property protection on applications as aforesaid, to issue the same to the said ASSIGNEE, its successors, legal representatives and assigns, in accordance with the terms of this instrument.

AND WE HEREBY covenant and agree that we have full right to convey the entire interest herein assigned, and that we have not executed, and will not execute, any agreement in conflict herewith.

AND WE HEREBY further covenant and agree that we will communicate to the said ASSIGNEE, its successors, legal representatives and assigns, any facts known to us respecting said invention, and testify in any legal proceeding, sign all lawful papers, execute all divisional, continuing, reissue and foreign applications, make all rightful oaths, and generally do everything possible to aid the said ASSIGNEE, its successors, legal representatives and assigns, to obtain and enforce proper protection for said invention in all countries.

My Commission Expires 120, 20, 2004

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### POWER OF ATTORNEY

## IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

Application of: Stuart A. KAUFFMAN et al.

Application No.: 09/868,981

Group Art Unit: To Bc Assigned

Filed: June 22, 2001

Examiner: To Be Assigned

For:

A SYSTEM AND METHOD FOR

THE ANALYSIS AND

PREDICTION OF ECONOMIC

**MARKETS** 

Attorney Docket No.: 9392-016-999

# POWER OF ATTORNEY BY ASSIGNEE AND EXCLUSION OF INVENTOR(S) UNDER 37 C.F.R. 3,71

Assistant Commissioner for Patents Washington, D.C. 20231

Sir:

The undersigned assignee of the entire interest in the above-identified subject application hereby appoints: Berj A. Terzian (Reg. No. 20060), David Weild, III (Reg. No. 21094), Jonathan A. Marshall (Reg. No. 24614), Barry D. Rein (Reg. No. 22411), Stanton T. Lawrence, III (Reg. No. 25736), Charles E. McKenney (Reg. No. 22795), Philip T. Shannon (Reg. No. 24278), Francis E. Morris (Reg. No. 24615), Charles E. Miller (Reg. No. 24576), Gidon D. Stern (Reg. No. 27469), John J. Lauter, Jr. (Reg. No. 27814), Brian M. Poissant (Reg. No. 28462), Brian D. Coggio (Reg. No. 27624), Rory J. Radding (Reg. No. 28749), Stephen J. Harbulak (Reg. No. 29166), Donald J. Goodell (Reg. No. 19766), James N. Palik (Reg. No. 25510), Thomas E. Friebel (Reg. No. 29258), Laura A. Coruzzi (Reg. No. 30742), Jennifer Gordon (Reg. No. 30753), Geraldine F. Baldwin (Reg. No. 31232), Victor N. Balancia (Reg. No. 31231), Samuel B. Abrams (Reg. No. 30605), Steven I. Wallach (Reg. No. 35402), Marcia H. Sundeen (Rog. No. 30893), Paul J. Zegger (Reg. No. 33821), Edmond R. Bannon (Reg. No. 32110), Bruce J. Barker (Reg. No. 33291), Adriane M. Antler (Reg. No. 32605), Thomas G. Rowan (Reg. No. 34419), James G. Markey (Reg. No. 31636), Thomas D. Kohler (Reg. No. 32797), Scott D. Stimpson (Reg. No. 33607), Gary S. Williams (Reg.

und de la companya de

#### POWER OF ATTORNEY

No. 31066), Ann L. Gisolfi (Reg. No. 31956), Todd A. Wagner (Reg. No. 35399), Scott B. Familiant (Reg. No. 35514), Kelly D. Talcott (Reg. No. 39582), Francis D. Cerrito (Reg. No. 38100), Anthony M. Insogna (Reg. No. 35203), Brian M. Rothery (Reg. No. 35340), Brian D. Siff (Reg. No. 35679), Alan Tenenbaum (Reg. No. 34939), Michael J. Lyons (Reg. No. 37,386), Garland T. Stephens (Reg. No. 37,242) and William J. Sipio (Reg. No. 34,514), all of Pennie & Edmonds LLP, whose addresses are 1155 Avenue of the Americas, New York, Now York 10036, 1667 K Street N.W., Washington, DC 20006 and 3300 Hillview Avenue, Palo Alto, CA 94304, all of Pennie & Edmonds LLP (PTO Customer No. 20582), as its attorneys to prosecute this application and to transact all business in the United States Patent and Trademark Office connected therewith, said appointment to be to the exclusion of the inventors and their attorney(s) in accordance with the provisions of 37 C.F.R. 3.71, provided that, if any one of these attorneys ceases being affiliated with the law firm of Pennie & Edmonds LLP as partner, counsel, or employee, then the appointment of that attorney and all powers derived therefrom shall terminate on the date such attorney ceases being so affiliated.

An assignment of the entire interest in the above-identified subject application:

at reel/frame \_\_\_/\_.

Please direct all correspondence for this application to customer no. 20582.

ASSIGNEE:

Bios Group Inc.

Signature:

Typed Name:

Robert R. MacDonald

Position/Title:

President

Address:

317 Paseo de Peralta

Santa Fc. New Mexico 87501

Date:

12/5/01

[]

[X]

was recorded on

is submitted herewith for recording.

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## DECLARATION FOR NON-PROVISIONAL PATENT APPLICATION'

As a below named inventor, I hereby declare that:

My residence, post office address and citizenship are as stated below at 201 et seq. beneath my name.

I believe I am the original, first and sole inventor if only one name is listed at 201 below, or an original, first and joint inventor if plural names are listed at 201 et seq. below, of the subject matter which is claimed and for which a patent is sought on the invention entitled

## A SYSTEM AND METHOD FOR THE ANALYSIS AND PREDICTION OF ECONOMIC MARKETS

and for which a patent application:

□ is attached hereto and includes amendment(s) filed on (if applicable)

was filed in the United States on June 22, 2001 as Application No. 09/868,981 (for declaration not accompanying application)

with amendment(s) filed on (if applicable)

was filed as PCT international Application No. PCT/US99/30640 on December 22, 1999 and was amended under PCT Article 19 on of

I hereby state that I have reviewed and understand the contents of the above identified application, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose information known to me to be material to patentability as defined in Title 37, Code of Federal Regulations, §1.56.

I hereby claim foreign priority benefits under Title 35, United States Code, \$119(a)-(d) of any foreign application(s) for patent or inventor's certificate listed below and have also identified below any foreign application for patent or inventor's certificate having a filing date before that of the application on which priority is claimed:

EARLIEST FOREIGN APPLICA	TION(S), IF ANY, FILED PRI	OR TO THE FILING DATE (	OF THE APPLICATION	
APPLICATION NUMBER	COUNTRY	DATE OF FILING (day, month, year)	PRIORITY CLAIMED	
			YES □ NO □	
			YES - NO -	
			YES - NO -	

I hereby claim the benefit under Title 35, United States Code, §119(e) of any United States provisional application(s) listed below.

PROVISIONAL APPLICATION NUMBER	FILING DATE
60/113,502	December 22, 1998

I hereby claim the benefit under Title 35, United States Code, §120 of any United States application(s) listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States application in the manner provided by the first paragraph of Title 35, United States Code §112, I acknowledge the duty to disclose information known to me which is material to patentability as defined in Title 37, Code of Federal Regulations, §1.56 which became available between the filing date of the prior application and the national or PCT international filing date of this application:

NON-PROVISIONAL	EW ING DAME	STATUS			
APPLICATION SERIAL NO.	FILING DATE	PATENTED	PENDING	ABANDONED	
PCT/US99/30640	December 22, 1999		X		

<sup>\*</sup> for use only when the application is assigned to a company, partnership or other organization.

may	J1				
	FULL NAME OF INVENTOR	LAST NAME KAUFFMAN	FIRST NAME Stuart	MIDDLE NAME A.	
2 0 1	RESIDENCE & CITIZENSHIP	Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSH United States	IP
)	POST OFFICE ADDRESS	STREET 1811 S. Campno Cruz Blanca	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
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		SIGNATURE OF INVENTOR 202		DATE	
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$\begin{bmatrix} 2 \\ 0 \\ 3 \end{bmatrix}$	RESIDENCE & CITIZENSHIP	CITY Durham	STATE OR FOREIGN COUNTRY NC	COUNTRY OF CITIZENSH United Kingdom	
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		SIGNATURE OF INVENTOR 203 Richard GF	Mus	/ 0 ~ 2 - 2	2001
	FULL NAME OF INVENTOR	LAST NAME COWAN	FIRST NAME _Jack	MIDDLE NAMED.	
2 0 4	RESIDENCE & CITIZENSHIP	CITY Chicago	STATE OR FOREIGN COUNTRY  IL	COUNTRY OF CITIZENSH United States	IP
	POST OFFICE ADDRESS	STREET 5448 Ridgewood Court	CITY Chicago	STATE OR COUNTRY IL	ZIP CODE 60615
		SIGNATURE OF INVENTOR 204		DATE	
	FULL NAME OF INVENTOR	LAST NAME TEILTELBAUM	FIRST NAME Daniel	MIDDLE NAME	-
2 0 5	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSH United States	IP
	POST OFFICE ADDRESS	STREET 618 Old Santa Fe Trail #G	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
·		SIGNATURE OF INVENTOR 205		DATE	<del></del>

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I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issuing thereon. LAST HAME POLETHAND MEDDLE HAME FULL NAME OF INVENTOR OUTKIN Alexander 2 CITY STATE OR FORBION COUNT COUNTRY OF CITEZENSHIP 0 RESIDENCE & Santa Fe NM Russin CITIZENSHIP 6 STALET **arx** STATE OR COUNTRY DI COOK POST OFFICE 1548 Avida de Las Americas Santa Fe NM 87501 ADDRESS SIGNATURE OF INVENTOR 201 Stexander 9/28/01 LAST NAME COCT NAME MIDDLE NAME **FULL NAME** SAWHILI Bruce K. OF INVENTOR STATE OR FORMON COUNTRY RESIDENCE & CITIZENSHIP COLWERT OF COTTON HOLD Samu Ec NM United States TRACT CITY STATE OR COUNTRY to cook POST OFFICE 87501 1028 Don Cubaro Santa Fe NM **ADDRESS** SIGNATURE OF INVENTOR 102 LAST NAME PIRIT HAME NOTICLE NAME FULL NAME MAKHANKOV Vladimir G. OP INVENTOR STATE OR FOREIGN COUNTY COUNTRY OF CITIZONSHIP residence & Some Fe NM Russia CITIZENSHIP STRUCT STATE OR COUNTRY ZIF CODE POST OFFICE 4148 Chaparron Place Senta Fe ADDRESS NM 87501 SIGNATURE OF INVENTOR 141 12/06/2001 LAST NAME HTOOLE NAME FULL NAME DARLEY Visice OF INVENTOR ary STATE OR FOREIGN COUNTRY COUNTRY OF CITIZENSHIP RESIDENCE & Santa Fo MM United Kingdom CITEZENSHIP POST OFFICE ĊΩΥ STATE OR COUNTRY ET COOR 794 Calle Altamira ADDRESS Santa Fe NM 87501 LASTNAKK FORET NUME MEDBLENAME **FULL NAME** 

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	POST OFFICE ADDRESS	rreter 1548 Avida de Las Americas	crry Santa Fe	STATE OR COUNTRY NM	87501
	×	Hexander L	antein	9/28/01	
	FULL NAME OF INVENTOR	SAWHILL	Bruce Bruce	K.	- <b></b>
7	RESIDENCE & CITIZENSHIP	Santa Fe	NM "	Colorrer or controls of United States	हिंग्से हरा प्रस्ता । -
	POST OFFICE ADDRESS	1028 Don Cubara	CITY Santa Fe	NM	211 COOL 87501
		Bulkaribes of physician 101	20	9/28/2	00 /
	FULL NAME OF INVENTOR	MAKHANKOV CUETHUME	Past Habel Vladiant	G.	
2 0 8	RESIDENCE & CITIZENSHIP	city Santa Fe	NW STATE OR PORTION COUNTRY	COUNTRY OF CITIZENSMI Russia	
	POST OFFICE ADDRESS	arker 4148 Chaparron Place	Santa Fe	STATE OR COUNTRY NM	ш соос 87501
	·	SIGNATURE OF INVENTOR 201		12/06/	2001
	FULL NAME OF INVENTOR	LATRAME DARLEY	PILST NAME VÍJICO	ниюсе каме М.	
0 9	RESIDENCE &	OTY Senta Fe	FTATE OF FOREIGN COUNTRY	Country of contrastor	
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2 0 10	RESIDENÇE & CITIZENSHIP	an	STATE OR PORTION COUNTRY	COUNTRY OF CHURCH HIP	
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	FULL NAME OF INVENTOR	LAST NAME OUTKIN	FIRST NAME Alexander	MIDDLE NAME	
· 2 0 6	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSII Russia	1P
	POST OFFICE ADDRESS	1548 Avida de Las Americas	Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 201 Alexander	Outris	9/28/0 <sub>1</sub>	,
	FULL NAME OF INVENTOR	LAST NAME SAWHILL	FIRST NAME Bruce	MIDDLE NAME K.	
2 0 7	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSH United States	IP .
	POST OFFICE ADDRESS	STREET  1028 Don Cubero	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 202	20	9/28/2	200/
	FULL NAME OF INVENTOR	LAST NAME MAKHANKOV	FIRST NAME Vladimír	MIDDLE NAME G.	
2 0 8	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSHI Russia	P
	POST OFFICE ADDRESS	street 4148 Chaparton Place	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 203		DATE	
	FULL NAME OF INVENTOR	LAST NAME DARLEY	FIRST NAME Vince	MIDDLE NAME M.	
2 0 9	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSHIP United Kingdom	
	POST OFFICE ADDRESS	street 794 Calle Altamira	CITY Santa Fe	STATE OR COUNTRY	ZIP CODE 87501
 		SIGNATURE OF INVENTOR 204	97=3	DATE 11 /10 /2	or )
	FULL NAME OF INVENTOR	LAST NAME	FIRST NAME	MIDDLE NAME	
2 0 10	RESIDENCE & CITIZENSHIP	CITY	STATE OR FOREIGN COUNTRY	COUNTRY OF CITIZENSHI	P
	POST OFFICE ADDRESS	STREET	СПУ	STATE OR COUNTRY	ZIP CODE
•		SIGNATURE OF INVENTOR 105		DATE	

	FULL NAME OF INVENTOR	LAST NAME KAUFFMAN	FIRST NAME Stuart	MIDDLE NAME A.	
2 0 1	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSE United States	IIP
	POST OFFICE ADDRESS	STREET 1811 S. Caprimo Cruz Blanca	Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF EVENTOR 201	fe-	9-28-20	c/
	FULL NAME OF INVENTOR	LAST NAME MACREADY	FIRST NAME William	MIDDLE NAME G.	
2 0 2	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	country of citizensh Canada	IIP
	POST OFFICE ADDRESS	street 339½-Delgado	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 202		DATE	
	FULL NAME OF INVENTOR	LAST NAME PALMER	FIRST NAME Richard	MIDDLE NAME G.	
2 0 3	RESIDENCE & CITIZENSHIP	CITY Durham	STATE OR FOREIGN COUNTRY NC	COUNTRY OF CITIZENSHIP United Kingdom	
	POST OFFICE ADDRESS	STREET 4030 Forestdale Drive	спү Durham	STATE OR COUNTRY NC	ZIP CODE 27712
•		SIGNATURE OF INVENTOR 203		DATE	
	FULL NAME OF INVENTOR	LAST NAME COWAN	FIRST NAME  Jack	MIDDLE NAME D.	<u> </u>
2 0 4	RESIDENCE & CITIZENSHIP	CITY Chicago	STATE OR FOREIGN COUNTRY  IL	COUNTRY OF CITIZENSHIP United States	
	POST OFFICE ADDRESS	STREET 5448 Ridgewood Court	CITY Chicago	STATE OR COUNTRY IL	ZIP CODE 60615
		SIGNATURE OF INVENTOR 204		DATE	
	FULL NAME OF INVENTOR	LAST NAME TE ITELISAUM TEIKTELBAUM D.T.	FIRST NAME Daniel	MIDDLE NAME	
2 0 5	RESIDENCE & CITIZENSHIP	Santa Fo ARLINGTON	STATE OR FOREIGN COUNTRY	COUNTRY OF CITIZENSH United States	P
	POST OFFICE ADDRESS	STREET 4001 N・9上 井(314 618 Old Santa Fe Trail #G	Santa Fe	STATE OR COUNTRY NM VA	2IP CODE 87501- 2220 3
		SIGNATURE OF INVENTOR 205		DATE (0 · 04 · 200	ı

	FULL NAME	LAST NAME KAUFFMAN	FIRST NAME Stuart	MIDDLE NAME A.	
2	OF INVENTOR  RESIDENCE &	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSHI United States	P
l	POST OFFICE	STREET 1811 S. Caprijno Cruz Blanca	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
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		State	fer	9-28-20	c1
	FULL NAME OF INVENTOR	LAST NAME MACREADY	FIRST NAME William	MIDDLE NAME G.	
2 0 2	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSHI Canada	Р
	POST OFFICE ADDRESS	street 339½ Delgado	CITY Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 202		DATE	
	FULL NAME OF INVENTOR	LAST NAME PALMER	FIRST NAME Richard	MIDDLE NAME G.	
2 0 3	RESIDENCE & CITIZENSHIP	CITY Durham	STATE OR FOREIGN COUNTRY NC	COUNTRY OF CITIZENSHIP United Kingdom	
	POST OFFICE ADDRESS	street 4030 Forestdale Drive	CITY Durham	STATE OR COUNTRY NC	ZIP CODE 27712
		SIGNATURE OF INVENTOR 203 Richard G Pa	lner	DATE 10~ 2 2	00 l
	FULL NAME OF INVENTOR	LAST NAME COWAN	FIRST NAME  Jack	MIDDLE NAME D.	
2 0 4	RESIDENCE & CITIZENSHIP	спу Chicago	STATE OR FOREIGN COUNTRY  IL	COUNTRY OF CITIZENSHIP United States	
	POST OFFICE ADDRESS	STREET 5448 Ridgewood Court	CITY Chicago	STATE OR COUNTRY  IL	ZIP CODE 60615
		SIGNATURE OF INVENTOR 204		DATE	
	FULL NAME OF INVENTOR	LAST NAME TEILTELBAUM	FIRST NAME Daniel	MIDDLE NAME	,
2 0 5	RESIDENCE & CITIZENSHIP	спү Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSHIR United States	
	POST OFFICE ADDRESS	STREET 618 Old Santa Fe Trail #G	CITY Santa Fe	STATE OR COUNTRY NM	ziр собе 87501
		SIGNATURE OF INVENTOR 205		DATE	
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	FULL NAME OF INVENTOR	LASTHANE KAUPFMAN	FULLY HANGS Squart	мерыя ныла А.	
2 0 1	RESIDENCE & CITIZENSHIP	CITY Santa Fc	STATE OR MOREION COUNTRY NM	COUNTRY OF CITED/HIP United States	
	POST OFFICE ADDRESS	1811 S. Commo Cruz Blanca	CTT SANTA Po	STATE OR COUNTRY NM	21° CODE 87501
		SIGNATURE OF PRVENTOR SUI	f.	9-28-20	c/
	FULL NAME OF INVENTOR	MACREADY	mst have William	MEDICE NAMES  G.	
2 0 2	RESIDENCE & CITIZENSHIP	City Santa Fe	STATE OR POREIGN COLDITARY NIM	Canada	,
	POST OFFICE ADDRESS	# Coming School	erre Santa Fe	NM	8750T 87505
	,	William G. Mac	realy	Dec S	701
	FULL NAME OF INVENTOR	LAST NAME PALMER	FILET MAINS Richard	MIDDUS HAME G.	
2 0 3	RESIDENCE & CITIZENSHIP	cny Durhem	STATE OR FOREIGN COLUMNY NC	COUNTRY OF CITEDUSHIP United Kingdom	
_	POST OFFICE ADDRESS	4030 Forestdale Drive	CITY Durtham	STATE OR COUNTRY NC	27712
		BIGNATURE OF INVENTOR 101		DATE	
	FULL NAME OF INVENTOR	COWAN	THET NAME  Jack	MIDOLENAIA : D.	
2 0 4	RESIDENCE & CITIZENSHIP	ary Chlcago	STATE OR FOREIGH COUNTRY  IL	COUNTRY OF CHIZZENSUS United States	
	POST OFFICE ADDRESS	STRIET 5448 Ridgewood Court	cmy Chicago	STATE OR COUNTRY  IL	2n CODE 60615
		SICHATURE OF INVENTIOR 204		DATE	
	FULL NAME OF INVENTOR	TELEFICIALIN D.T.	PRSTHAME Daniel	HUDOLE HAME	
2 0 5	RESIDENCE &	CONTRA ARLIHOTON	STATE OF FORCION COUNTRY	COUNTRY OF CITEZONING United States	
	POST OFFICE ADDRESS	STREET 4061 N・4世 社(314) 410 014 South Po Treff #6	on Aprincial	STATE OR COUNTRY	## cook ## 2550 3
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	FULL NAME OF INVENTOR	LAST NAME KAUFFMAN	FIRST NAME Stuart	MIDDLE NAME A.	
2 0 1	RESIDENCE & CITIZENSHIP	city Santa Fe	STATE OR FOREIGN COUNTRY  NM	COUNTRY OF CITIZENSHIP United States	
	POST OFFICE ADDRESS	street 1811 S. Camino Cruz Blanca	Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 201	f.	9-28-20	, cı
_	FULL NAME OF INVENTOR	LAST NAME MACREADY	FIRST NAME William	MIDDLE NAME G.	
2 0 2	RESIDENCE & CITIZENSHIP	CITY Santa Fe	STATE OR FOREIGN COUNTRY NM	COUNTRY OF CITIZENSE  Canada	ПР
	POST OFFICE ADDRESS	street 339½-Delgado	спү Santa Fe	STATE OR COUNTRY NM	ZIP CODE 87501
		SIGNATURE OF INVENTOR 202		DATE	
2 0 3	FULL NAME OF INVENTOR	LAST NAME PALMER	FIRST NAME Richard	MIDDLE NAME G.	
	RESIDENCE & CITIZENSHIP	CITY Durham	STATE OR FOREIGN COUNTRY NC	COUNTRY OF CITIZENSHIP United Kingdom	
	POST OFFICE ADDRESS	street 4030 Forestdale Drive	спу Durham	STATE OR COUNTRY NC	ZIP CODE 27712
		SIGNATURE OF INVENTOR 203		DATE	
	FULL NAME OF INVENTOR	LAST NAME COWAN	FIRST NAME  Jack	MIDDLE NAME D.	
2 0 4	RESIDENCE & CITIZENSHIP	CITY Chicago	STATE OR FOREIGN COUNTRY  IL	COUNTRY OF CITIZENSHIP United States	
	POST OFFICE ADDRESS	STREET 5448 Ridgewood Court	спу Chicago	STATE OR COUNTRY IL	ZIP CODE 60615
		SIGNATURE OF INVENTOR 204		DATE A	
	FULL NAME OF INVENTOR	LAST NAME TE ITELSATUM TEIKTELBAUM D.T.	FIRST NAME Daniel	MIDDLE NAME	
2 0 5	RESIDENCE & CITIZENSHIP	CITY GARLLA EC ARLINGTON	STATE OR FOREIGN COUNTRY -NM VA	COUNTRY OF CITIZENSHI United States	P
	POST OFFICE ADDRESS	STREET 4001 N.94 #1314 618 Old Santa Fe Trail #6	CITY ARY METER	STATE OR COUNTRY  NH Vf)	21P CODE 87501-7220 3
		SIGNATURE OF INVENTOR 20:		0 · 04 · 200	1

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